

relax

Version 3.1.2



Molecular dynamics by  
NMR data analysis

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# Abbreviations

**AIC:** Akaike's Information Criteria (model selection method)

**AICc:** small sample size corrected AIC (model selection method)

**API:** application programming interface

**ANOVA:** analysis of variance (field of statistics)

**BC:** back calculation

**BIC:** Bayesian Information Criteria (model selection method)

**BFGS:** Broyden-Fletcher-Goldfarb-Shanno (optimisation method)

$C(\tau)$ : correlation function

$\chi^2$ : chi-squared function

**CG:** conjugate gradient (optimisation)

**CPMG:** the Carr-Purcell-Meiboom-Gill pulse sequence

**CR72:** the [Carver and Richards \(1972\)](#) relaxation dispersion model

**CSA:** chemical shift anisotropy

**CV:** cross validation

**CVS:** Concurrent Versions System (open source version control system)

$\mathfrak{D}$ : the set of diffusion tensor parameters

$\mathfrak{D}_{\parallel}$ : the eigenvalue of the spheroid diffusion tensor corresponding to the unique axis of the tensor

$\mathfrak{D}_{\perp}$ : the eigenvalue of the spheroid diffusion tensor corresponding to the two axes perpendicular to the unique axis

$\mathfrak{D}_a$ : the anisotropic component of the Brownian rotational diffusion tensor

$\mathfrak{D}_{iso}$ : the isotropic component of the Brownian rotational diffusion tensor

$\mathfrak{D}_r$ : the rhombic component of the Brownian rotational diffusion tensor

$\mathfrak{D}_{ratio}$ : the ratio of  $\mathfrak{D}_{\parallel}$  to  $\mathfrak{D}_{\perp}$

$\mathfrak{D}_x$ : the eigenvalue of the Brownian rotational diffusion tensor in which the corresponding eigenvector defines the x-axis of the tensor

$\mathfrak{D}_y$ : the eigenvalue of the Brownian rotational diffusion tensor in which the corresponding eigenvector defines the y-axis of the tensor

$\mathfrak{D}_z$ : the eigenvalue of the Brownian rotational diffusion tensor in which the corresponding eigenvector defines the z-axis of the tensor

**DPL94**: the [Davis et al. \(1994\)](#) relaxation dispersion model

**DQ**: double quantum

$\epsilon_i$ : elimination value

**FSF**: Free Software Foundation

**GNU**: GNU's Not Unix!

**GPG**: GNU Privacy Guard (software)

**GPL**: GNU general public licence

**GUI**: graphical user interface

**ID string**: identification string

**IT99**: the [Ishima and Torchia \(1999\)](#) relaxation dispersion model

$J(\omega)$ : spectral density function

**LM63**: the [Luz and Meiboom \(1963\)](#) relaxation dispersion model

**M61**: the [Meiboom \(1961\)](#) relaxation dispersion model

**MC**: Monte Carlo (simulations)

**MD**: molecular dynamics (simulations)

**MMQ**: proton-heteronuclear SQ, ZQ, DQ, and MQ data (multi-multiple quantum)

**MP05**: the [Miloushev and Palmer \(2005\)](#) relaxation dispersion model

**MPI**: message passing interface

**MQ**: multiple quantum

**NMR**: if you do not know this one, do not read further

**NNTP**: network news transfer protocol

**NOE**: nuclear Overhauser effect

**NS**: numeric solution

**ORD**: optical rotatory dispersion

**OS**: operating system

**PCS**: pseudocontact shift

**PDB**: Protein Data Bank



**pdf:** probability distribution function

**PRE:** paramagnetic relaxation enhancement

$r$ : bond length

$R_1$ : spin-lattice relaxation rate

$R_2$ : spin-spin relaxation rate

$R_{ex}$ : chemical exchange relaxation rate

**RDC:** residual dipolar coupling

**RMSD:** root-mean-square deviation

**ROE:** rotating-frame Overhauser effect

**RSDM:** reduced spectral density mapping

**RSS:** rich site summary (web feed format)

$S^2$ ,  $S_f^2$ , and  $S_s^2$ : model-free generalised order parameters

**SVN:** Apache Subversion (open source version control system)

$\tau_e$ ,  $\tau_f$ , and  $\tau_s$ : model-free effective internal correlation times

$\tau_m$ : global rotational correlation time

**TP02:** the [Trott and Palmer \(2002\)](#) relaxation dispersion model

**TAP03:** the [Trott et al. \(2003\)](#) relaxation dispersion model

**TSMFK01:** the [Tollinger et al. \(2001\)](#) relaxation dispersion model

**UI:** user interface

**XML:** extensible markup language

**ZQ:** zero quantum



# Preface - citing relax

The relax project is a large collection of work created by diverse authors. It is a community driven project created by NMR spectroscopists which supports a broad range of dynamics analyses. Care must be taken to properly cite the parts of relax that you use so that the correct authors receive the citations and credit they deserve. The following is a breakdown of all of the citations relating to relax, including the basic citations for the various analysis types.

## The software relax

### relax references

The primary citations for relax are:

- d’Auvergne, E. J. and Gooley, P. R. (2008a). Optimisation of NMR dynamic models I. Minimisation algorithms and their performance within the model-free and Brownian rotational diffusion spaces. *J. Biomol. NMR*, **40**(2), 107–119. ([10.1007/s10858-007-9214-2](https://doi.org/10.1007/s10858-007-9214-2))
- d’Auvergne, E. J. and Gooley, P. R. (2008b). Optimisation of NMR dynamic models II. A new methodology for the dual optimisation of the model-free parameters and the Brownian rotational diffusion tensor. *J. Biomol. NMR*, **40**(2), 121–133. ([10.1007/s10858-007-9213-3](https://doi.org/10.1007/s10858-007-9213-3))

### Graphical user interface reference

The primary citation for the GUI is:

- Bieri, M., d’Auvergne, E., and Gooley, P. (2011). relaxGUI: a new software for fast and simple NMR relaxation data analysis and calculation of ps-ns and  $\mu$ s motion of proteins. *J. Biomol. NMR*, **50**, 147–155. ([10.1007/s10858-011-9509-1](https://doi.org/10.1007/s10858-011-9509-1))

## The multi-processor reference

Although not published, if the multi-processor framework is used to run relax on multi-core systems, grids, or clusters, then please acknowledge the author of that code – Gary Thompson.

## Specific analyses

The following subsections list the citations for the individual analysis specific parts of relax.

## Model-free analysis references

The base citations for model-free theory are:

- Lipari, G. and Szabo, A. (1982a). Model-free approach to the interpretation of nuclear magnetic-resonance relaxation in macromolecules I. Theory and range of validity. *J. Am. Chem. Soc.*, **104**(17), 4546–4559. ([10.1021/ja00381a009](https://doi.org/10.1021/ja00381a009))
- Lipari, G. and Szabo, A. (1982b). Model-free approach to the interpretation of nuclear magnetic-resonance relaxation in macromolecules II. Analysis of experimental results. *J. Am. Chem. Soc.*, **104**(17), 4559–4570. ([10.1021/ja00381a010](https://doi.org/10.1021/ja00381a010))
- Clore, G. M., Szabo, A., Bax, A., Kay, L. E., Driscoll, P. C., and Gronenborn, A. M. (1990). Deviations from the simple 2-parameter model-free approach to the interpretation of N-15 nuclear magnetic-relaxation of proteins. *J. Am. Chem. Soc.*, **112**(12), 4989–4991. ([10.1021/ja00168a070](https://doi.org/10.1021/ja00168a070))

If the automated analysis of the `dauvergne_protocol.py` sample script or the GUI model-free analysis which uses the same protocol has been used, then the following citations are all implicit:

- d’Auvergne, E. J. and Gooley, P. R. (2003). The use of model selection in the model-free analysis of protein dynamics. *J. Biomol. NMR*, **25**(1), 25–39. ([10.1023/a:1021902006114](https://doi.org/10.1023/a:1021902006114))
- d’Auvergne, E. J. and Gooley, P. R. (2006). Model-free model elimination: A new step in the model-free dynamic analysis of NMR relaxation data. *J. Biomol. NMR*, **35**(2), 117–135. ([10.1007/s10858-006-9007-z](https://doi.org/10.1007/s10858-006-9007-z))
- d’Auvergne, E. J. and Gooley, P. R. (2007). Set theory formulation of the model-free problem and the diffusion seeded model-free paradigm. *Mol. Biosyst.*, **3**(7), 483–494. ([10.1039/b702202f](https://doi.org/10.1039/b702202f))
- d’Auvergne, E. J. and Gooley, P. R. (2008a). Optimisation of NMR dynamic models I. Minimisation algorithms and their performance within the model-free and Brownian rotational diffusion spaces. *J. Biomol. NMR*, **40**(2), 107–119. ([10.1007/s10858-007-9214-2](https://doi.org/10.1007/s10858-007-9214-2))

- d’Auvergne, E. J. and Gooley, P. R. (2008b). Optimisation of NMR dynamic models II. A new methodology for the dual optimisation of the model-free parameters and the Brownian rotational diffusion tensor. *J. Biomol. NMR*, **40**(2), 121–133. ([10.1007/s10858-007-9213-3](https://doi.org/10.1007/s10858-007-9213-3))

Otherwise, if model-free analysis is used in relax but not via the inbuilt automated protocol, the first reference is for model selection, the second is for eliminating failed model-free models, and the forth is for the optimisation improvements (the third and fifth are for the automated protocol). All of the model-free implementation details of relax are covered by the PhD thesis (available as a PDF or as a printed version on Amazon.com) of:

- d’Auvergne, E. J. (2006). *Protein dynamics: a study of the model-free analysis of NMR relaxation data*. PhD thesis, Biochemistry and Molecular Biology, University of Melbourne. <http://eprints.infodiv.unimelb.edu.au/archive/00002799/>. ([10.187/2281](https://doi.org/10.187/2281))

The reference for the hybridisation of different global diffusion models to analyse the residual inter-domain dynamics – a not very well documented feature of relax – is:

- Horne, J., d’Auvergne, E., Coles, M., Velkov, T., Chin, Y., Charman, W., Prankerd, R., Gooley, P., and Scanlon, M. (2007). Probing the flexibility of the DsbA oxidoreductase from *Vibrio cholerae*—a 15N - 1H heteronuclear NMR relaxation analysis of oxidized and reduced forms of DsbA. *J. Mol. Biol.*, **371**(3), 703–716. ([10.1016/j.jmb.2007.05.067](https://doi.org/10.1016/j.jmb.2007.05.067))

If the software Modelfree4 or Dasha are used as replacement optimisation engines from within relax, the citations for Modelfree4 are:

- Palmer, A. G., Rance, M., and Wright, P. E. (1991). Intramolecular motions of a zinc finger DNA-binding domain from Xfin characterized by proton-detected natural abundance C-12 heteronuclear NMR-spectroscopy. *J. Am. Chem. Soc.*, **113**(12), 4371–4380. ([10.1021/ja00012a001](https://doi.org/10.1021/ja00012a001))
- Mandel, A. M., Akke, M., and Palmer, 3rd, A. G. (1995). Backbone dynamics of *escherichia coli* ribonuclease HI: correlations with structure and function in an active enzyme. *J. Mol. Biol.*, **246**(1), 144–163. ([10.1006/jmbi.1994.0073](https://doi.org/10.1006/jmbi.1994.0073))

and for Dasha:

- Orekhov, V. Y., Nolde, D. E., Golovanov, A. P., Korzhnev, D. M., and Arseniev, A. S. (1995a). Processing of heteronuclear NMR relaxation data with the new software DASHA. *Appl. Magn. Reson.*, **9**(4), 581–588. ([10.1007/bf03162365](https://doi.org/10.1007/bf03162365))

## Consistency testing analysis references

The base citations for the consistency testing of NMR relaxation is:

- Fushman, D., Tjandra, N., and Cowburn, D. (1999). An approach to direct determination of protein dynamics from  $^{15}\text{N}$  NMR relaxation at multiple fields, independent of variable  $^{15}\text{N}$  chemical shift anisotropy and chemical exchange contributions. *J. Am. Chem. Soc.*, **121**(37), 8577–8582. ([10.1021/ja9904991](https://doi.org/10.1021/ja9904991))
- Farrow, N. A., Zhang, O. W., Szabo, A., Torchia, D. A., and Kay, L. E. (1995). Spectral density-function mapping using N-15 relaxation data exclusively. *J. Biomol. NMR*, **6**(2), 153–162. ([10.1007/bf00211779](https://doi.org/10.1007/bf00211779))
- Fushman, D., Tjandra, N., and Cowburn, D. (1998). Direct measurement of  $^{15}\text{N}$  chemical shift anisotropy in solution. *J. Am. Chem. Soc.*, **120**(42), 10947–10952. ([10.1021/ja981686m](https://doi.org/10.1021/ja981686m))

The first is the main citation, whereas the next are the individual tests. The citation for the consistency testing of NMR relaxation as implemented in relax is:

- Morin, S. and Gagné, S. (2009a). Simple tests for the validation of multiple field spin relaxation data. *J. Biomol. NMR*, **45**, 361–372. ([10.1007/s10858-009-9381-4](https://doi.org/10.1007/s10858-009-9381-4))

## N-state model analysis references

Some citations demonstrating as well as presenting the use of the N-state model for diverse analyses types are:

- Sun, H., d’Auvergne, E. J., Reinscheid, U. M., Dias, L. C., Andrade, C. K. Z., Rocha, R. O., and Griesinger, C. (2011). Bijvoet in solution reveals unexpected stereoselectivity in a michael addition. *Chem. Eur. J.*, **17**(6), 1811–1817. ([10.1002/chem.201002520](https://doi.org/10.1002/chem.201002520))
- Erdelyi, M., d’Auvergne, E., Navarro-Vazquez, A., Leonov, A., and Griesinger, C. (2011). Dynamics of the glycosidic bond: Conformational space of lactose. *Chem. Eur. J.*, **17**(34), 9368–9376. ([10.1002/chem.201100854](https://doi.org/10.1002/chem.201100854))

## Reduced spectral density mapping references

The base citations for reduced spectral density mapping are:

- Farrow, N. A., Zhang, O. W., Szabo, A., Torchia, D. A., and Kay, L. E. (1995). Spectral density-function mapping using N-15 relaxation data exclusively. *J. Biomol. NMR*, **6**(2), 153–162. ([10.1007/bf00211779](https://doi.org/10.1007/bf00211779))
- Lefevre, J., Dayie, K., Peng, J., and Wagner, G. (1996). Internal mobility in the partially folded DNA binding and dimerization domains of GAL4: NMR analysis of the N-H spectral density functions. *Biochemistry*, **35**(8), 2674–2686. ([10.1021/bi9526802](https://doi.org/10.1021/bi9526802))

## Relaxation dispersion references

For the base citations for relaxation dispersion, please see chapter 10 on page 139 for a listing of the individual models. The main citation is:

- Morin, S. e. a. (2014). relax: the analysis of biomolecular kinetics using NMR relaxation dispersion data. *In press*

## Generic parts of relax

The following subsections will list the citations for the parts of relax independent of the specific analyses.

### Model selection references

The citation for the model selection component of relax is:

- d’Auvergne, E. J. and Gooley, P. R. (2003). The use of model selection in the model-free analysis of protein dynamics. *J. Biomol. NMR*, **25**(1), 25–39. ([10.1023/a:1021902006114](https://doi.org/10.1023/a:1021902006114))

The base citations for the specific model selection techniques of AIC, AICc, and BIC are respectively:

- Akaike, H. (1973). Information theory and an extension of the maximum likelihood principle. In: Petrov, B. N. and Csaki, F. (eds.): *Proceedings of the Second International Symposium on Information Theory*. Budapest, pages 267–281, Akademia Kiado
- Hurvich, C. M. and Tsai, C. L. (1989). Regression and time-series model selection in small samples. *Biometrika*, **76**(2), 297–307. ([10.1093/biomet/76.2.297](https://doi.org/10.1093/biomet/76.2.297))
- Schwarz, G. (1978). Estimating dimension of a model. *Ann. Stat.*, **6**(2), 461–464. ([10.1214/aos/1176344136](https://doi.org/10.1214/aos/1176344136))

## Other citations

If you believe that other citations should be included in this chapter, please contact the relax users mailing list (relax-users at gna.org).





# Part I

## The basics



# Chapter 1

## Introduction

The program relax is designed for the study of molecular dynamics through the analysis of experimental NMR data. Organic molecules, proteins, RNA, DNA, sugars, and other biomolecules are all supported. It was originally written for the model-free analysis of protein dynamics, though its scope has been significantly expanded. It is a community driven project created by NMR spectroscopists for NMR spectroscopists. It supports many analysis types including:

**Model-free analysis** - the Lipari and Szabo model-free analysis of NMR relaxation data

**$R_1$  and  $R_2$**  - the exponential curve fitting for the calculation of the  $R_x$  NMR relaxation rates.

**NOE** - the calculation of the steady-state NOE NMR relaxation data.

**Data consistency** - the consistency testing of multiple field NMR relaxation data.

**RSDM** - Reduced Spectral Density Mapping.

**Frame order and N-state model** - study of domain motions via the N-state model and frame order dynamics theories using anisotropic NMR parameters such as RDCs and PCSs.

**Stereochemistry** - investigations of absolute stereochemistry of flexible molecules.

**Relaxation dispersion** - the study of processes on the chemical exchange timescale.

The aim of relax is to provide a seamless and extremely flexible environment able to accept input in any format produced by other NMR software, able to faultlessly create input files, control, and read output from various programs including Modelfree and Dasha, output results in many formats, and visualise the data by controlling programs such as Grace, OpenDX, MOLMOL, and PyMOL. All data analysis tools from optimisation to model selection to Monte Carlo simulations are inbuilt into relax. Therefore the use of additional programs is optional.

The flexibility of relax arises from the choice of relax's scripting capabilities, its Python prompt interface, or its graphical user interface (GUI). Extremely complex scripts can be

created from simple building blocks to fully automate data analysis. A number of sample scripts have been provided to help understand script construction. In addition, any of Python's powerful features or functions can be incorporated as the script is executed as an arbitrary Python source file within relax's environment. The modules of relax can also be used as a vast library of dynamics related functions by your own software.

relax is free software (free as in freedom) which is licenced under the GNU General Public Licence (GPL). You are free to copy, modify, or redistribute relax under the terms of the GPL.

## 1.1 Program features

### 1.1.1 Literature

The primary references for the program relax are [d'Auvergne and Gooley \(2008a\)](#) and [d'Auvergne and Gooley \(2008b\)](#). To properly cite the various parts of relax used in your analysis, please see Chapter on page [xxiii](#).

### 1.1.2 Supported NMR theories

The following relaxation data analysis techniques are currently supported by relax:

- Model-free analysis ([Lipari and Szabo \(1982a,b\)](#); [Clore et al. \(1990\)](#) and the specific implementation of [d'Auvergne and Gooley \(2003, 2006, 2007, 2008a,b\)](#)). This includes the hybridisation of global diffusion models to study residual domain dynamics ([Horne et al., 2007](#)).
- Reduced spectral density mapping ([Farrow et al., 1995](#); [Lefevre et al., 1996](#)).
- Consistency testing – the validation of multiple field NMR relaxation data ([Morin and Gagné, 2009a](#); [Fushman et al., 1999](#)).
- Exponential curve fitting (to find the  $R_1$  and  $R_2$  relaxation rates).
- Steady-state NOE calculation.
- Determination of absolute stereochemistry of flexible molecules via the N-state model using isotropic and anisotropic NMR parameters such as NOE, ROE, and RDC combined with MD simulation or simulated annealing, and ORD ([Sun et al., 2011](#)).
- The N-state model for investigating domain motions.
- The frame order theory.
- Conformational analysis of paramagnetically tagged molecules via the N-state model ([Erdelyi et al., 2011](#)).
- Analysis and comparison of ensembles of structures using RDCs, PCSs, NOEs, etc. (the N-state model of dynamics).
- The analysis of relaxation dispersion.

## The future

Because relax is free software, if you would like to contribute addition features, functions, or modules which you have written for your own publications for the benefit of the field, almost anything relating to molecular dynamics may be accepted. Please see the Open Source chapter on page 29 for more details.

### 1.1.3 Data analysis tools

The following tools are implemented as modular components to be used by any data analysis technique:

- Numerous high-precision optimisation algorithms.
- Model selection ([d’Auvergne and Gooley, 2003](#); [Chen et al., 2004](#)):
  - Akaike’s Information Criteria (AIC).
  - Small sample size corrected AIC (AICc).
  - Bayesian or Schwarz Information Criteria (BIC).
  - Bootstrap model selection.
  - Single-item-out cross-validation (CV).
  - Hypothesis testing ANOVA model selection (only the model-free specific technique of [Mandel et al. \(1995\)](#) is supported).
- Monte Carlo simulations (error analysis for all data analysis techniques).
- Model elimination – the removal of failed models prior to model selection ([d’Auvergne and Gooley, 2006](#)).

### 1.1.4 Data visualisation

The results of an analysis, or any data input into relax, can be visualised using a number of programs:

**MOLMOL** 1D data can be mapped onto a structure either by the creation of MOLMOL macros or by direct control of the program.

**PyMOL** 3D objects such as the diffusion tensor representation can be displayed with the structure.

**Grace** any 2D data can be plotted.

**OpenDX** The chi-squared space of models with three parameters can be mapped and 3D images of the space produced.

### 1.1.5 Interfacing with other programs

relax can create the input files, execute in-line, and then read the output of the following programs. These programs can be used as optimisation engines replacing the minimisation algorithms built into relax:

- Dasha (model-free analysis).
- Modelfree (model-free analysis).

### 1.1.6 The user interfaces (UI)

relax can be used through the following UIs:

**The prompt** this is the primary interface of relax. Rather than reinventing a new command language, relax's interface is the powerful Python prompt. This gives the power user full access to a proven programming language. See Figure 1.1 for a screenshot.

**Scripting** this provides a more powerful and flexible framework for controlling the program. The script will be executed as Python code enabling advanced programming for automating data analysis. All the features available within the prompt environment are accessible to the script. See Figure 1.2 for a screenshot.

**GUI** the graphical user interface provides a sub-set of relax's features - the automatic  $R_1$  and  $R_2$  relaxation rate curve-fitting, the NOE calculations, and the automatic model-free analysis provided by the `dauvergne_protocol` module (d'Auvergne and Gooley, 2008b). See Figure 1.3 for a screenshot.

## 1.2 How to use relax

### 1.2.1 The prompt

The primary interface of relax is the prompt. After typing “**relax**” within a terminal you will be presented with

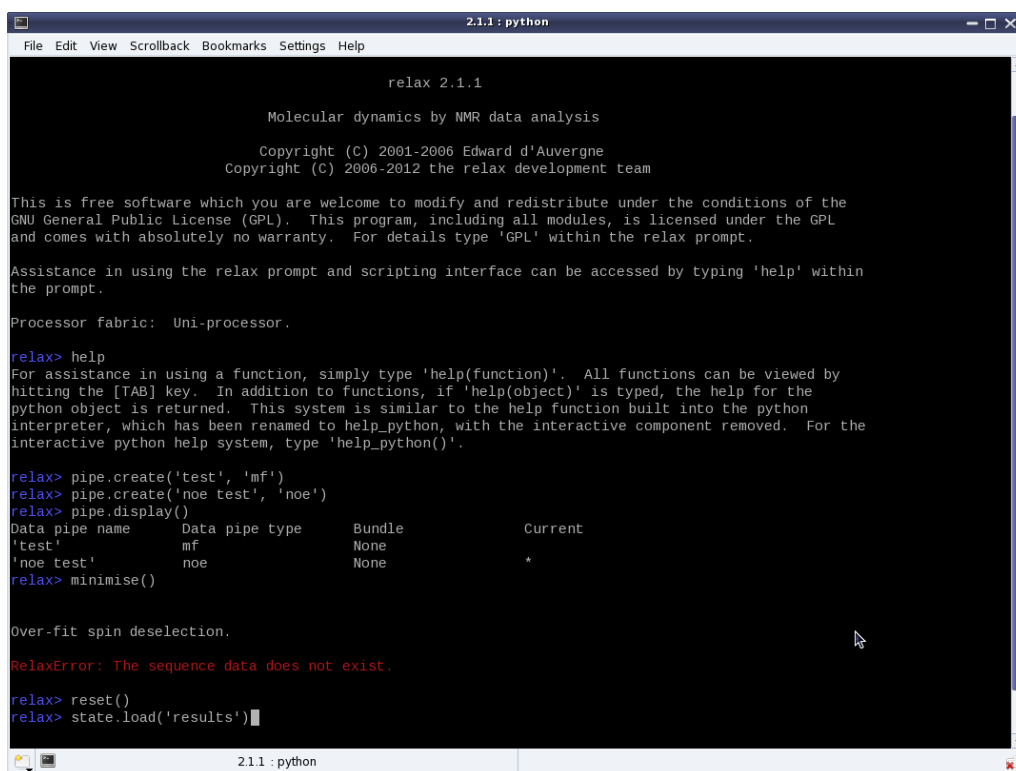
```
relax>
```

This is the Python prompt which has been tailored specifically for relax. You will hence have full access, if desired, to the power of the Python programming language to manipulate your data. You can for instance type

```
relax> print("Hello World")
```

the result being

```
relax> print("Hello World")
Hello World
relax>
```



```

2.1.1: python
File Edit View Scrollback Bookmarks Settings Help

relax 2.1.1

Molecular dynamics by NMR data analysis

Copyright (C) 2001-2006 Edward d'Auvergne
Copyright (C) 2006-2012 the relax development team

This is free software which you are welcome to modify and redistribute under the conditions of the
GNU General Public License (GPL). This program, including all modules, is licensed under the GPL
and comes with absolutely no warranty. For details type 'GPL' within the relax prompt.

Assistance in using the relax prompt and scripting interface can be accessed by typing 'help' within
the prompt.

Processor fabric: Uni-processor.

relax> help
For assistance in using a function, simply type 'help(function)'. All functions can be viewed by
hitting the [TAB] key. In addition to functions, if 'help(object)' is typed, the help for the
python object is returned. This system is similar to the help function built into the python
interpreter, which has been renamed to help_python, with the interactive component removed. For the
interactive python help system, type 'help_python()'.

relax> pipe.create('test', 'mf')
relax> pipe.create('noe test', 'noe')
relax> pipe.display()
Data pipe name      Data pipe type      Bundle      Current
'test'              mf                  None
'noe test'          noe                 None        *
relax> minimise()

Over-fit spin deselection.

RelaxError: The sequence data does not exist.

relax> reset()
relax> state.load('results')

```

Figure 1.1: A screenshot of relax being run in the primary prompt mode.

Or using relax as a calculator

```

relax> (1.0 + (2 * 3))/10
0.69999999999999996
relax>

```

## 1.2.2 Python

relax has been designed such that knowledge about Python is not required to be able to fully use the program. A few basics though will aid in understanding relax.

A number of simple programming axioms includes that of strings, integers, floating point numbers, and lists. A string is text and within Python (as well as relax) this is delimited by either single or double quotes. An integer is a number with no decimal point whereas a float is a number with a decimal point. A list in Python (called an array in other languages) is a list of anything separated by commas and delimited by square brackets, an example is `[0, 1, 2, 'a', 1.2143235]`.

Probably the most important detail is that functions in Python require brackets around their arguments. For example

```
relax> minimise()
```

will commence minimisation however

```
relax> minimise
```

```

1.3.15: python
[edward@localhost 1.3.15]$ ./relax simple_script.py

relax 1.3.15

Molecular dynamics by NMR data analysis

Copyright (C) 2001-2006 Edward d'Auvergne
Copyright (C) 2006-2012 the relax development team

This is free software which you are welcome to modify and redistribute under the conditions of the
GNU General Public License (GPL). This program, including all modules, is licensed under the GPL
and comes with absolutely no warranty. For details type 'GPL' within the relax prompt.

Assistance in using the relax prompt and scripting interface can be accessed by typing 'help' within
the prompt.

Processor fabric: Uni-processor.

script = 'simple_script.py'
-----
pipe.create(pipe_name='Dy test', pipe_type='N-state')
align_tensor.init(tensor='Dysprosium', params=(1.0278e-03, -1.4860e-03, 8.4778e-04, 5.7108e-04, 3.6500e-04), param_types=1)
rdc.calc_q_factors()
align_tensor.delete()
align_tensor.display()
-----

relax> pipe.create(pipe_name='Dy test', pipe_type='N-state')
relax> align_tensor.init(tensor='Dysprosium', params=(0.0010278, -0.001486, 0.00084778, 0.00057108, 0.000365), scale=1.0, angle_units='deg',
param_types=1, errors=False)
relax> rdc.calc_q_factors(spin_id=None)
RelaxWarning: No RDC data exists, Q factors cannot be calculated.
relax> align_tensor.delete(tensor=None)
Removing the 'Dysprosium' tensor.
relax> align_tensor.display(tensor=None)
RelaxError: No alignment tensor data exists.

[edward@localhost 1.3.15]$

```

Figure 1.2: A screenshot of relax being run in scripting mode.

will do nothing.

The arguments to a function are simply a comma separated list within the brackets of the function. For example to save the program’s current state type

```
relax> state.save('save', force=True)
```

Two types of arguments exist in Python – standard arguments and keyword arguments. The majority of arguments you will encounter within relax are keyword arguments however you may, in rare cases, encounter a non-keyword argument. For these standard arguments just type the values in, although they must be in the correct order. Keyword arguments consist of two parts – the key and the value. For example the key may be `file` and the value you would like to supply is “R1.out”. Various methods exist for supplying this argument. Firstly you could simply type “R1.out” into the correct position in the argument list. Secondly you can type `file='R1.out'`. The power of this second option is that argument order is unimportant. Therefore if you would like to change the default value of the very last argument, you don’t have to supply values for all other arguments. The only catch is that standard arguments must come before the keyword arguments.

### 1.2.3 User functions

For standard data analysis a large number of specially tailored functions called “user functions” have been implemented. These are accessible from the relax prompt by simply typing the name of the function. An example is `help()`. An alphabetical listing of all accessible user functions together with full descriptions is presented later in this manual.



A few special objects which are available within the prompt are not actually functions. These objects do not require brackets at their end for them to function. For example to exit relax type

```
relax> exit
```

Another special object is that of the function class. This object is simply a container which holds a number of user functions. You can access the user function within the class by typing the name of the class, then a dot “.”, followed by the name of the user function. An example is the user function for reading relaxation data out of a file and loading the data into relax. The function is called “read” and the class is called “**relax\_data**”. To execute the function, type something like

```
relax> relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',  
    res_num_col=1, data_col=3, error_col=4)
```

On first usage the relax prompt can be quite daunting. Two features exist to increase the usability of the prompt – the help system and tab completion.

### 1.2.4 The help system

For assistance in using a function simply type

```
relax> help(function)
```

In addition to functions if

```
relax> help(object)
```

is typed the help for the python object is returned. This system is similar to the help function built into the python interpreter, which has been renamed to **help\_python**, with the interactive component removed. For the standard interactive python help system type

```
relax> help_python()
```

### 1.2.5 Tab completion

Tab completion is implemented to prevent insanity as the function names can be quite long – a deliberate feature to improve usability. The behaviour of the tab completion is very similar to that of the bash prompt.

Not only is tab completion useful for preventing RSI but it can also be used for listing all available functions. To begin with if you hit the [TAB] key without typing any text all available functions will be listed (along with function classes and other python objects). This extends to the exploration of user functions within a function class. For example to list the user functions within the function class **model\_free** type

```
relax> model_free.
```

The dot character at the end is essential. After hitting the [TAB] key you should see something like

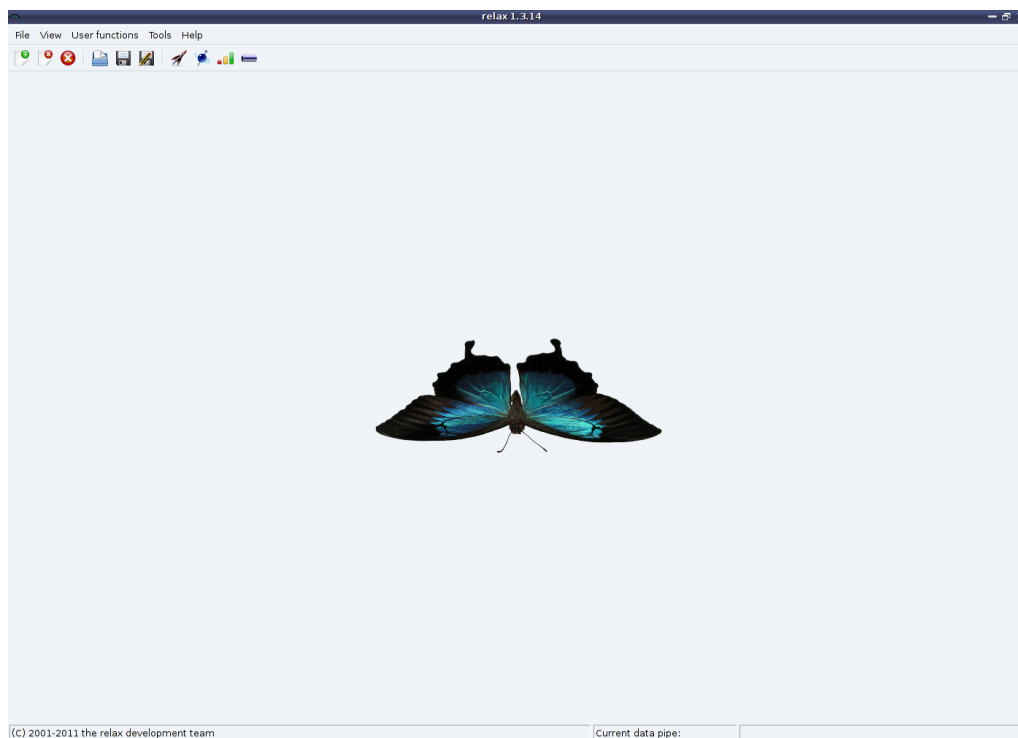


Figure 1.3: Screenshot of the relax GUI interface – the starting interface. To start one of the automated analyses, either the menu “File→New analysis” or the new analysis button in the toolbar should be selected.

```
relax| model_free.
model_free.__class__
model_free.__doc__
model_free.__init__
model_free.__module__
model_free.__relax__
model_free.__relax_help__
model_free.create_model
model_free.delete
model_free.remove_tm
model_free.select_model
relax> model_free.
```

All the objects beginning with an underscore are “hidden”, they contain information about the function class and should be ignored. From the listing the user functions `copy`, `create_model`, `delete`, `remove_tm`, and `select_model` contained within `model_free` are all visible.

### 1.2.6 The data pipe

Within relax all user functions operate on data stored within the current data pipe. This pipe stores data is input, processed, or output as user functions are called. There are different types of data pipe for different analyses, e.g. a reduced spectral density mapping pipe, a model-free pipe, an exponential curve-fitting pipe, etc. Multiple data pipes can be created within relax and various operations performed in sequence on these pipes. This is

useful for operations such as model selection whereby the function `model_selection` can operate on a number of pipes corresponding to different models and then assign the results to a newly created pipe. When running relax you choose which pipe you are currently in by using the `pipe.switch` user function to jump between pipes.

The flow of data through relax can be thought of as travelling through these pipes. User functions exist to transfer data between these pipes and other functions combine data from multiple pipes into one or vice versa. The simplest invocation of relax would be the creation of a single data pipe and with the data being processed as it is passing through this pipe.

The primary method for creating a data pipe is through the user function `pipe.create`. For example

```
relax> pipe.create('m1', 'mf')
```

will create a model-free data pipe labelled “m1”. The following is a table of all the types which can be assigned to a data pipe.

| Data pipe type | Description                                |
|----------------|--|
| “ct”           | Consistency testing of relaxation data     |
| “frame order”  | The Frame Order analyses of domain motions |
| “jw”           | Reduced spectral density mapping           |
| “hybrid”       | A special hybridised data pipe             |
| “mf”           | Model-free data analysis                   |
| “N-state”      | N-state model of domain motions            |
| “noe”          | Steady state NOE calculation               |
| “relax_fit”    | Relaxation curve-fitting                   |

### 1.2.7 The spin and interatomic data containers

Any data which is not considered global for the molecule, such as diffusion tensors, alignment tensors, global minimisation statistics, etc., are stored within two special structures of the data pipes. Any NMR data or information which is specific to an isolated spin system is stored within special spin containers. This includes for example relaxation data, CSA information, nuclear isotope type, chemical element type, model-free parameters, reduced spectral density mapping values, spin specific minimisation statistics and PCS data. NMR data or information which is defined as being between two spin systems, such as the magnetic dipole-dipole interaction involved in both NMR relaxation and RDC data, interatomic vectors and NOESY data, is stored within the interatomic data containers. The spin and interatomic data containers and their associated data can be manipulated using a multitude of the relax user functions.

### 1.2.8 Scripting

What ever is done within the prompt is also accessible through scripting (Figure 1.2). First type your commands into a text file ending in `*.py`. To use this mode of relax, you will need to open up a terminal in your respective operating system:

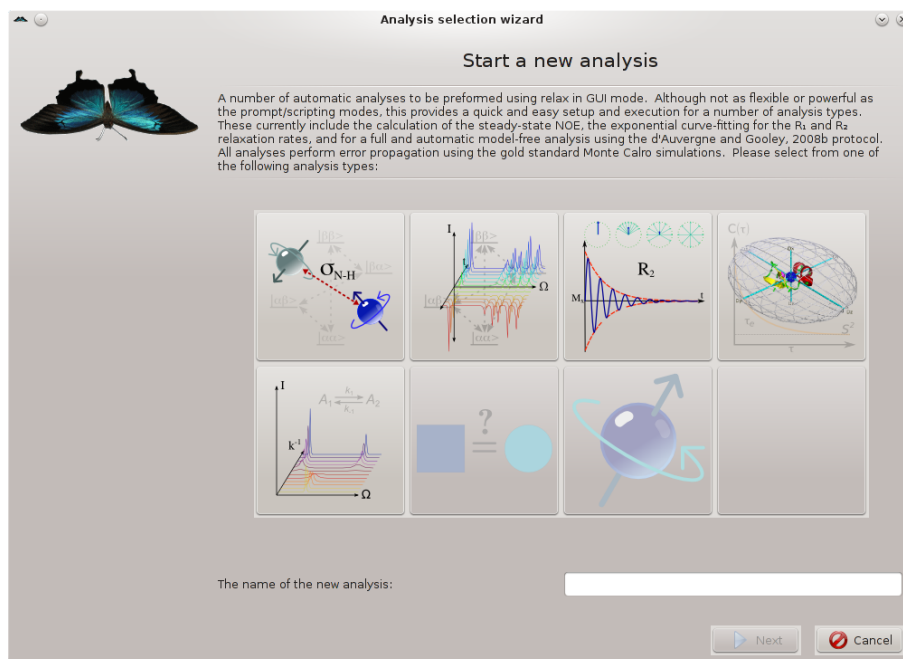


Figure 1.4: Screenshot of the relax GUI interface – the analysis selection wizard. From here, the steady-state NOE analysis, the  $R_1$  and  $R_2$  relaxation rates via exponential curve-fitting, and the automated model-free analysis can be selected.

**GNU/Linux:** Here you have an incredible number of choices. If you don't have a preferred shell already, you could try one of **Konsole**, **GNOME Terminal** or even **XTerm** if you are a masochist.

**Mac OS X:** This is as simple as in GNU/Linux – just launch **Terminal.app** from the **Utilities** folder.

**MS Windows:** If your system supports it, you should install and use **Windows PowerShell**. The alternative is the nasty **cmd** command line terminal program which comes installed by default on all Windows versions. The **PowerShell**, although nowhere near as powerful as the Linux and Mac terminals, is a huge improvement on the ancient **cmd** program and will make relax much better to use on MS Windows.

Once your terminal is running, go to the directory containing your script using the **cd** command (if you do not know what this is, please see the documentation for your terminal program to understand some of its basic usage). Once you are in the correct directory, within the terminal type:

```
$ relax your_script.py
```

You will need to replace **your\_script.py** with the name of your script. In most cases you would probably like to keep a log of all of the messages, warnings and errors relax produces for future reference. To activate logging within relax, type:

```
$ relax --log log your_script.py
```

This will place all output (both **STDOUT** and **STDERR**) into the **log** file (you can choose any name for this log file). Alternatively you can both log the output and simultaneously see the messages in your terminal by typing:

```
$ relax --tee log your_script.py
```

These command line arguments could be replaced by IO redirection if this is a familiar concept to you, but note that these arguments are active also in the GUI mode whereby IO redirection in the terminal will have no effect. An example of a simple script which will minimise the model-free model “m4” after loading six relaxation data sets is

```
1 # Create the data pipe.
2 name = 'm4'
3 pipe.create(name, 'mf')
4
5 # Load the PDB file.
6 structure.read_pdb('1f3y.pdb')
7
8 # Set up the 15N and 1H spins.
9 structure.load_spins('@N', ave_pos=True)
10 structure.load_spins('@H', ave_pos=True)
11 spin.isotope('15N', spin_id='@N')
12 spin.isotope('1H', spin_id='@H')
13
14 # Load the relaxation data.
15 relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
16                 res_num_col=1, data_col=3, error_col=4)
17 relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
18                 res_num_col=1, data_col=3, error_col=4)
19 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
20                 res_num_col=1, data_col=3, error_col=4)
21 relax_data.read(ri_id='R1_500', ri_type='R1', frq=500.0*1e6, file='r1.500.out',
22                 res_num_col=1, data_col=3, error_col=4)
23 relax_data.read(ri_id='R2_500', ri_type='R2', frq=500.0*1e6, file='r2.500.out',
24                 res_num_col=1, data_col=3, error_col=4)
25 relax_data.read(ri_id='NOE_500', ri_type='NOE', frq=500.0*1e6, file='noe.500.out',
26                 res_num_col=1, data_col=3, error_col=4)
27
28 # Initialise the diffusion tensor.
29 diffusion_tensor.init((2e-8, 1.3, 60, 290), param_types=1, axial_type='prolate', fixed=
30                       True)
31
32 # Create all attached protons.
33 sequence.attach_protons()
34
35 # Define the magnetic dipole-dipole relaxation interaction.
36 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
37 interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)
38 interatom.unit_vectors()
39
40 # Define the CSA relaxation interaction.
41 value.set(-172 * 1e-6, 'csa')
42
43 # Select a preset model-free model.
44 model_free.select_model(model=name)
45
46 # Grid search.
47 grid_search(inc=11)
48
49 # Minimise.
50 minimise('newton')
51
52 # Finish.
53 results.write(file='results', force=True)
```

```
47 state.save('save', force=True)
```

Scripting is much more powerful than the prompt as advanced Python programming can be employed (see the file `relax_curve_diff.py` in the `sample_scripts` directory for an example).

## Sample scripts

A few sample scripts have been provided in the directory `sample_scripts`. These can be copied and modified for different types of data analysis.

### 1.2.9 The test suite

To test that the program functions correctly, `relax` possesses an inbuilt test suite. The suite is a collection of simple tests which execute or probe different parts of the program checking that the software runs without problem. The test suite is executed by running `relax` using the command

```
$ relax --test-suite
```

Alternatively the three components of the test suite – system tests, unit tests, and GUI tests – can be run separately with

```
$ relax --system-tests
```

```
$ relax --unit-tests
```

```
$ relax --gui-tests
```

### 1.2.10 The GUI

If the `wxPython` module is installed on your system, you will have access to the GUI interface of `relax`. To launch `relax` in GUI mode, type either

```
$ relax -g
```

or

```
$ relax --gui
```

In most cases you will probably like to have a permanent copy of all the messages, warnings, and errors `relax` produces for future reference. In such a case you could run the GUI with:

```
$ relax --gui --log log
```

This will place all of the output into the `log` file.

The GUI is currently an interface to the automated analyses, providing an easy way to perform quick analyses. The interface consists of a tab for each analysis. By clicking on the “File→New analysis” menu entry or the “New analysis” toolbar button, the analysis wizard will appear (see Figure 1.4). The following analyses can be set up using this wizard:

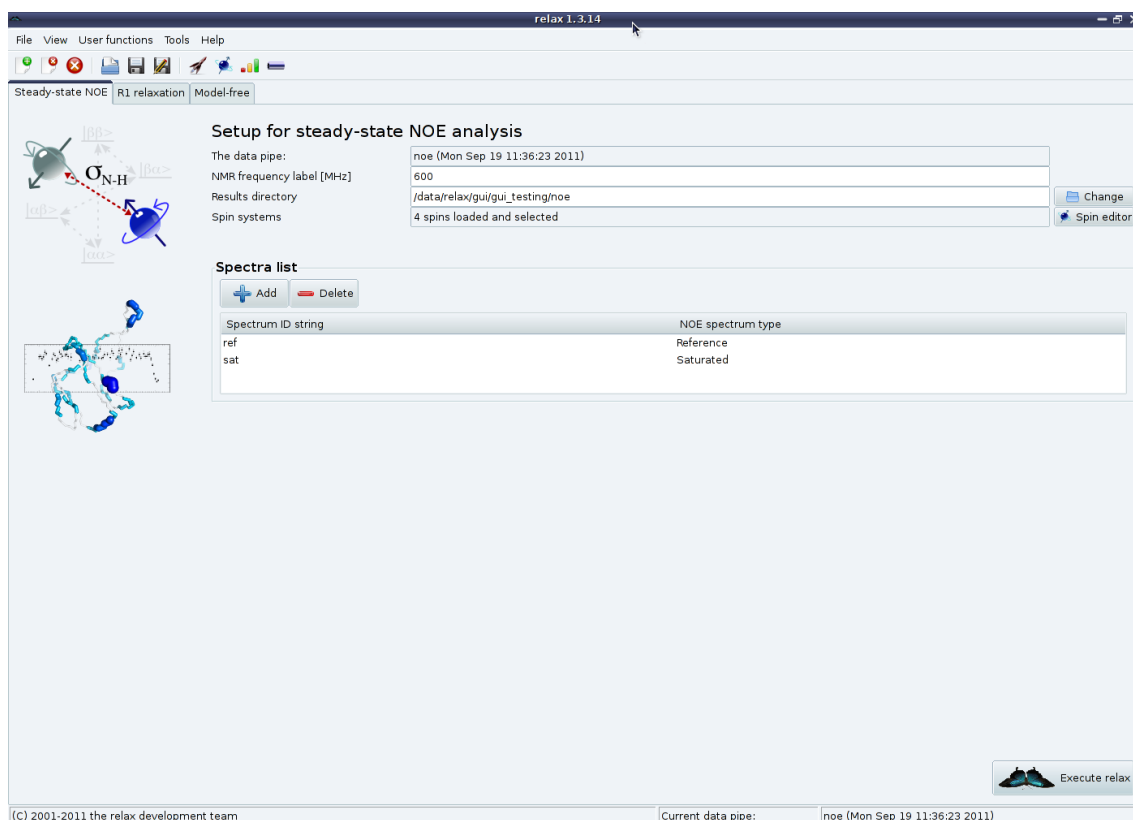


Figure 1.5: Screenshot of the relax GUI interface – the steady-state NOE analysis.

**Steady-state NOE:** this provides access to the steady-state NOE calculation with pseudo Monte Carlo simulations for error analysis (this falls back to bootstrapping as this is a calculation rather than optimisation). See Figure 1.5 on page 15.

**R<sub>1</sub> and R<sub>2</sub> :** these provide easy access to optimisations and error analysis for the R<sub>1</sub> and R<sub>2</sub> relaxation rates via exponential curve-fitting (see Figures 1.6 and 1.7 on pages 16 and 17).

**Model-free analysis :** A fully automatic model-free protocol is provided in another tab. This operates via the `dauvergne_protocol` module which implements the protocol of d’Auvergne and Gooley (2008b) (see Figure 1.8 on page 18).

A number of windows in the GUI provide user feedback or allow for the viewing and editing of data. These include:

**The relax controller :** This window shows the progress of relax’s execution and displays relax’s text output for checking if the analysis has been performed correctly and has completed successfully (see Figure 1.9).

**Spin viewer window :** This is used to load spins system information into the relax data store and to see the contents of the spin containers (see Figure 1.10).

**Results viewer window :** This presents a list of the results files which can be opened by double clicking for visualisation using a text editor, Grace, PyMOL, MOLMOL, etc (see Figure 1.11).

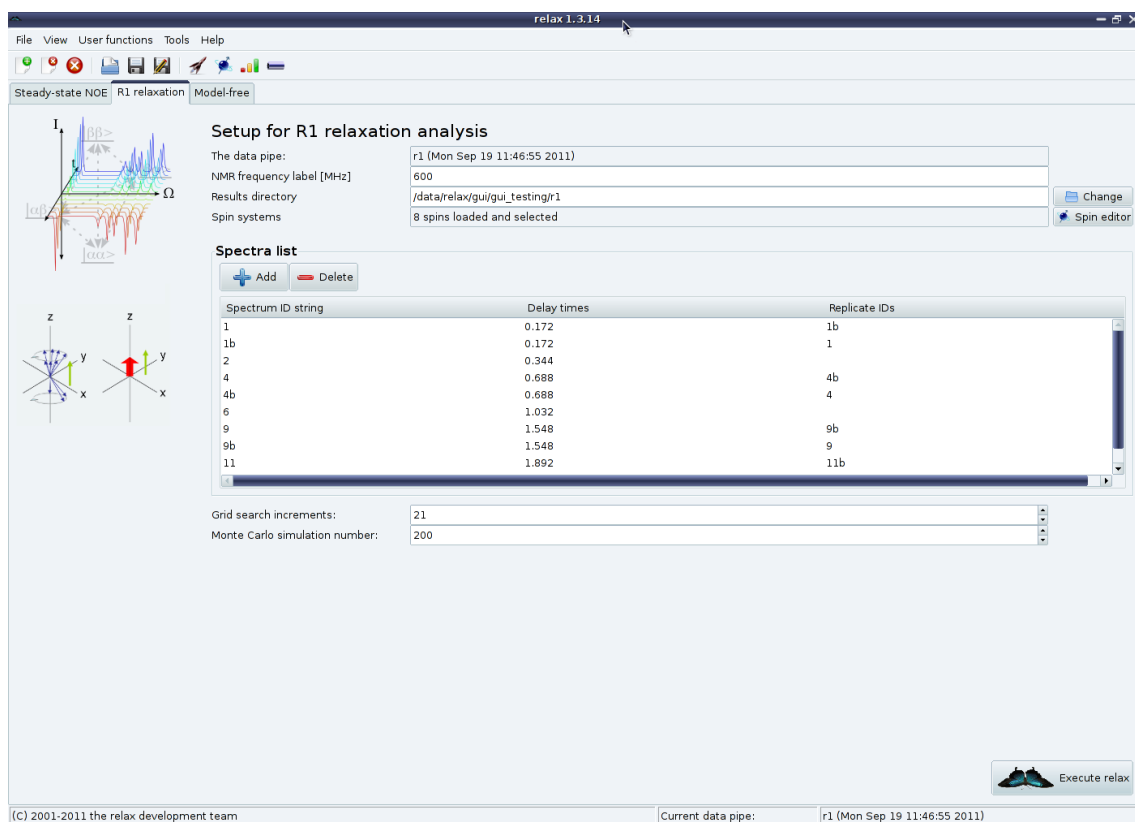


Figure 1.6: Screenshot of the relax GUI interface – the  $R_1$  analysis.

**Data pipe editor** : This window allows for easy manipulation of the data pipes of the relax data store (see Figure 1.12).

**The relax prompt** : This window gives access to the relax prompt (see Figure 1.13).

### 1.2.11 Access to the internals of relax

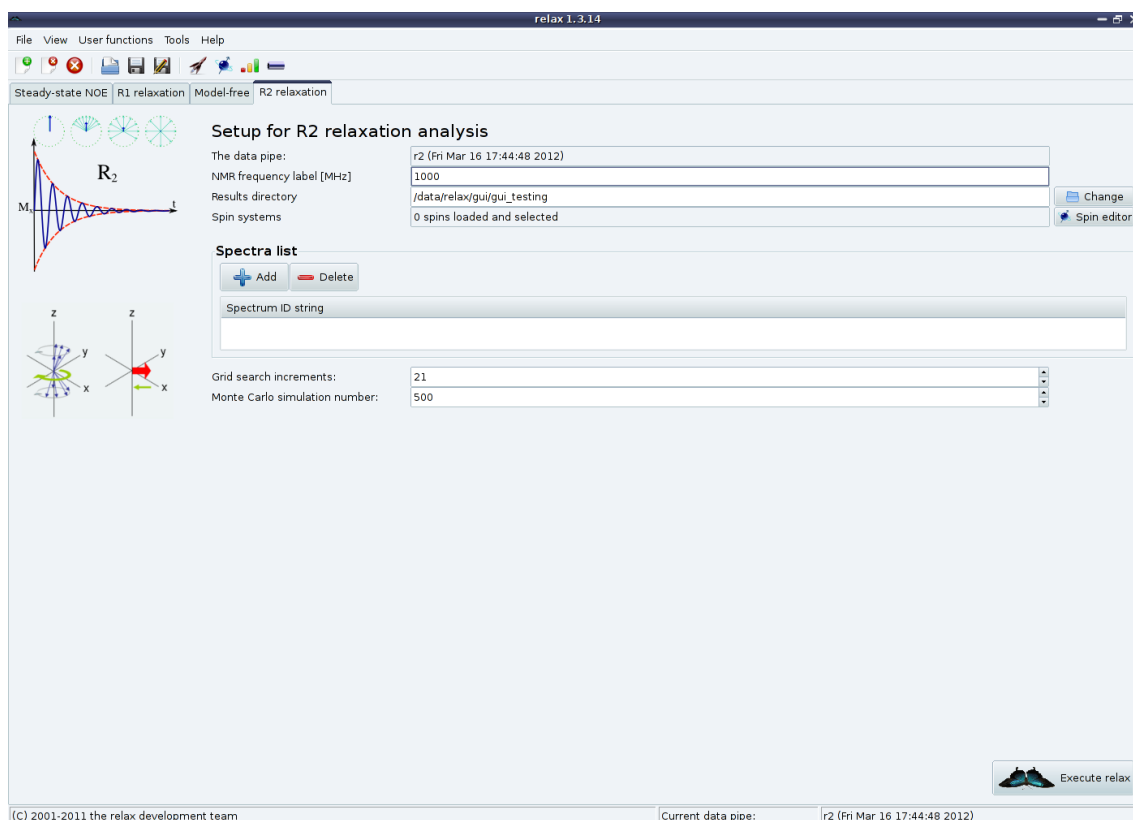
To enable advanced Python scripting and control, many parts of relax have been designed in an object oriented fashion. If you would like to play with internals of the program the entirety of relax is accessible by importation. For example all data is contained within the object called the relax data store which, to be able to access it, needs be imported by typing:

```
relax> from data_store import Relax_data_store; ds = Relax_data_store()
```

The `ds` object is a dictionary type which contains the multiple data pipes. All of relax's packages, modules, functions, and classes are also accessible by import statements. For example to create a rotation matrix from three Euler angles in the z-y-z notation, type:

```
relax> alpha = 0.1342
relax> beta = 1.0134
relax> gamma = 2.4747
relax> from lib.geometry.rotations import euler_to_R_zyz
relax> from numpy import float64, zeros
relax> R = zeros((3,3), float64)
```



Figure 1.7: Screenshot of the relax GUI interface – the  $R_2$  analysis.

```

relax> euler_to_R_zyz(alpha, beta, gamma, R)
relax> print(R)
[[-0.494666415429033 -0.557373756841289 -0.666813041737502]
 [ 0.219125193028791 -0.822460914570202  0.524921131013452]
 [-0.84100492699311  0.113545317776532  0.528978424497956]]
relax>

```

## 1.3 The multi-processor framework

### 1.3.1 Introduction to the multi-processor

Thanks to Gary Thompson's multi-processor framework, relax can be run on multi-core/multi-CPU systems or on clusters to speed up calculations. As most analyses are relatively quick and would not benefit from the multi-processor framework, only the model-free and frame order analyses have currently been parallelised to run within this framework. To use the multi-processor framework, the following should be installed:

**OpenMPI:** This is the most commonly used Message Passing Interface (MPI) protocol software. The rest of this manual will assume that this is the implementation in use. If another implementation is used, please see the specific documentation for that software for how to set up a program to run via MPI.

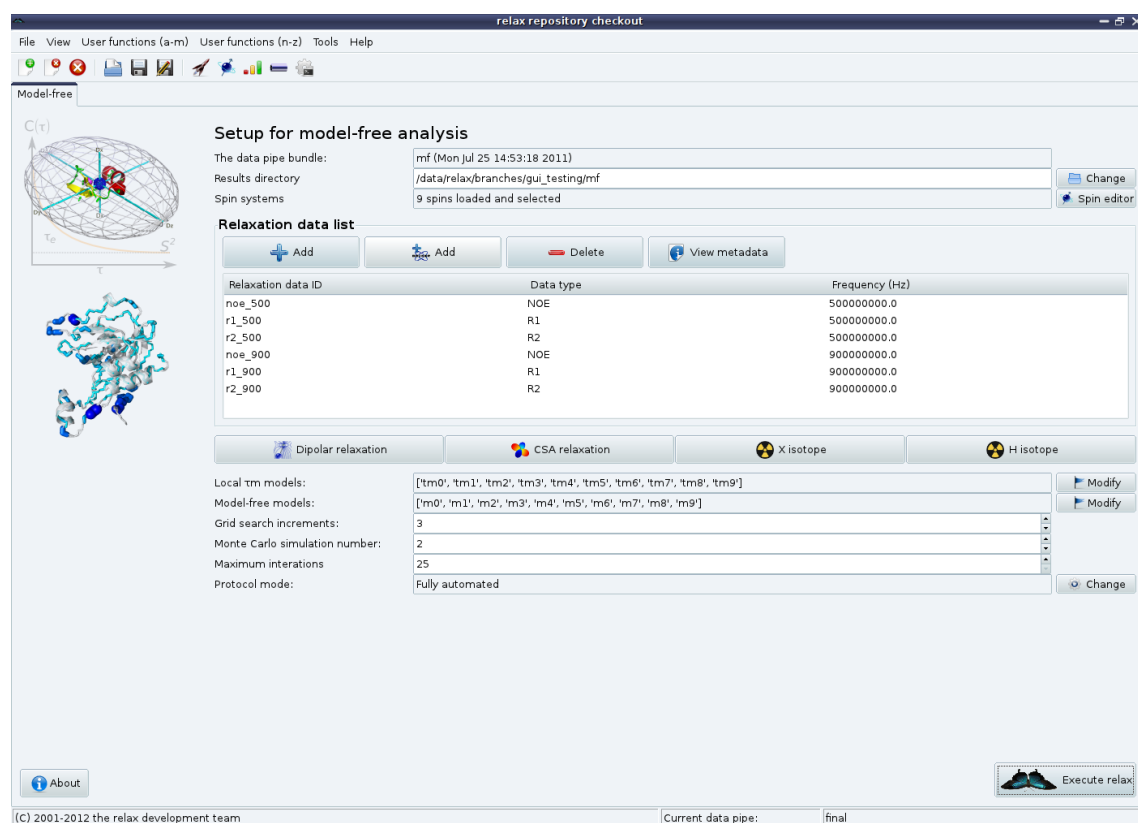


Figure 1.8: Screenshot of the relax GUI interface – the automated model-free analysis. The analysis is fully automated via a new model-free protocol as described in detail in Chapter 7. Clicking on the “About” button in the bottom left hand corner will give a full description of the protocol. For using this interface or any of the modern-day model-free protocols, data from at least two magnetic field strengths must be without question collected.

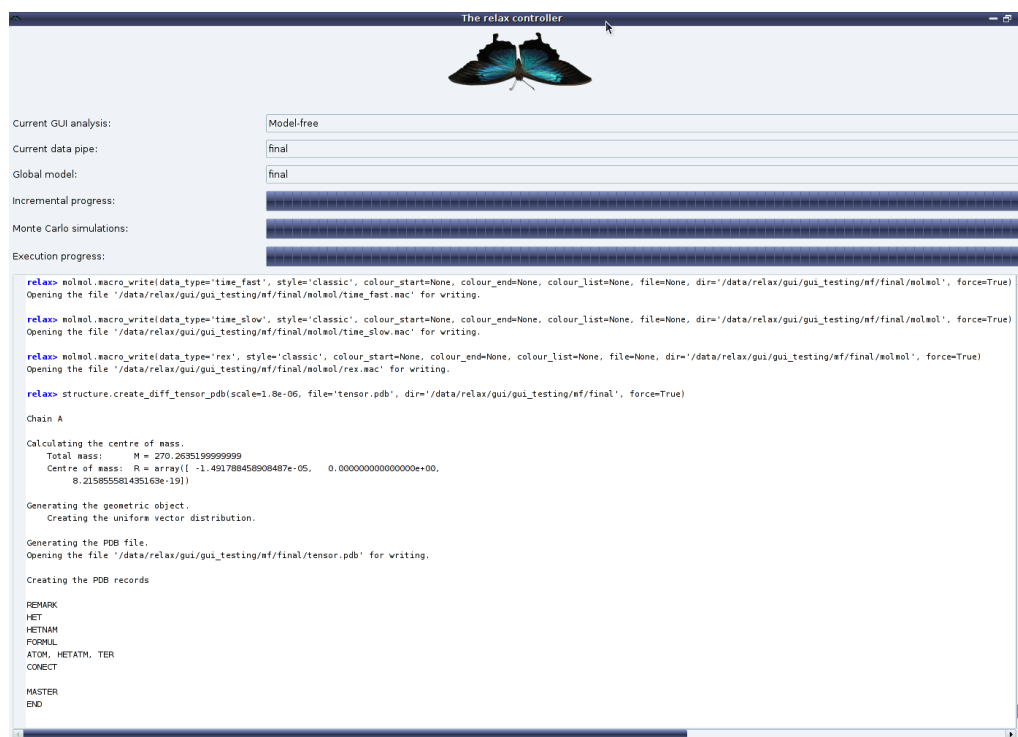


Figure 1.9: Screenshot of the relax GUI interface – the relax controller window. The purpose of the controller is for feedback. It shows the current analysis and current data pipe, a number of progress gauges, and the relax text output.

**mpi4py:** This dependency is essential for running in MPI mode in relax. If you would like to use another Python implementation to access the MPI protocol, please consider becoming a relax developer.

### 1.3.2 Usage of the multi-processor

If you have access to a 256 node cluster and can run calculations on all nodes, assuming that the `dauvergne_protocol.py` automated model-free analysis sample script will be used (after modification for the system under study), relax can be executed by typing:

```
$ mpirun -np 257 /usr/local/bin/relax --multi='mpi4py' --tee log dauvergne_protocol.py
```

Note that the argument `-np` value is one more than the number of slaves you would like to run. You should then see the following text in the initial relax printout:

```
Processor fabric: MPI 2.1 running via mpi4py with 256 slave processors & 1 master. Using
Open MPI 1.4.3.
```

### 1.3.3 Further details

For a full description of the multi-processor framework and how to use it, please see Gary Thompson's official announcement on the [relax-devel mailing list](#).

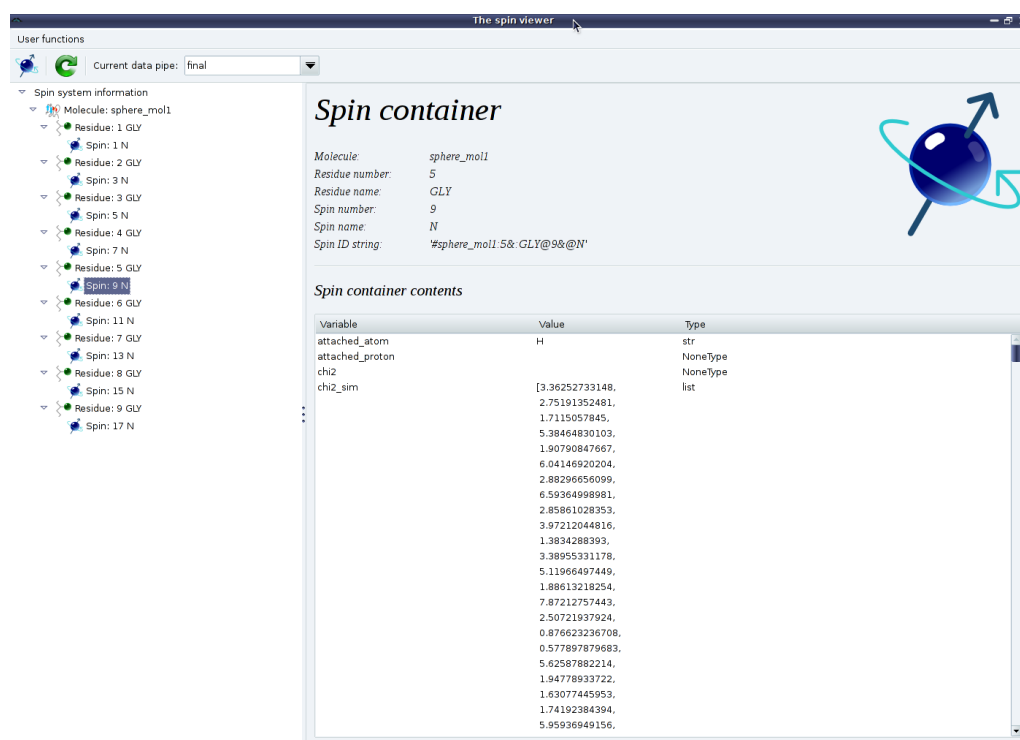


Figure 1.10: Screenshot of the relax GUI interface – the spin viewer window. This viewer is designed for easy addition and manipulation of spin systems within the relax data store. The window is accessible via the “View→Spin viewer” menu entry, typing “[Ctrl-T]”, the spin viewer button in the toolbar, or the “spin editor” button within the auto-analysis tabs.

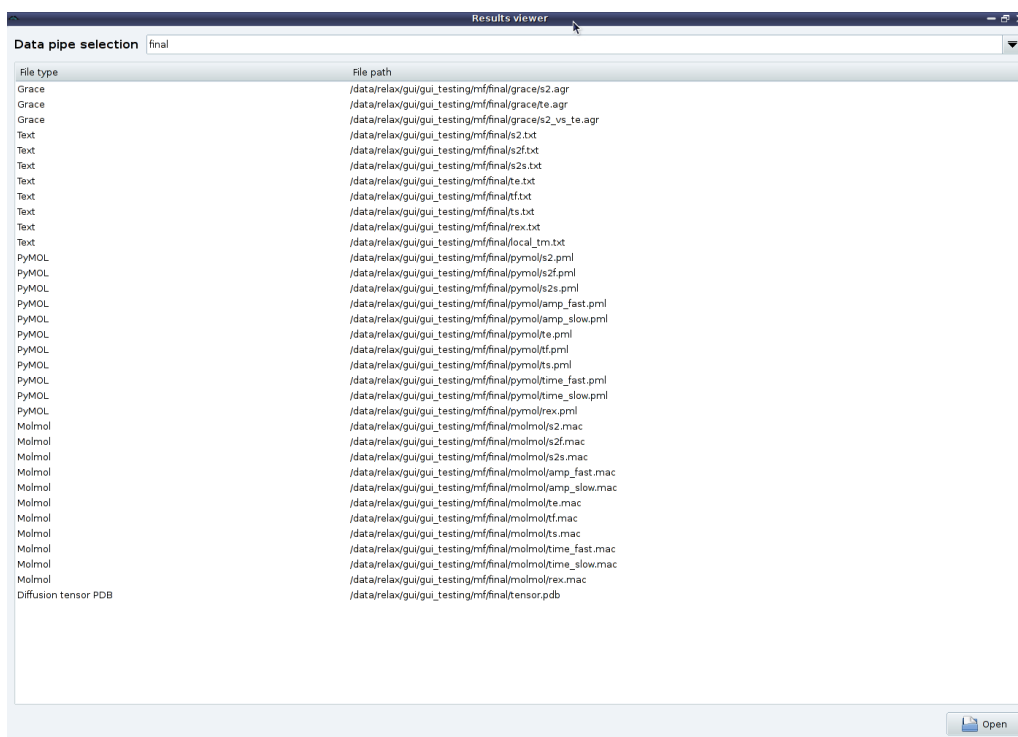


Figure 1.11: Screenshot of the relax GUI interface – the results viewer window. At the end of one of the automated analyses, a number of results files will be created. This can include text files containing the results, 2D Grace plots of the results, PyMOL and MOLMOL macros plotting the results onto the structure, diffusion tensor objects for viewing in PyMOL, etc. This window allows for easy opening of these results files.

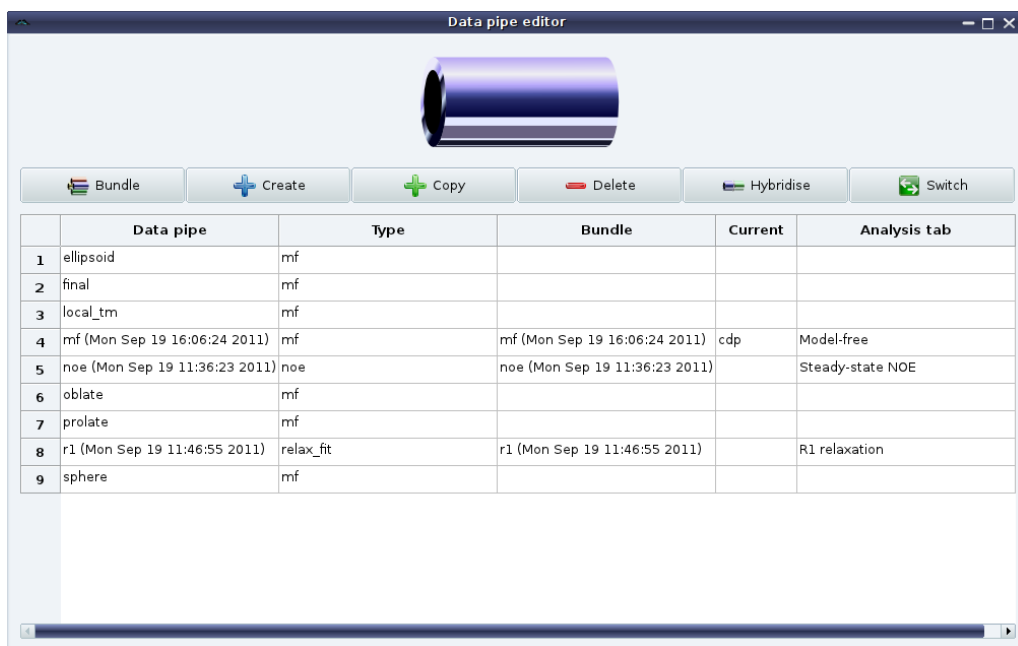


Figure 1.12: Screenshot of the relax GUI interface – the pipe editor window. One analysis may consist of one or more data pipes. And each analysis has its own unique set of data pipes. This editor allows for the easy manipulation of data pipes for advanced users.

```

The relax prompt

relax 1.3.14

Molecular dynamics by NMR data analysis

Copyright (C) 2001-2006 Edward d'Auvergne
Copyright (C) 2006-2012 the relax development team

This is free software which you are welcome to modify and redistribute under the conditions of the
GNU General Public License (GPL). This program, including all modules, is licensed under the GPL
and comes with absolutely no warranty. For details type 'GPL' within the relax prompt.

Assistance in using the relax prompt and scripting interface can be accessed by typing 'help' within
the prompt.

Processor fabric: Uni-processor.

Startup script executed: /etc/pythonrc.py
relax> pipe.display()
Data pipe name      Data pipe type      Current
'ellipsoid'         mf
'noe (Mon Sep 19 11:36:23 2011)' noe
'mf (Mon Sep 19 16:06:24 2011)' mf
'r1 (Mon Sep 19 11:46:55 2011)' relax_fit
'local_tm'          mf
'sphere'            mf
'oblate'            mf
'final'             mf
'prolate'           mf
relax>

```

Figure 1.13: Screenshot of the relax GUI interface – the prompt window. This window mimics relax in the prompt user interface mode, and provides the full power of the prompt/script UI modes within the GUI.

## 1.4 Usage of the name relax

The program relax is so relaxed that the first letter should always be in lower case!

## Chapter 2

# Installation instructions

### 2.1 Dependencies

The following packages need to be installed before using relax:

**Python:** Version 2.5 or higher.

**NumPy:** Version 1.0.4 or higher. This package is used for most of the numerical calculations within relax.

**SciPy:** Version 0.7.1 or higher. This package is optional. It is required only for the frame order theory analyses.

**wxPython:** Version 2.8 or higher. This package is also optional. It is required for the operation of the graphical user interface (GUI).

**mpi4py:** Version 1.2 or higher. This optional dependency is essential for running relax in MPI multi-processor mode.

Older versions of these packages may work, use them at your own risk. If, for older dependency versions, errors do occur please submit a bug report to the bug tracker at <https://gna.org/bugs/?group=relax>. That way a solution may be created for the next relax release.

Note that only the official Python distribution from <http://python.org> is supported. If you use the Enthought Python Distribution (EPD) or other non-official distributions you may encounter problems with the relax C modules, the graphical user interface, or other issues. These alternative distributions are to be used at your own risk. Any issues encountered will not be considered as relax bugs.

## 2.2 Installation

### 2.2.1 The source releases

Two types of software packages are available for download – the precompiled and source distribution. Currently only relaxation curve-fitting requires compilation to function and all other features of relax will be fully functional without compilation. If relaxation curve-fitting is required but no precompiled version of relax exists for your operating system or architecture then, if a C compiler is present, the C code can be compiled into the shared objects files `*.so`, `*.pyd` or `*.dylib` which are loaded as modules into relax. To build these modules the Scons system from <http://scons.org/> is required. This software requires the Python and numpy header files installed. Once Scons is installed type

```
$ scons
```

in the base directory where relax has been installed and the C modules should, hopefully, compile without any problems. Otherwise please submit a bug report to the bug tracker at <https://gna.org/bugs/?group=relax>.

### 2.2.2 Installation on GNU/Linux

To install the program relax on a GNU/Linux system download either the precompiled distribution labelled `relax-x.x.x.GNU-Linux.arch.tar.bz2` matching your machine architecture or the source distribution `relax-x.x.x.src.tar.bz2`. A number of installation methods are possible. The simplest way is to switch to the user “root”, unpack and decompress the archive within the `/usr/local` directory by typing, for instance

```
$ tar jxvf relax-x.x.x.GNU-Linux.i686.tar.bz2
```

then create a symbolic link in `/usr/local/bin` by moving to that directory and typing

```
$ ln -s ../relax/relax .
```

and finally possibly creating the byte-compiled Python `*.pyc` files to speed up the start time of relax by typing

```
$ python -m compileall .
```

in the relax base directory. Alternatively if the Scons system is installed, by typing as the root user

```
$ scons install
```

in the relax base directory, a directory in `/usr/local/` called `relax` will be created, all the uncompressed and untarred files will be copied into this directory, a symbolic link in `/usr/local/bin` to the file `/usr/local/relax/relax` will be created, and then finally the Python `*.pyc` files will be byte-compiled. To change the installation path to a non-standard location the Scons script `sconstruct` in the base relax directory should be modified by changing the variable `INSTALL_PATH` to point to the desired location.



### 2.2.3 Installation on MS Windows

In addition to the above dependencies, running relax on MS Windows requires a number of additional programs. These include:

**pyreadline:** Version 1.3 or higher.

**ctypes:** The pyreadline package requires ctypes.

To install, simply download the pre-compiled binary distribution `relax-x.x.x.Win32.zip` or the source distribution `relax-x.x.x.src.zip` and extract the files to `C:\Program Files\relax-x.x.x`. Then add this directory to the system environment path (in Windows XP, right click on “My Computer”, go to “Properties”, click on the “Advanced” tab, and click on the “Environment Variables” button. Then double click on the “Path” system variable and add the text “`;C:\Program Files\relax-x.x.x`” to the end of variable value field. The Python installation must also be located on the path (add the text “`;C:\Python27`”, changing the text to point to the correct directory, to the field). To run the program from any directory inside the Windows command prompt (or dos prompt) type:

```
C:\> relax
```

Note that the pre-compiled binary distribution was built using a specific Python version and that that version may need to be installed for the modules to be loaded. More details are given on the [download](#) webpage.

### 2.2.4 Installation on Mac OS X

There are three ways of installing relax on a Mac. These are described at <http://www.nmr-relax.com/download.html> and are the pre-compiled relax application, the Fink or the source releases.

#### The relax application

The stand-alone relax application requires none of the dependencies listed above to be installed. It is a universal binary compiled for the i386, x86-64 and PPC CPU architectures (fat3) using the Mac OS X 10.5 framework. It should therefore run on Leopard, Snow Leopard, and Lion. This very large bundle does not require system administrator access to run.

#### Fink

Certain relax versions are available for Mac OS X within the Fink project. These can be installed for Python 2.7 with the command:

```
> fink install relax-py27
```

The relax releases packaged within Fink can be browsed at <http://pdb.finkproject.org/pdb/browse.php?name=relax>. If the desired version is

not available, please download the relevant source package below or contact the fink project using the “Maintainer” email address given in the relax fink pages.

Note that when installing via fink, all the dependencies will be automatically selected and installed as well. Although automatic, when starting from scratch that there could be well over 250 source packages that need to be compiled (to set up the full GNU compilation chain and other libraries which are then required to build Python, numpy, scipy, etc.). This may take anywhere between 2 days to over a week (don’t forget to mention this fact to your poor sys-admin).

The fink relax packages for different Python versions are [relax-py27](#), [relax-py26](#), [relax-py25](#) and [relax-py24](#).

### Source release

See Section [2.2.1](#) on page [24](#).

### 2.2.5 Installation on your OS

For all others systems, please use the source distribution files and the Scons software to build the C modules.

### 2.2.6 Running a non-compiled version

Compilation of the C code is not essential for running relax, however certain features of the program will be disabled. Currently only the exponential curve-fitting for determining the  $R_1$  and  $R_2$  relaxation rates requires compilation. To run relax without compilation install the dependencies detailed above, download the source distribution which should be named `relax-x.x.x.src.tar.bz2`, extract the files, and then run the file called `relax` in the base directory.

## 2.3 Optional programs

The following is a list of programs which can be used by relax although they are not essential for normal use.

### 2.3.1 Grace

Grace is a program for plotting two dimensional data sets in a professional looking manner. It is used to visualise parameter values. It can be downloaded from <http://plasma-gate.weizmann.ac.il/Grace/>.

### 2.3.2 OpenDX

Version 4.1.3 or compatible. OpenDX is used for viewing the output of the space mapping function and is executed by passing the command `dx` to the command line with various options. The program is designed for visualising multidimensional data and can be found at <http://www.opendx.org/>.

### 2.3.3 Molmol

Molmol is used for viewing the PDB structures loaded into the program and to display parameter values mapped onto the structure.

### 2.3.4 PyMOL

PDB structures can also be viewed using PyMOL. This program can also be used to display geometric objects generated by relax for representing physical concepts such as the diffusion tensor and certain cone diffusion models.

### 2.3.5 Dasha

Dasha is a program used for model-free analysis of NMR relaxation data. It can be used as an optimisation engine to replace the minimisation algorithms implemented within relax.

### 2.3.6 Modelfree4

Art Palmer's Modelfree4 program is also designed for model-free analysis and can be used as an optimisation engine to replace relax's high precision minimisation algorithms.



## Chapter 3

# Open source infrastructure

### 3.1 The relax web sites

The main web site for relax is <http://www.nmr-relax.com>. From these pages general information about the program, links to the latest documentation, links to the most current software releases, and information about the mailing lists are available. There are also Google search capabilities built into the pages for searching both the HTML version of the manual and the archives of the mailing lists.

The relax web site is hosted by the Gna! project (<https://gna.org/>) which is described as “a central point for development, distribution and maintenance of Libre Software (Free Software) projects”. relax is a registered Gna! project and its primary Gna! web site is <https://gna.org/projects/relax>. This site contains many more technical details than the main web site.

### 3.2 The mailing lists

A number of mailing lists have been created covering different aspects of relax. These include the announcement list, the relax users list, the relax development list, and the relax committers list.

#### 3.2.1 relax-announce

The relax announcement list “relax-announce at gna.org” is reserved for important announcements about the program including the release of new program versions. The amount of traffic on this list is relatively low. If you would like to receive information about relax you can subscribe to the list by visiting the information page at <https://mail.gna.org/listinfo/relax-announce/>. Previous announcements can be viewed at <https://mail.gna.org/public/relax-announce/>.

### 3.2.2 relax-users

If you would like to ask questions about relax, discuss certain features, receive help, or to communicate on any other subject related to relax the mailing list “relax-users at gna.org” is the place to post your message. To subscribe to the list go to the relax-users information page at <https://mail.gna.org/listinfo/relax-users/>. You can also browse the mailing list archives at <https://mail.gna.org/public/relax-users/>.

### 3.2.3 relax-devel

A second mailing list exists for posts relating to the development of relax. The list is “relax-devel at gna.org” and to subscribe go to the relax-devel information page at <https://mail.gna.org/listinfo/relax-devel/>. Feature requests, program design, or any other posts relating to relax’s structure or code should be sent to this list instead. The mailing list archives can be browsed at <https://mail.gna.org/public/relax-devel/>.

### 3.2.4 relax-commits

One last mailing list is the relax commits list. This list is reserved for automatically generated posts created by the version control software which looks after the relax source code and these web pages. If you would like to become a developer you can subscribe to the list at relax-commits information page <https://mail.gna.org/listinfo/relax-commits/>. The list can also be browsed at <https://mail.gna.org/public/relax-commits/>.

### 3.2.5 Replying to a message

When replying to a message on these lists remember to hit ‘respond to all’ so that the mailing list is included in the CC field. Otherwise your message will only be sent to the original poster and not return back to the list. Only messages to relax-users and relax-devel will be accepted. If you are using Gmail’s web based interface, please do not click on ‘Edit Subject’ as this currently mangles the email headers, creates a new thread on the mailing list, and makes it difficult to follow the thread.

## 3.3 Reporting bugs

One of the philosophies in the construction of relax is that if there is something which is not immediately obvious then that is considered a design bug. If any flaws in relax are uncovered including general design flaws, bugs in the code, or documentation issues these can be reported within relax’s bug tracker system. The link to submit a bug is <https://gna.org/bugs/?group=relax&func=additem> while the main page for browsing, submitting, viewing the statistics, or searching through the database is at <https://gna.org/bugs/?group=relax>. Please do not report bugs to personal email addresses or to the mailing lists.

When reporting a bug please include as much information as possible so that the problem can be reproduced. Include information such as the release version or the revision number if the repository sources are being used. Also include all the steps performed in order to trigger the bug. Attachment of files is allowed so scripts and subsets of the input data can be included. However please do not attach large files to the report. Prior to reporting the bug try to make sure that the problem is indeed a bug and if you have any doubts please feel free to ask on the relax-users mailing list. To avoid duplicates be sure that the bug has not already been submitted to the bug tracker. You can search the bugs from the page <https://gna.org/project/search.php?group=relax>.

Once the bug has been confirmed by one of the relax developers you may speed up the resolution of the problem by trying to fixing the bug yourself. If you do wish to play with the source code and try to fix the issue see the relax development chapter of this manual on how to check out the latest sources (Chapter 11 on page 191), how to generate a patch (which is just the output of diff in the ‘unified’ format), and the guidelines for the format of the code.

### 3.4 Latest sources – the relax repositories

relax’s source code is kept within a version control system called Subversion (<http://subversion.tigris.org/>). Subversion or SVN allows fine control over the development of the program. The repository contains all information about every change ever made to the program. To learn more about the system the Subversion book located at <http://svnbook.red-bean.com/> is a good place to start. The contents of the relax repository can be viewed on-line at <http://svn.gna.org/viewcvs/relax/>. The current sources can be downloaded using the SVN protocol by typing

```
$ svn co svn://svn.gna.org/svn/relax/trunk relax-trunk
```

however if this does not work, try the command

```
$ svn co http://svn.gna.org/svn/relax/trunk relax-trunk
```

to download using the HTTP protocol. The entire relax repository is backed up daily to <http://svn.gna.org/daily/relax.dump.gz>.

### 3.5 News

Summaries of the latest news on relax can be found on the relax web site <https://gna.org/projects/relax>. However more information can be found at the dedicated news page <https://gna.org/news/?group=relax>.

### 3.6 The relax distribution archives

The relax distribution archives, the files to download to install relax, can be found at <http://download.gna.org/relax/>. If a compiled binary distribution for your architecture

does not exist you are welcome to create this distribution yourself and submit it for inclusion in the relax project. To do this a number of steps are required. Firstly, the code to each relax release or version resides in the ‘tags’ directory of the relax repository. To check out version 2.1.1 for example type

```
$ svn co svn://svn.gna.org/svn/relax/tags/2.1.1 relax
```

Again the sources are available through HTTP by typing

```
$ svn co http://svn.gna.org/svn/relax/tags/2.1.1 relax
```

The binary distribution can then be created for your architecture by shifting to the main directory of the checked out sources and typing

```
$ cd relax
$ scons binary_dist
```

At the end SCons will attempt to make a GPG signature for the newly created archive. However this will fail as the current relax private GPG key is not available for security reasons. If the SCons command fails, excluding the GPG signing, please submit a bug report with as much information possible including the details described next to <https://gna.org/bugs/?group=relax&func=additem> (the python and SCons version numbers may also be useful). Once the file has been created post a message to the relax development mailing list describing the compilation and the creation of the archive, the relax version number, the machine architecture, operating system, and the name of the new file. Do not attach the file though. You will then receive a response explaining where to send the file to. For security the archive will be thoroughly checked and if the source code is identical to that in the repository and the C modules are okay, the file will be GPG signed and uploaded to <http://download.gna.org/relax/>.



## Chapter 4

# The relax data model

### 4.1 The concept of the relax data model

To begin to understand how to use relax, a basic comprehension of the relax data model is needed. The data model includes the concepts of the relax data store, the data pipes, the molecule, residue and spin data structures and the interatomic data containers. These concepts are independent of the specific analyses presented in the next chapters and are important for setting up relax.

### 4.2 The data model

#### 4.2.1 The relax data store

All permanent data handled by relax is kept in a structure known as the relax data store. This structure is initialised when relax is launched. The data store is primarily organised into a series of objects known as data pipes, and all usage of relax revolves around the flow of information in these data pipes.

#### Data pipes



The first thing one must do when relax is launched is to create a data pipe. When using the GUI, a base data pipe will be created when opening one of the automatic analyses via the analysis selection window (see figure 1.4 on page 12). This will also create a data pipe bundle for the analysis (*vide infra*). Alternatively the data pipe editor window can be

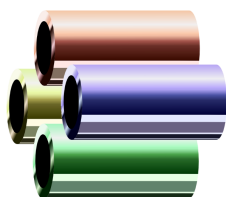
used to create data pipes (see figure 1.12 on page 21). For the prompt/scripting modes, or the “User functions→pipe→create” menu entry, a data pipe can be initialised by specifying the unique name of the data pipe and the data pipe type:

```
1 pipe.create(pipe_name='NOE 1200 MHz', pipe_type='noe')
```

A number of relax operations will also create data pipes by merging a group of pipes or branching pre-existing pipes. See section 1.2.6 on page 10 for additional details.

All data not associated with spin systems will be stored in the base data pipe. This includes information such as global optimisation statistics, diffusion tensors, alignment tensors, 3D structural data, the molecule, residue and spin container data structure and the interatomic data containers. One data pipe from the set will be defined as being the current data pipe, and all operations in relax will effect data from this pipe. The `pipe.switch` user function in all UI modes can be used to change which pipe is the current data pipe. In the GUI, switching between analysis tabs will automatically switch the current data pipe to match the analysis being displayed.

## Data pipe bundles



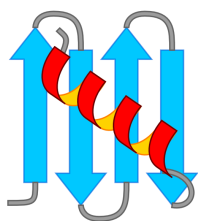
Related data pipes can be grouped into a ‘bundle’. For example if the data pipes “sphere”, “oblate spheroid”, “prolate spheroid”, and “ellipsoid” preexist, these can be grouped into a bundle called “diffusion tensors” with the following series of user function calls:

```
1 pipe.bundle(bundle='diffusion tensors', pipe='sphere')
2 pipe.bundle(bundle='diffusion tensors', pipe='oblate spheroid')
3 pipe.bundle(bundle='diffusion tensors', pipe='prolate spheroid')
4 pipe.bundle(bundle='diffusion tensors', pipe='ellipsoid')
```

The data pipe editor window of the GUI can also be used to bundle pipes together (see figure 1.12 on page 21).

### 4.2.2 Molecule, residue, and spin containers

Within a data pipe is the molecule, residue, and spin container data structure. Data which is specific to a given nucleus is stored in a special spin container structure. This includes relaxation data, model-free parameters, reduced spectral density mapping values, spin specific optimisation parameters, chemical shift tensor information, pseudo-contact shift values, etc. The spin containers can be created from 3D structural data or a sequence file, as described in the next two sections, or manually built.



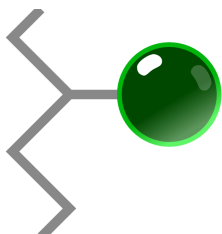
### Molecule containers

The spin containers are part of a nested set of containers, and are graphically depicted in the spin viewer window of the GUI in figure 1.10 on page 20. As can be seen from the figure, the top level holds a single molecular container. Multiple molecular containers can be present if the study is of a molecular complex. Using the GUI menus or the prompt/scripting mode, molecule containers can be manually created with the user function:

```
1 molecule.create(mol_name='glycerol', mol_type='organic molecule')
```

In the spin viewer window of the GUI, right clicking on the “Spin system information” element will pop up a menu with an entry for adding molecule containers. Right clicking on molecule containers will show a pop up menu with an entry for permanently deleting the container.

### Residue containers



Nested within the molecule containers are residue containers. These are graphically depicted in the spin viewer window (see figure 1.10 on page 20). Each molecule container can possess multiple residues. These require either a unique residue number or unique residue name. For organic molecules where the residue concept is meaningless, all spin containers can be held within a single unnamed and unnumbered residue container. Using the GUI menus or the prompt/scripting mode, residue containers can be manually created with the user function:

```
1 residue.create(res_num='-5', res_name='ASP')
```

Alternatively residues can be added in the spin viewer window from the pop up menu when right clicking on molecule containers, and can be deleted via the pop up menu when right clicking on the residue to delete.

## Spin containers



Spin containers are nested within a residue container (again graphically depicted in the spin viewer window in figure 1.10 on page 20). Multiple spin containers can exist per residue. This allows, for example, a single model-free analysis simultaneously on the backbone nitrogen spins, side-chain tryptophan indole nitrogen spins and alpha carbon spins. Or, for example, studying the pseudocontact shifts for all nitrogen, carbon and proton spins in the molecule simultaneously.

Spin containers can be manually added via the `spin.create` user function in the GUI or prompt/scripting mode:

```
1 spin.create(spin_num='200', spin_name='NE1')
```

The spin viewer window can also be used by right clicking on residue containers.

## Spin ID strings

Spins are often identified in relax using their ID strings. The spin ID strings follow the basic construct found in a number of other NMR software such as MOLMOL. The identification string is composed of three components:

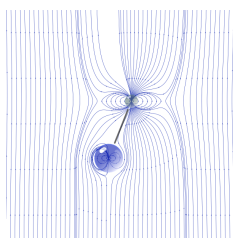
- The molecule ID token beginning with the “#” character,
- The residue ID token beginning with the “:” character,
- The atom or spin system ID token beginning with the “@” character.

Each token can be composed of multiple elements – one per spin – separated by the “,” character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the “-” character. Negative numbers are supported. The full ID string specification is “#<mol\_name> :<res\_id>[, <res\_id>[, <res\_id>, ...]] @<atom\_id>[, <atom\_id>[, <atom\_id>, ...]]”, where the token elements are “<mol\_name>”, the name of the molecule, “<res\_id>”, the residue identifier which can be a number, name, or range of numbers, “<atom\_id>”, the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the “#” character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can, in some instances, be used to select spins. For example the string “@H\*” will select the protons ‘H’, ‘H2’ and ‘H98’.

## 4.3 Interatomic data containers



Separate from the spin containers, yet strongly linked to them, are the interatomic data containers. These containers are grouped together within the same data pipe as the spins they point to. These define interactions between two spins located anywhere within the molecule, residue and spin nested data structure. These are automatically created when reading in data defined between two spins such as RDCs and NOE distance constraints. They can also be created using the `interatom.define` user function:

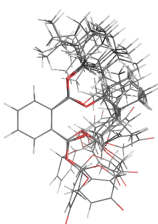
```
1 interatom.define(spin_id1=':2@N', spin_id2=':2@H')
```

As the interatomic data container concept is relatively new, how they are created and handled is likely to evolve and change in the future.

## 4.4 Setup in the prompt/script UI

Below are three different examples showing how to set up the relax data model for any analysis type requiring spin specific data.

### 4.4.1 Script mode – spins from structural data



3D structural data is stored at the level of the current data pipe. This data is completely separate from the molecule, residue and spin data structure. However the structural data can be used to generate the spin containers. For example for the nitrogen relaxation in a model-free analysis where both the nitrogen and proton are needed to define the magnetic dipole-dipole relaxation:

```
1 # Create a data pipe.
2 pipe.create(pipe_name='ellipsoid', pipe_type='mf')
3
4 # Load the PDB file.
5 structure.read_pdb('1f3y.pdb')
6
7 # Set up the 15N and 1H backbone spins.
```

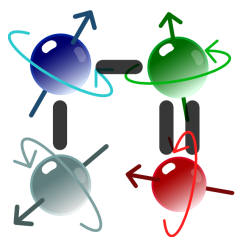
```

8  structure.load_spins('@N', ave_pos=True)
9  structure.load_spins('@H', ave_pos=True)
10
11 # Set up the 15N and 1H for the tryptophan indole ring.
12 structure.load_spins('@NE1', ave_pos=True)
13 structure.load_spins('@HE1', ave_pos=True)
14
15 # Define the spin isotopes.
16 spin.isotope('15N', spin_id='@N*')
17 spin.isotope('1H', spin_id='@H*')
```

The `structure.read_pdb` user function will load the structural data into the current data pipe, and the `structure.load_spins` user function will create the molecule, residue, and spin containers as needed. This will also load atomic position information into the matching spin containers. The `spin.isotope` user function is required to define the magnetic dipole-dipole interaction and is information not present in the PDB file.

Note that if structural data from the PDB is used to generate the spin containers, then all subsequent data loaded into relax must follow the exact naming convention from the PDB file. Automatic residue name matching (i.e. ‘GLY’ = ‘Gly’ = ‘gly’ = ‘G’) is currently not supported.

#### 4.4.2 Script mode – spins from a sequence file



Alternatively to setting up the molecule, residue, and spin containers via 3D structural data, a plain text columnar formatted file can be used. This is useful for when no 3D structure exists for the molecule. It also has the advantage that the residue and atom names need not conform to the PDB standard. An example for reading sequence data is:

```

1  # Create a data pipe.
2  pipe.create(pipe_name='R1 1200', pipe_type='relax_fit')
3
4  # Set up the 15N spins.
5  sequence.read(file='noe.500.out', mol_name_col=1, res_num_col=2, res_name_col=3,
6                spin_num_col=4, spin_name_col=5)
7  spin.element(element='N', spin_id='@N*')
8  spin.isotope('15N', spin_id='@N')
```

Here the molecule, residue, and spin information is extracted from the “noe.500.out” file which could look like:

| # | mol_name           | res_num | res_name | spin_num | spin_name | value            | error            |
|---|--------------------|---------|----------|----------|-----------|------------------|------------------|
| 1 | Ap4Aase_new_3_mol1 | 1       | GLY      | 1        | N         | None             | None             |
| 2 | Ap4Aase_new_3_mol1 | 2       | PRO      | 11       | N         | None             | None             |
| 3 | Ap4Aase_new_3_mol1 | 3       | LEU      | 28       | N         | None             | None             |
| 4 | Ap4Aase_new_3_mol1 | 4       | GLY      | 51       | N         | 0.03892194698453 | 0.01903177024613 |

|                    |    |     |     |     |                  |                  |
|--------------------|----|-----|-----|-----|------------------|------------------|
| Ap4Aase_new_3_mol1 | 5  | SER | 59  | N   | 0.31240422567912 | 0.01859693729836 |
| Ap4Aase_new_3_mol1 | 6  | MET | 71  | N   | 0.42850831873249 | 0.0252585632304  |
| Ap4Aase_new_3_mol1 | 7  | ASP | 91  | N   | 0.53054928103134 | 0.02799062314416 |
| Ap4Aase_new_3_mol1 | 8  | SER | 104 | N   | 0.56528429775819 | 0.02170612146773 |
| Ap4Aase_new_3_mol1 | 9  | PRO | 116 | N   | None             | None             |
| Ap4Aase_new_3_mol1 | 40 | TRP | 685 | N   | 0.65394813490548 | 0.03830061886537 |
| Ap4Aase_new_3_mol1 | 40 | TRP | 698 | NE1 | 0.67073879732046 | 0.01426066343831 |

The file can contain columns for the molecule name, the residue name and number, and the spin name and number in any order though not all are needed. For example for a single protein system, the molecule name, residue name and spin number are nonessential. Or for an organic molecule, the molecule name, residue name and number and spin number could be nonessential. The subsequent user functions in the above example are used to set up the spin containers appropriately for a model-free analysis. These are not required in the automatic analysis of GUI as these user functions will be presented to you when adding relaxation data, or when clicking on the heteronucleus and proton buttons (“X isotope” and “H isotope”).

In the GUI, the creation of molecule, residue, and spin containers from a sequence file is also available via the “Load spins” wizard within the spin viewer window (*vide supra*).

#### 4.4.3 Script mode – manual construction

For the masochists out there, the full molecule, residue and spin data structure can be manually constructed. For example:

```

1 # Manually create the molecule, residue, and spin containers.
2 molecule.create(mol_name='Ap4Aase', mol_type='protein')
3 residue.create(res_num=1, res_name='GLY')
4 residue.create(res_num=3, res_name='LEU')
5 residue.create(res_num=96, res_name='TRP')
6 spin.create(res_num=1, spin_name='N')
7 spin.create(res_num=3, spin_name='N')
8 spin.create(res_num=96, spin_name='N')
9 spin.create(res_num=96, spin_name='NE1')
```

These user functions can be repeated until the full sequence has been constructed.

## 4.5 Setup in the GUI

### 4.5.1 GUI mode – setting up the data pipe

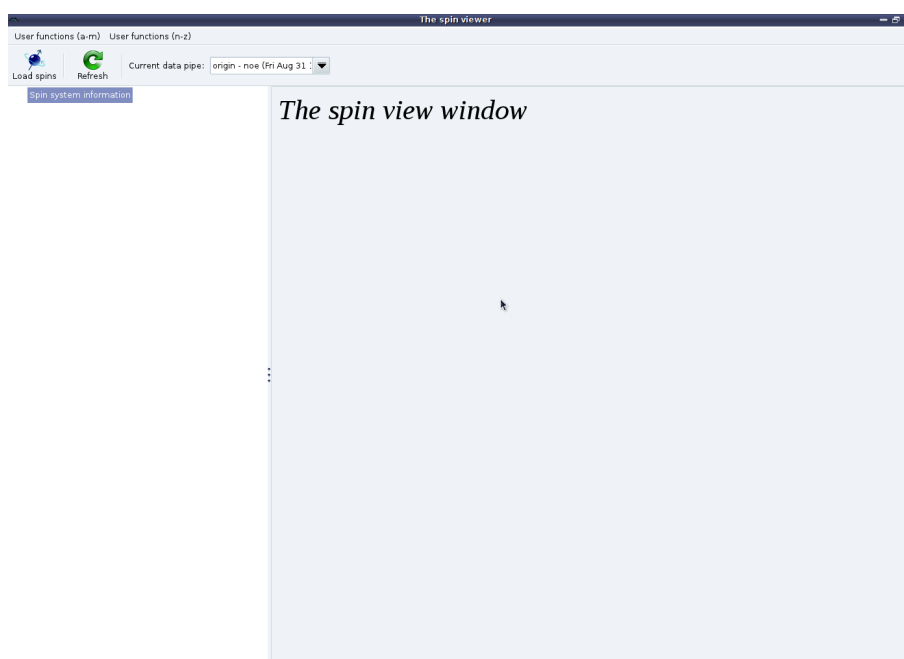
In the GUI, the most common way to create the data pipe is to initialise one of the auto-analyses via the analysis selection wizard (see Figure 1.4 on page 12). The initialisation will create the appropriate starting data pipe. Alternatively the data pipe editor can be used (see Figure 1.12 on page 21). Or the “User functions→pipe→create” menu item can be selected for graphical access to the `pipe.create` user function.

### 4.5.2 GUI mode – spins from structural data

For this section, the example of protein  $^{15}\text{N}$  relaxation data will be used to illustrate how to set up the data structures. To manipulate the molecule, residue and spin data structures in the GUI, the most convenient option is to use the spin viewer window (see Figure 1.10 on page 20). This window can be opened in four ways:

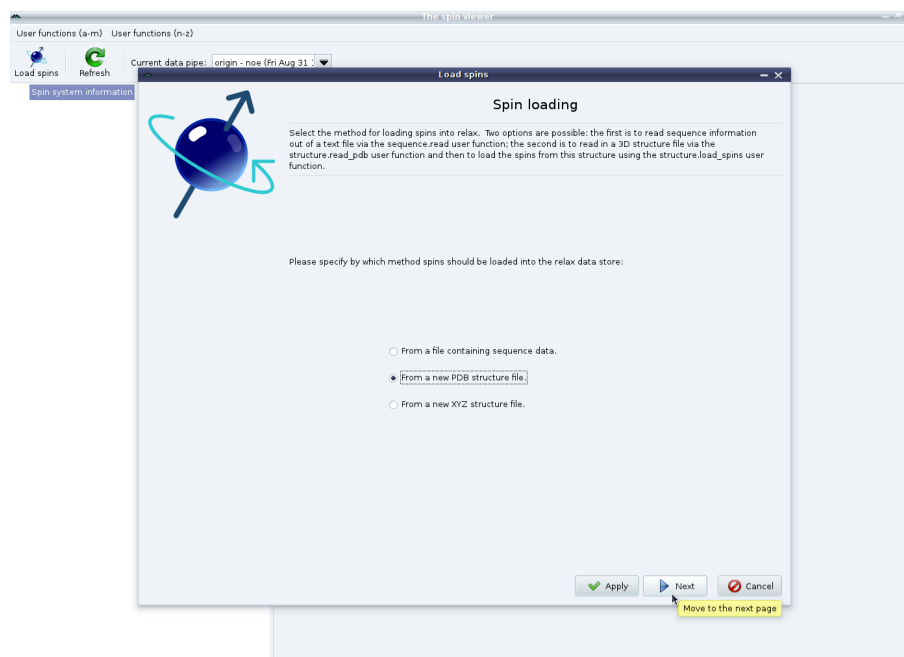
- The “View→Spin viewer” menu item,
- The “[Ctrl+T]” key combination,
- The spin viewer icon in the toolbar (represented by the blue spin icon),
- The “Spin editor” button part of the “Spin systems” GUI element in the specific analysis tabs.

You will then see:

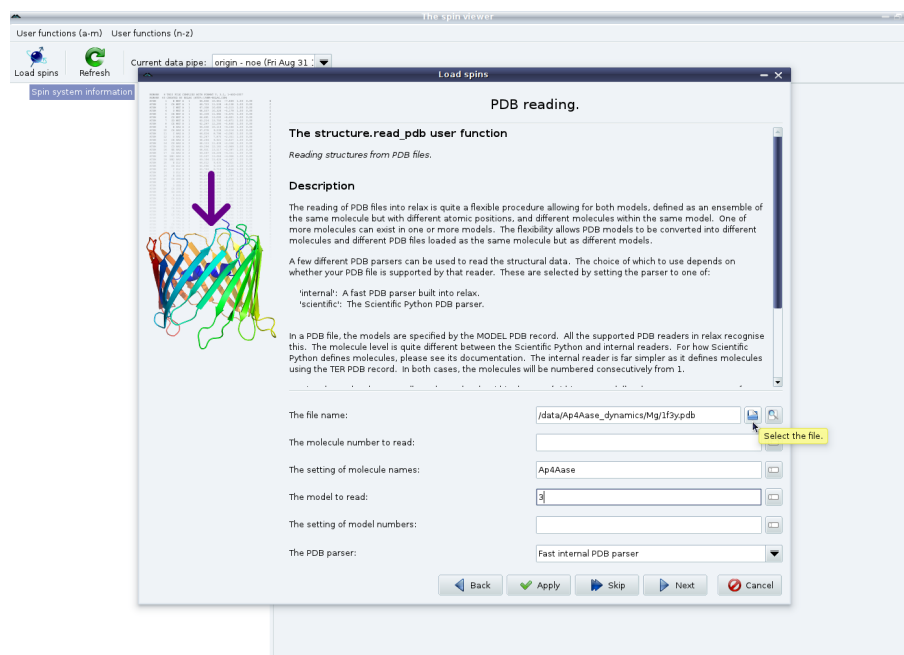


At this point, click on the “Load spins” button (or the “Load spins” menu entry from the right click pop up menu) to launch the spin loading wizard. A number of options will be presented to you:

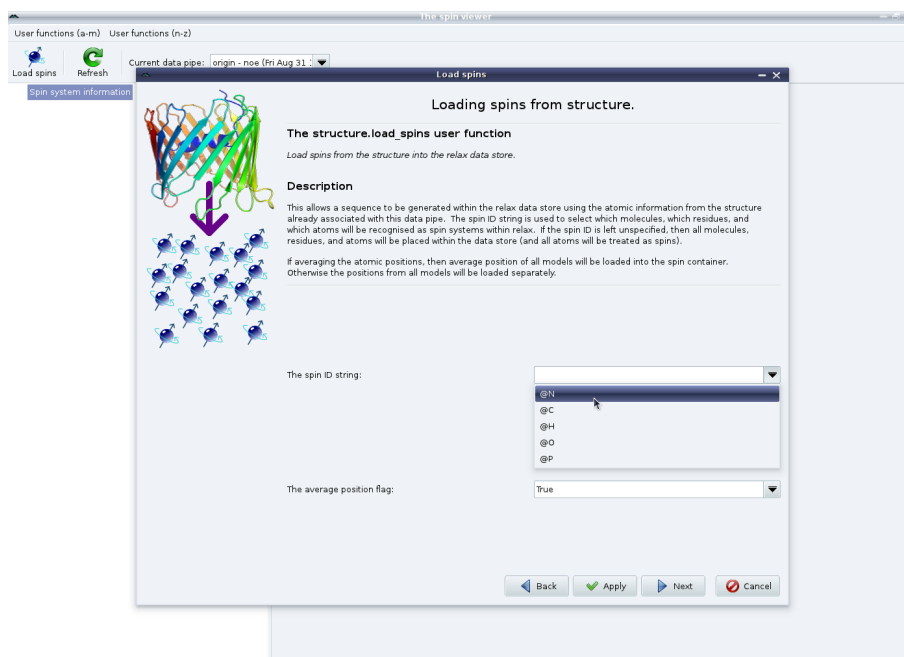




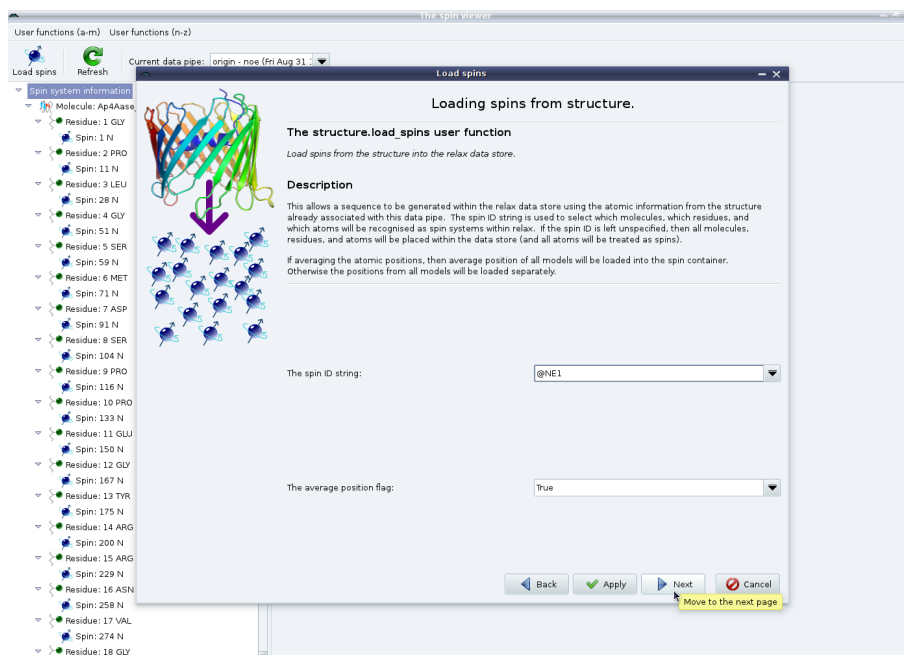
Here the spins will be loaded from a PDB file. If you do not have a 3D structure file, please see the next section. After selecting “From a new PDB structure file” and clicking on “Next”, you will see:



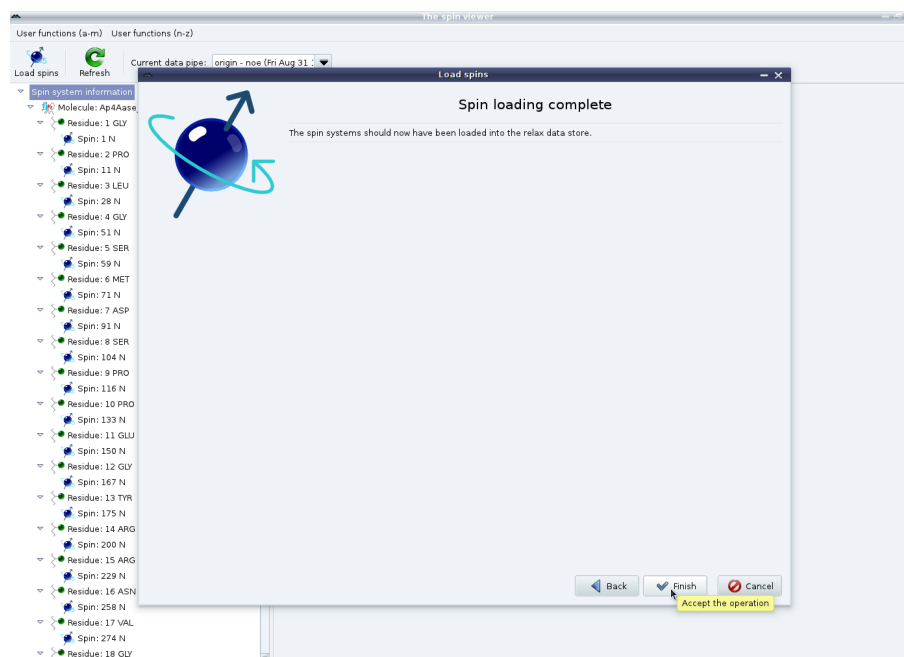
Now select the PDB file you wish to use. The other options in this screen allow you to handle NMR models and multiple molecules within a single PDB file. These options are explained in the window. Hovering the mouse over the options will give additional hints. In this example, the 3<sup>rd</sup> model from the 1F3Y PDB file will be read and the single molecule will be named “Ap4Aase” to override the default naming of “1f3y\_mol1”. Now click on “Next” to bring up the spin loading page:



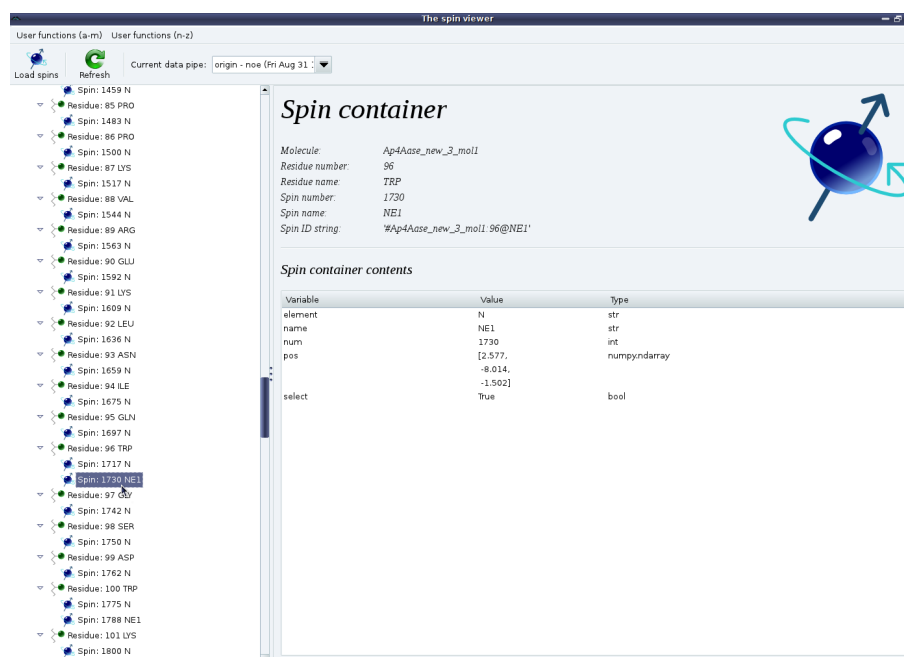
This is a bit more complicated. In this example we are studying the backbone dynamics of  $^{15}\text{N}$  spins of a protein. Therefore first set the spin ID string to “@N” (which can be selected from the pull down) and click on “Apply” to set up the backbone spins. Do not click on “Next” yet. If the current study requires the specification of the dipole-dipole interaction (for example if it involves relaxation data – model-free analyses, consistency testing, reduced spectral density mapping; or the dipolar coupling – the N-state model or ensemble analyses, the Frame Order theory) you will also need to load the  $^1\text{H}$  spins as well. Therefore set the spin ID string to “@H” and click on “Apply” again.



Now change the spin ID string to “@N1” and then click on “Next” (or “Apply” if the Trp protons “@HE1” need to be loaded as well). This will add spin containers for the tryptophan indole  $^{15}\text{N}$  spins. Finally click on “Finish” to exit the wizard:



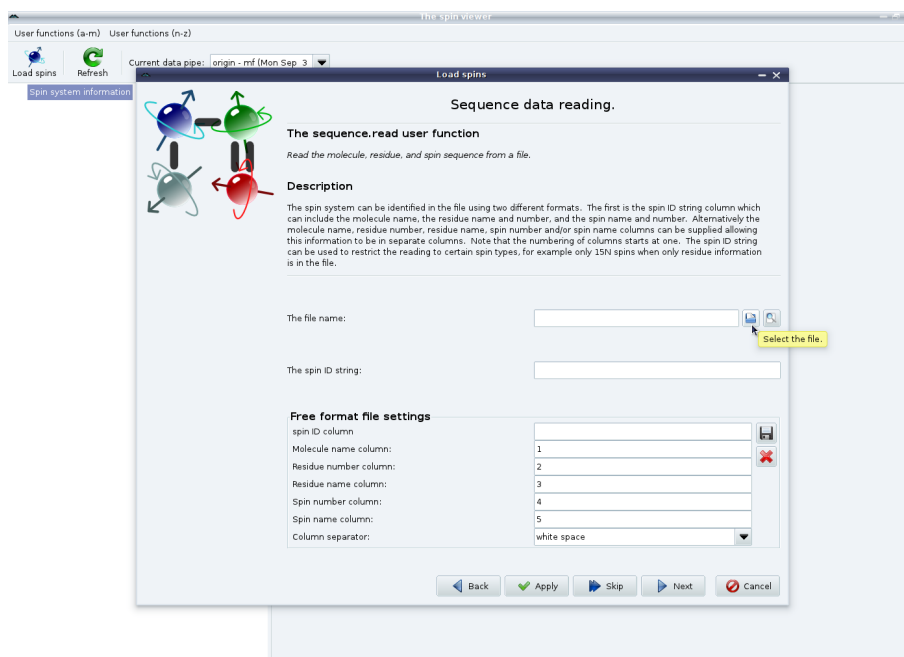
You should now see something such as:



If the  $^1\text{H}$  spins have been loaded as well, then you should see exactly twice as many spin containers as shown above.

### 4.5.3 GUI mode – spins from a sequence file

Starting from the empty spin viewer window on page 40), click on the “Load spins” button. You will then see the spin loading wizard (see page 41). Select the option for reading data from a sequence file. You should then see:



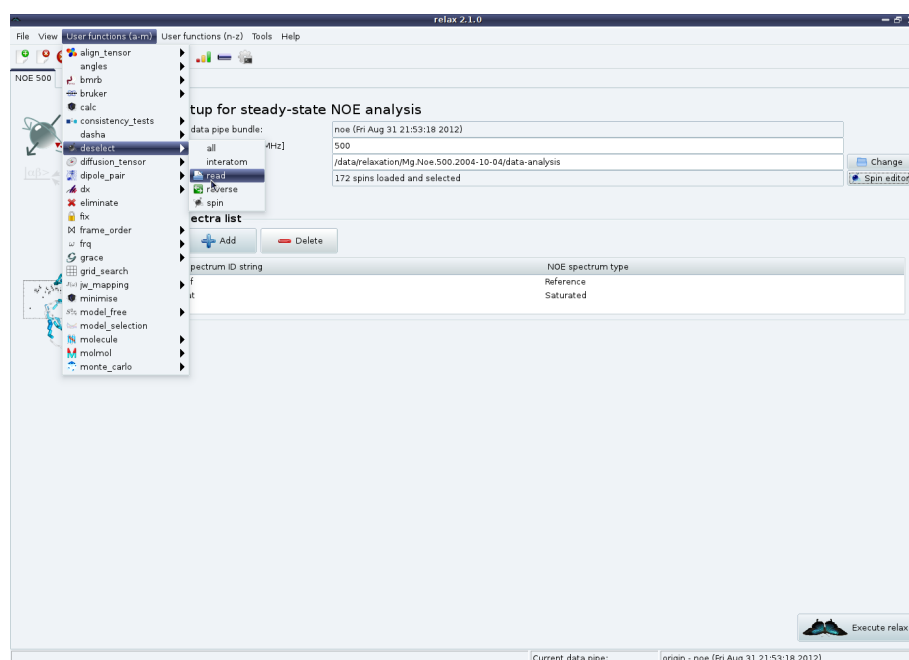
Select the file to load and change the “Free format file settings” as needed. An example of a suitable format is given on page 39. Click on “Next” to reach the wizard ending page (see 43). Finally click on “Finish” to exit the wizard.

#### 4.5.4 GUI mode – manual construction

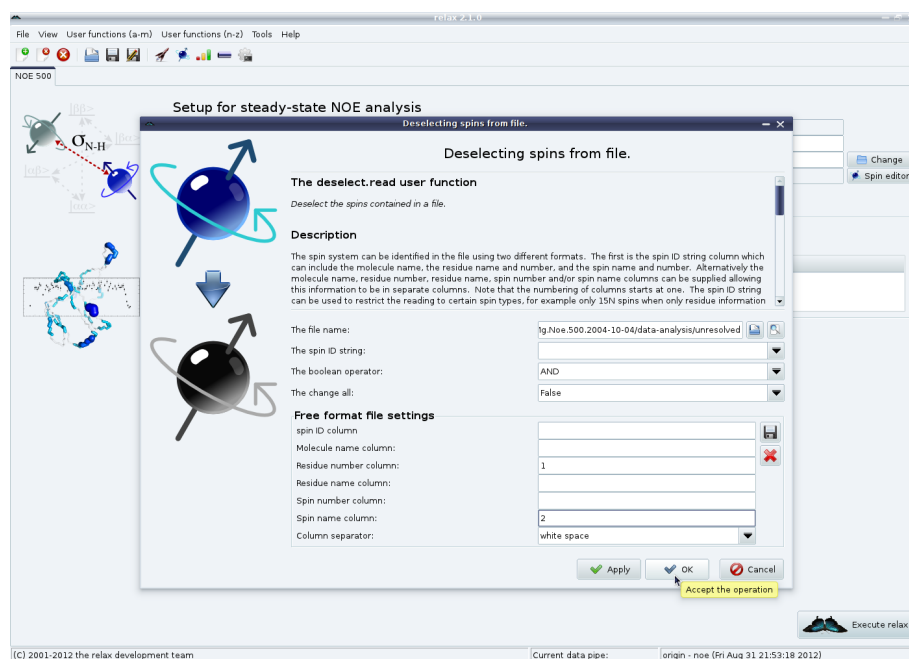
Just as in the prompt/script UI mode, the molecules, residues and spins can be manually added. First add a molecule by right clicking on the “Spin system information” element and selecting the relevant entry in the popup menu. Then right click on the newly created molecule container to add residues, and right click on residue containers to add spins.

#### 4.5.5 GUI mode – deselect spins

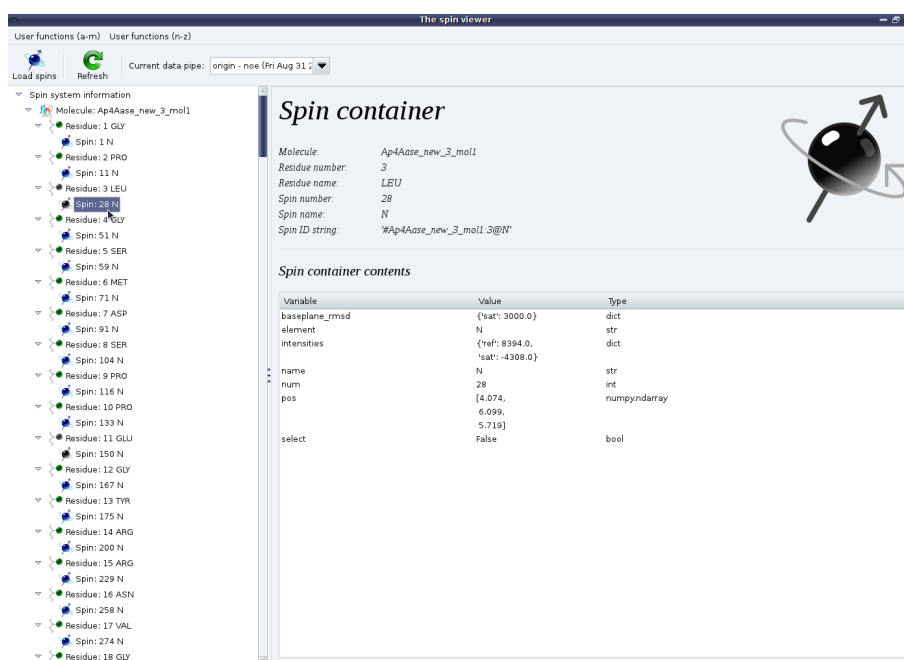
To deselect spins (for example if they are unresolved, overlapping peaks), click on the “User functions→deselect→read” menu item from the main relax window or the spin viewer window:



Select the file listing the unresolved spins and change the column numbers in the “Free format file settings” GUI element as needed:



Alternatively the spin editor window can be reopened and the spins manually deselected by right clicking on them and selecting “Deselect”. Returning to the spin editor window, you should now see certain spins coloured grey:



## 4.6 The next steps

This chapter presented the basics of setting up the relax data store, concepts which are needed for all analysis types built into relax. The next chapters will introduce specific analyses types – the steady-state NOE,  $R_1$  and  $R_2$  relaxation curve-fitting, and the automated full model-free analysis protocol of [d’Auvergne and Gooley \(2007, 2008b\)](#) – which build on the ideas introduced here.

## **Part II**

# **The specific analyses**





## Chapter 5

# The $R_1$ and $R_2$ relaxation rates – relaxation curve-fitting



### 5.1 Introduction to relaxation curve-fitting

The fitting of exponentials to relaxation curves (relaxation curve-fitting or as used throughout this chapter abbreviated simply as relax-fit) involves a number of steps including the loading of data, the calculation of both the average peak intensity across replicated spectra and the standard deviations of those peak intensities, selection of the experiment type, optimisation of the parameters of the exponential curves during the fit for each observed spin, Monte Carlo simulations to find the parameter errors, and saving and viewing the results. To simplify the process a sample script will be followed step by step as was done with the NOE calculation.

### 5.2 From spectra to peak intensities for the relaxation rates

The following subsections simply contain advice on how to go from the recorded FIDs to the peak lists ready to be input into relax. This need not be followed – it is simply a set of recommendations for obtaining the highest quality relaxation rates.

### 5.2.1 Temperature control and calibration



Before starting with the spectral processing, it should be noted that proper temperature control and calibration are essential for relaxation data. Small temperature changes can have an effect on the viscosity and hence global tumbling of the molecule being studied and, as the molecular diffusion tensor is the major contributor to relaxation, any non-consistent data will likely lead to artificial motions appearing in subsequent model-free analyses.

Per-experiment temperature calibration is essential and the technique used will need to be specified for BMRB data deposition. Note that the standard MeOH/ethylene glycol calibration of a spectrometer is of no use when you are running experiments which pump in large amounts of power into the probe head. Although the R1 experiment should be about the same temperature as a HSQC and hence be close to the standard MeOH/ethylene glycol spectrometer calibration, the R2 CPMG or spin lock and, to a lesser extent, the NOE pre-saturation pump a lot more power into the probe head. The power differences can either cause the temperature in the sample to be too high or too low. This is unpredictable as the thermometer used by the VT unit is next to the coils in the probe head and not inside the NMR sample. So the VT unit tries to control the temperature inside the probe head rather than in the NMR sample. However between the thermometer and the sample is the water of the sample, the glass of the NMR tube, the air gap where the VT unit controls air flow and the outside components of the probe head protecting the electronics. If the sample, the probe head or the VT unit is changed, this will have a different affect on the per-experiment temperature. The VT unit responds differently under different conditions and may sometimes over or under compensate by a couple of degrees. Therefore each relaxation data set from each spectrometer requires a per-experiment calibration.

Explicit temperature control techniques are also essential for relaxation data collection. Again the technique used will be asked for by relax for BMRB data deposition. A number of factors can cause significant temperature fluctuations between individual relaxation experiments. This includes the daily temperature cycle of the room housing the spectrometer, different amounts of power for the individual experiments, etc. The best methods for eliminating such problems are single scan interleaving and temperature compensation block. Single scan interleaving is the most powerful technique for averaging the temperature fluctuations not only across different experiments, but also across the entire measurement time. The application of off-resonance temperature compensation blocks at the start of the experiment is useful for the R2 and will normalise the temperature between the individual experiments, but single scan or single fid interleaving is nevertheless required for normalising the temperature across the entire measurement.

### 5.2.2 Spectral processing

For the best measurement of peak heights across the myriad of NMR spectral analysis software, it is recommend to zero fill a lot – 8k to 16k would give the best results. This does not increase the information content of the spectrum or decrease the errors, it simply interpolates. Even if the NMR spectral software performs 3-point quadratic interpolation

Table 5.1: Summary, First Point Scaling and Phase Correction

| Delay     | P1  | FID          | Spectrum                        |
|-----------|-----|--------------|---------------------------------|
| 0 point   | 0   | Scale -c 0.5 |                                 |
| 1/2 point | 180 | Scale -c 1.0 | Folded peaks have opposite sign |
| 1 point   | 360 | Scale -c 1.0 | Use “POLY -auto -ord 0”         |

between the highest points to determine the peak height, the additional free interpolation will make the estimation more accurate.

Additionally, care must be taken to properly scale the first point as this can cause a baseline roll which will affect peak heights. A very useful description comes directly from the [NMRPipe manual](#):

Depending on the delay, the first point of the FID should be adjusted before Fourier Transform. The first point scaling factor is selected by the window function argument `-c`.

If the required first order phase P1 for the given dimension is 0.0, the first point scaling factor should be 0.5. This is because the discrete Fourier transform does the equivalent of counting the point at  $t=0$  twice. If the first point is not scaled properly in this case, ridge-line baseline offsets in the spectrum will result.

In all other cases (P1 is not zero), this scale factor should be 1.0. This is because the first point of the FID no longer corresponds to  $t=0$ , and so it shouldn't be scaled. If the scale factor is not set correctly, it will introduce a baseline distortion which is either zero-order or sinusoidal, depending on what first-order phase is required. When possible, it is best to set up experiments with either exactly 0, 1/2, or 1-point delay. There are several reasons:

- Phase correction values can be determined easily.
- If the delay is not a multiple of 1/2 point, the phase of folded peaks will be distorted.
- The Hilbert transform (HT) is used, sometimes automatically, to reconstruct previously deleted imaginary data for interactive rephasing or inverse processing. But, the HT can only reconstruct imaginary data perfectly if the phase is a multiple of 1/2 point.
- Data with  $P1 = 360$  have the first point  $t=0$  missing (i.e. 1 point delay). Since the first point of the FID corresponds to the sum of points in the corresponding spectrum, this missing first point can be “restored” by adding a constant to the phased spectrum. This can be done conveniently by automated zero-order baseline correction, as shown in table 5.1.

Here is an example NMRPipe script designed for optimal relaxation rate extraction:

```

1  #!/bin/csh
2
3  setenv FILEROOT $1

```

```

4  set PHASE=81.4
5
6  echo "\n# Fourier Transform (nmrPipe fid/*.fid to ft/*.dat)"
7  echo "# t2 phase is set to $PHASE"
8  echo "# t1 phase is set to 0.0\n"
9
10 nmrPipe -in fid/$FILEROOT.fid \
11 | nmrPipe -fn SOL \
12 | nmrPipe -fn GM -g1 15 -g2 20 -c 0.5 \
13 | nmrPipe -fn ZF -size 8192 \
14 | nmrPipe -fn FT -auto \
15 | nmrPipe -fn PS -p0 $PHASE -p1 0.0 -di -verb \
16 | nmrPipe -fn TP \
17 | nmrPipe -fn SP -off 0.5 -end 0.98 -pow 2 -c 0.5 \
18 | nmrPipe -fn ZF -size 8192 \
19 | nmrPipe -fn FT -auto \
20 | nmrPipe -fn PS -p0 0.0 -p1 0.0 -di -verb \
21 | nmrPipe -fn TP \
22 | nmrPipe -fn POLY -auto \
23 | nmrPipe -fn EXT -left -sw \
24 | nmrPipe -out ft/$FILEROOT.dat -ov

```

The script is run by supplying the FILEROOT value as a command line option so if the script is called `nmrpipe.sh` and the `var2pipe` or `bruk2pipe` processed file `R1_ncyc4.fid` is in the `fid` directory, you would run:

```
$ ./nmrpipe.sh R1_ncyc4
```

The `ft` directory must exist for this script to execute. Different experiment specific options may be needed such as:

```

| nmrPipe -fn REV \
| nmrPipe -fn FT -neg \
| nmrPipe -fn PS -rs 2.5 \

```

The script should be changed for different phasing, first point scaling, a polynomial baseline correction added in the direct dimension or removed from the indirect dimension, solvent suppression removed or changed, and the window functions modified for optimal spectral quality. Each system and spectrum is different, so it is recommended that to find the optimal processing that each part of the script be removed and re-added one-by-one between processing and checking of the resultant spectrum. Note that the extraction at the end after the polynomial baseline correction in the indirect dimension is important as the baseline correction often displays a much better performance when the empty part of the spectrum is used in the calculation.

### 5.2.3 Measuring peak intensities

For the measurement of peak intensities, again care must be taken. A read of the paper:

- Viles, J., Duggan, B., Zaborowski, E., Schwarzing, S., Huntley, J., Kroon, G., Dyson, H., and Wright, P. (2001). Potential bias in NMR relaxation data introduced by peak intensity analysis and curve fitting methods. *J. Biomol. NMR*, **21**, 1–9. ([10.1023/A:1011966718826](https://doi.org/10.1023/A:1011966718826))

is highly recommended. Despite the recommendations in the discussion of this paper, a different methodology using peak heights can be used to solve the same problems. This will be discussed in a paper which is currently in preparation from the Gooley group. The steps involved are:

- For the first spectrum in the time series, shift the peak list to the tops of the peaks (for example using “pc” in Sparky on subsets of peaks).
- Copy this 1<sup>st</sup> spectrum list onto all spectra, shifting the peaks to the top as in the previous step.
- When the peak disappears into the noise, leave it at its current position and do not type “pc” or equivalent. This will add weight to the first point in the subsequent step.
- Once all spectra are shifted, calculate an average peak list.
- Copy this average peak list onto fresh copies of all spectra.
- Measure peak heights using this averaged peak list.

This will produce the most accurate peak intensity measurements until better, more robust peak shape integration comes along. This is a special technique which is designed to minimise the white-noise bias talked about in the [Viles et al. \(2001\)](#) paper. As the noise often decreases with the decrease in total spectral power, using the tops of the peaks means that you are actually measuring the real peak height plus positive noise in all cases. This non-constant additional positive noise contribution can result in a double exponential in the measured data. The technique above eliminates this as you then measure close to real peak height with the addition of white noise centred at zero – it is both negative and positive to equal amounts – rather than the peak high with noise contribution strongly biased towards the positive. Where the peaks disappear, you then are measuring the pure baseplane noise. This is fine as these white-noise data points centred at zero will help in the subsequent exponential fit in relax.

If using Sparky then, to be sure that the peak heights are properly updated, for each spectrum type “pa” to select all peaks, “ph” to update all selected peak heights, “lt” to show the spectrum peaks window, make sure “data height” is selected in the options, and then save the peak list.

## 5.3 Relaxation curve-fitting in the prompt/script UI mode

### 5.3.1 Relax-fit script mode – the sample script

The following is a verbatim copy of the contents of the `sample_scripts/relax_fit.py` file. If your copy of the sample script is different than that below, please send an email to the relax-devel mailing list to tell the relax developers that the manual is out of date (see section 3.2.3 on page 30). You will need to first copy this script to a dedicated analysis directory containing peak lists, a PDB file and a file listing unresolved spin systems, and then modify its contents to suit your specific analysis. The script contents are:

```

1  # Script for relaxation curve-fitting.
2
3  # Create the 'rx' data pipe.
4  pipe.create('rx', 'relax_fit')
5
6  # Load the backbone amide 15N spins from a PDB file.
7  structure.read_pdb('Ap4Aase_new_3.pdb')
8  structure.load_spins(spin_id='@N')
9  structure.load_spins(spin_id='@NE1')
10
11 # Spectrum names.
12 names = [
13     'T2_ncyc1_ave',
14     'T2_ncyc1b_ave',
15     'T2_ncyc2_ave',
16     'T2_ncyc4_ave',
17     'T2_ncyc4b_ave',
18     'T2_ncyc6_ave',
19     'T2_ncyc9_ave',
20     'T2_ncyc9b_ave',
21     'T2_ncyc11_ave',
22     'T2_ncyc11b_ave'
23 ]
24
25 # Relaxation times (in seconds).
26 times = [
27     0.0176,
28     0.0176,
29     0.0352,
30     0.0704,
31     0.0704,
32     0.1056,
33     0.1584,
34     0.1584,
35     0.1936,
36     0.1936
37 ]
38
39 # Loop over the spectra.
40 for i in range(len(names)):
41     # Load the peak intensities.
42     spectrum.read_intensities(file=names[i]+'_list', dir=data_path, spectrum_id=names[i],
43                             int_method='height')
44
45     # Set the relaxation times.
46     relax_fit.relax_time(time=times[i], spectrum_id=names[i])
47
48 # Specify the duplicated spectra.
49 spectrum.replicated(spectrum_ids=['T2_ncyc1_ave', 'T2_ncyc1b_ave'])
50 spectrum.replicated(spectrum_ids=['T2_ncyc4_ave', 'T2_ncyc4b_ave'])
51 spectrum.replicated(spectrum_ids=['T2_ncyc9_ave', 'T2_ncyc9b_ave'])
52 spectrum.replicated(spectrum_ids=['T2_ncyc11_ave', 'T2_ncyc11b_ave'])
53
54 # Peak intensity error analysis.
55 spectrum.error_analysis()
56
57 # Deselect unresolved spins.
58 deselect.read(file='unresolved', mol_name_col=1, res_num_col=2, res_name_col=3,
59               spin_num_col=4, spin_name_col=5)
60
61 # Set the relaxation curve type.

```

```

60 relax_fit.select_model('exp')
61
62 # Grid search.
63 grid_search(inc=11)
64
65 # Minimise.
66 minimise('simplex', scaling=False, constraints=False)
67
68 # Monte Carlo simulations.
69 monte_carlo.setup(number=500)
70 monte_carlo.create_data()
71 monte_carlo.initial_values()
72 minimise('simplex', scaling=False, constraints=False)
73 monte_carlo.error_analysis()
74
75 # Save the relaxation rates.
76 value.write(param='rx', file='rx.out', force=True)
77
78 # Save the results.
79 results.write(file='results', force=True)
80
81 # Create Grace plots of the data.
82 grace.write(y_data_type='chi2', file='chi2.agr', force=True)    # Minimised chi-squared
    value.
83 grace.write(y_data_type='i0', file='i0.agr', force=True)        # Initial peak intensity.
84 grace.write(y_data_type='rx', file='rx.agr', force=True)        # Relaxation rate.
85 grace.write(x_data_type='relax_times', y_data_type='intensities', file='intensities.agr',
    force=True)    # Average peak intensities.
86 grace.write(x_data_type='relax_times', y_data_type='intensities', norm=True, file='
    intensities_norm.agr', force=True)    # Average peak intensities (normalised).
87
88 # Display the Grace plots.
89 grace.view(file='chi2.agr')
90 grace.view(file='i0.agr')
91 grace.view(file='rx.agr')
92 grace.view(file='intensities.agr')
93 grace.view(file='intensities_norm.agr')
94
95 # Save the program state.
96 state.save('rx.save', force=True)

```

The next sections will break this script down into its logical components and explain how these parts will be interpreted by relax. To execute this script, please see section 1.2.8 on page 11 for details.

### 5.3.2 Relax-fit script mode – initialisation of the data pipe

The data pipe is simply created by the command

```

3 # Create the 'rx' data pipe.
4 pipe.create('rx', 'relax_fit')

```

This user function will then create a relaxation exponential curve-fitting specific data pipe labelled “rx”. The second argument sets the pipe type to that of the relaxation curve-fitting. Setting the pipe type is important so that the program knows which user functions are compatible with the data pipe, for example in the steady-state NOE analysis

the function `minimise` (see page 332) is meaningless as the NOE values are calculated directly rather than optimised.

### 5.3.3 Relax-fit script mode – setting up the spin systems

The first thing which needs to be completed prior to any spin specific command is to generate the molecule, residue and spin data structures for storing the spin specific data. In the sample script above this is generated from a PDB file, however a plain text file with the sequence information can be used instead (see the `sequence.read` user function on page 435 for more details). In the case of the sample script, the command

```
6 # Load the backbone amide 15N spins from a PDB file.
7 structure.read_pdb(name, 'Ap4Aase_new_3.pdb')
```

will load the PDB file `Ap4Aase_new_3.pdb` into `relax`. Then

```
8 structure.load_spins(spin_id='@N')
9 structure.load_spins(spin_id='@NE1')
```

will generate the molecule, residue, and spin sequence for the current data pipe. In this situation there will be a single spin system per residue generated corresponding to the backbone amide nitrogens as well as  $^{15}\text{N}$  spins set up for the tryptophan indole nitrogens. Although the 3D coordinates have been loaded into the program from the PDB file, this structural information serves no purpose when calculating  $R_1$  and  $R_2$  values.

### 5.3.4 Relax-fit script mode – loading the data

To load the peak intensities into `relax` the `spectrum.read_intensities` and `relax_fit.relax_time` user functions are executed. Important keyword arguments for these user functions are the file name and directory, the spectrum identification string and the relaxation time period of the experiment in seconds. By default the file format will be automatically detected. Currently Sparky, XEasy, NMRView, and generic columnar formatted peak lists are supported. To be able to import any other type of format please send an email to the `relax` development mailing list with the details of the format. Adding support for new formats is trivial. The following series of commands – an expansion of the `for` loop in the sample script – will load peak intensities from six different relaxation periods, four of which have been duplicated, from Sparky peak lists with the peak heights in the 10<sup>th</sup> column.

```
spectrum.read_intensities('T2_ncyc1.list', spectrum_id='1', int_col=10)
relax_fit.relax_time(spectrum_id='1', time=0.0176)
spectrum.read_intensities('T2_ncyc1b.list', spectrum_id='1b', int_col=10)
relax_fit.relax_time(spectrum_id='1b', time=0.0176)
spectrum.read_intensities('T2_ncyc2.list', spectrum_id='2', int_col=10)
relax_fit.relax_time(spectrum_id='2', time=0.0352)
spectrum.read_intensities('T2_ncyc4.list', spectrum_id='4', int_col=10)
relax_fit.relax_time(spectrum_id='4', time=0.0704)
spectrum.read_intensities('T2_ncyc4b.list', spectrum_id='4b', int_col=10)
relax_fit.relax_time(spectrum_id='4b', time=0.0704)
spectrum.read_intensities('T2_ncyc6.list', spectrum_id='6', int_col=10)
relax_fit.relax_time(spectrum_id='6', time=0.1056)
spectrum.read_intensities('T2_ncyc9.list', spectrum_id='9', int_col=10)
```



```

relax_fit.relax_time(spectrum_id='9', time=0.1584)
spectrum.read_intensities('T2_ncyc9b.list', spectrum_id='9b', int_col=10)
relax_fit.relax_time(spectrum_id='9b', time=0.1584)
spectrum.read_intensities('T2_ncyc11.list', spectrum_id='11', int_col=10)
relax_fit.relax_time(spectrum_id='11', time=0.1936)
spectrum.read_intensities('T2_ncyc11b.list', spectrum_id='11b', int_col=10)
relax_fit.relax_time(spectrum_id='11b', time=0.1936)

```

The replicated spectra a set up with the commands

```

47 # Specify the duplicated spectra.
48 spectrum.replicated(spectrum_ids=['T2_ncyc1_ave', 'T2_ncyc1b_ave'])
49 spectrum.replicated(spectrum_ids=['T2_ncyc4_ave', 'T2_ncyc4b_ave'])
50 spectrum.replicated(spectrum_ids=['T2_ncyc9_ave', 'T2_ncyc9b_ave'])
51 spectrum.replicated(spectrum_ids=['T2_ncyc11_ave', 'T2_ncyc11b_ave'])

```

Note that the relaxation time period should be calculated directly from the pulse sequence (as the sum of delays and pulses for the period), as the estimated time may not match the real time. For the Sparky peak lists, by default relax assumes that the intensity value is in the 4<sup>th</sup> column. A typical file looks like:

| Assignment | w1      | w2    | Data Height |
|------------|---------|-------|-------------|
| LEU3N-HN   | 122.454 | 8.397 | 129722      |
| GLY4N-HN   | 111.999 | 8.719 | 422375      |
| SER5N-HN   | 115.085 | 8.176 | 384180      |
| MET6N-HN   | 120.934 | 8.812 | 272100      |
| ASP7N-HN   | 122.394 | 8.750 | 174970      |
| SER8N-HN   | 113.916 | 7.836 | 218762      |
| GLU11N-HN  | 122.194 | 8.604 | 30412       |
| GLY12N-HN  | 110.525 | 9.028 | 90144       |

By supplying the `int_col` argument to the `spectrum.read_intensities` user function, this can be changed. A typical XEasy file will look like:

| No. | Color | w1     | w2      | ass. in w1 | ass. in w2 | Volume    | Vol. Err. | Method | Comment |
|-----|-------|--------|---------|------------|------------|-----------|-----------|--------|---------|
| 2   | 2     | 10.014 | 134.221 | HN 21 LEU  | N 21 LEU   | 7.919e+03 | 0.00e+00  | m      |         |
| 3   | 2     | 10.481 | 132.592 | HE1 79 TRP | NE1 79 TRP | 1.532e+04 | 0.00e+00  | m      |         |
| 17  | 2     | 9.882  | 129.041 | HN 110 PHE | N 110 PHE  | 9.962e+03 | 0.00e+00  | m      |         |
| 18  | 2     | 8.757  | 128.278 | HN 52 ASP  | N 52 ASP   | 2.041e+04 | 0.00e+00  | m      |         |
| 19  | 2     | 10.086 | 128.297 | HN 69 SER  | N 69 SER   | 9.305e+03 | 0.00e+00  | m      |         |
| 20  | 3     | 9.111  | 127.707 | HN 15 ARG  | N 15 ARG   | 9.714e+03 | 0.00e+00  | m      |         |

where the peak height is in the **Volume** column. And for an NMRView file:

```

label dataset sw sf
H1 N15
cNTnC_noe0.nv
2505.63354492 1369.33557129
499.875 50.658000946
H1.L H1.P H1.W H1.B H1.E H1.J H1.U N15.L N15.P N15.W N15.B N15.E N15.J N15.U vol int stat comment flag0
0 {70.HN} 10.75274 0.02954 0.05379 ++ 0.0 {} {70.N} 116.37241 0.23155 0.35387 ++ 0.0 {} -6.88333129883 -0.1694 0 {} 0
1 {72.HN} 9.67752 0.03308 0.05448 ++ 0.0 {} {72.N} 126.41302 0.27417 0.37217 ++ 0.0 {} -5.49038267136 -0.1142 0 {} 0
2 {} 8.4532 0.02331 0.05439 ++ 0.0 {} {} 122.20137 0.38205 0.33221 ++ 0.0 {} -2.58034267191 -0.1320 0 {} 0

```

### 5.3.5 Relax-fit script mode – the rest of the setup

Once all the peak intensity data has been loaded a few calculations are required prior to optimisation. Firstly the peak intensities for individual spins needs to be averaged across replicated spectra. The peak intensity errors also have to be calculated using the standard deviation formula. These two operations are executed by the user function

```
53 # Peak intensity error analysis.
54 spectrum.error_analysis()
```

Any spins which cannot be resolved due to peak overlap were included in a file called `unresolved`. This file can consist of optional columns of the molecule name, the residue name and number, and the spin name and number. The matching spins are excluded from the analysis by the user function

```
56 # Deselect unresolved spins.
57 deselect.read(file='unresolved', mol_name_col=1, res_num_col=2, res_name_col=3,
    spin_num_col=4, spin_name_col=5)
```

Finally the experiment type is specified by the command

```
59 # Set the relaxation curve type.
60 relax_fit.select_model('exp')
```

The argument “`exp`” sets the relaxation curve to a two parameter  $\{R_x, I_0\}$  exponential which decays to zero. The formula of this function is

$$I(t) = I_0 e^{-R_x t}, \quad (5.1)$$

where  $I(t)$  is the peak intensity at any time point  $t$ ,  $I_0$  is the initial intensity, and  $R_x$  is the relaxation rate (either the  $R_1$  or  $R_2$ ). Changing the user function argument to “`inv`” will select the inversion recovery experiment. This curve consists of three parameters  $\{R_1, I_0, I_\infty\}$  and does not decay to zero. The formula is

$$I(t) = I_\infty - I_0 e^{-R_1 t}. \quad (5.2)$$

### 5.3.6 Relax-fit script mode – optimisation of exponential curves

Now that everything has been setup minimisation can be used to optimise the parameter values. Firstly a grid search is applied to find a rough starting position for the subsequent optimisation algorithm. Eleven increments per dimension of the model (in this case the two dimensions  $\{R_x, I_0\}$ ) is sufficient. The user function for executing the grid search is

```
62 # Grid search.
63 grid_search(inc=11)
```

The next step is to select one of the minimisation algorithms to optimise the model parameters. Currently for relaxation curve-fitting only simplex minimisation is supported. This is because the relaxation curve-fitting C module is incomplete only implementing the chi-squared function. The chi-squared gradient (the vector of first partial derivatives) and chi-squared Hessian (the matrix of second partial derivatives) are not yet implemented in the C modules and hence optimisation algorithms which only employ function calls are

supported. Simplex minimisation is the only technique in relax which fits this criterion. In addition constraints cannot be used as the constraint algorithm is dependent on gradient calls. Therefore the minimisation command for relaxation curve-fitting is forced to be

```
65 # Minimise.
66 minimise('simplex', constraints=False)
```

### 5.3.7 Relax-fit script mode – error analysis

Only one technique adequately estimates parameter errors when the parameter values were found by optimisation – Monte Carlo simulations. In relax this can be implemented by using a series of functions from the `monte_carlo` user function class. Firstly the number of simulations needs to be set

```
68 # Monte Carlo simulations.
69 monte_carlo.setup(number=500)
```

For each simulation, randomised relaxation curves will be fit using exactly the same methodology as the original exponential curves. These randomised curves are created by back calculation from the fitted model parameter values and then each point on the curve randomised using the error values set earlier in the script

```
70 monte_carlo.create_data()
```

As a grid search for each simulation would be too computationally expensive, the starting point for optimisation for each simulation can be set to the position of the optimised parameter values of the model

```
71 monte_carlo.initial_values()
```

Then exactly the same optimisation as was used for the model can be performed

```
72 minimise('simplex', constraints=False)
```

The parameter errors are then determined as the standard deviation of the optimised parameter values of the simulations

```
73 monte_carlo.error_analysis()
```

### 5.3.8 Relax-fit script mode – finishing off

To finish off, the script first saves the relaxation rates together with their errors in a simple text file

```
75 # Save the relaxation rates.
76 value.write(param='rx', file='rx.out', force=True)
```

Grace plots are created and viewed

```
81 # Create Grace plots of the data.
82 grace.write(y_data_type='chi2', file='chi2.agr', force=True) # Minimised chi-squared
    value.
83 grace.write(y_data_type='i0', file='i0.agr', force=True) # Initial peak intensity.
```

```
84 grace.write(y_data_type='rx', file='rx.agr', force=True)    # Relaxation rate.
85 grace.write(x_data_type='relax_times', y_data_type='intensities', file='intensities.agr',
86             force=True)    # Average peak intensities.
87 grace.write(x_data_type='relax_times', y_data_type='intensities', norm=True, file='
    intensities_norm.agr', force=True)    # Average peak intensities (normalised).
```

and viewed

```
88 # Display the Grace plots.
89 grace.view(file='chi2.agr')
90 grace.view(file='i0.agr')
91 grace.view(file='rx.agr')
92 grace.view(file='intensities.agr')
93 grace.view(file='intensities_norm.agr')
```

and finally the program state is saved for future reference

```
95 # Save the program state.
96 state.save(file='rx.save', force=True)
```

## 5.4 The relaxation curve-fitting auto-analysis in the GUI

The  $R_1$  and  $R_2$  relaxation rates can be calculated using the relax GUI (see Figures 1.6 and 1.7). These auto-analyses can be selected using the analysis selection wizard (Figure 1.4 on page 12). Just as with the steady-state NOE in the next chapter, these auto-analyses are very similar in spirit to the sample script described in this chapter, though the Grace 2D visualisation is more advanced. If you have read this chapter, the usage of these analyses should be self explanatory.

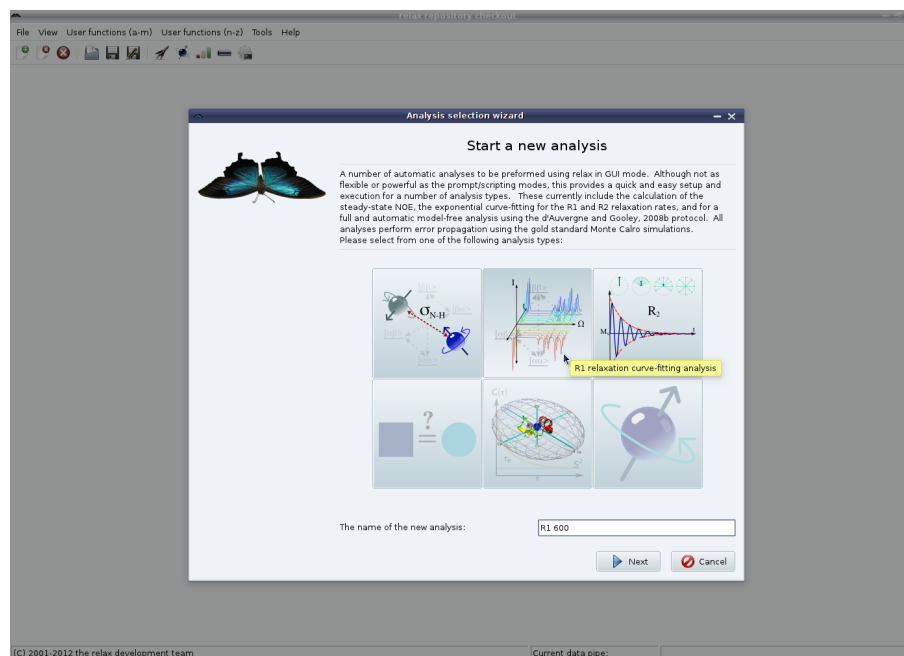
As in the script/prompt UI section above, the example of protein  $^{15}\text{N}$   $R_1$  relaxation analysis will be performed in the following sections. To keep track of all the messages relax produces for future reference, you can run the relax GUI with the following command line arguments:

```
$ relax --log log --gui
```

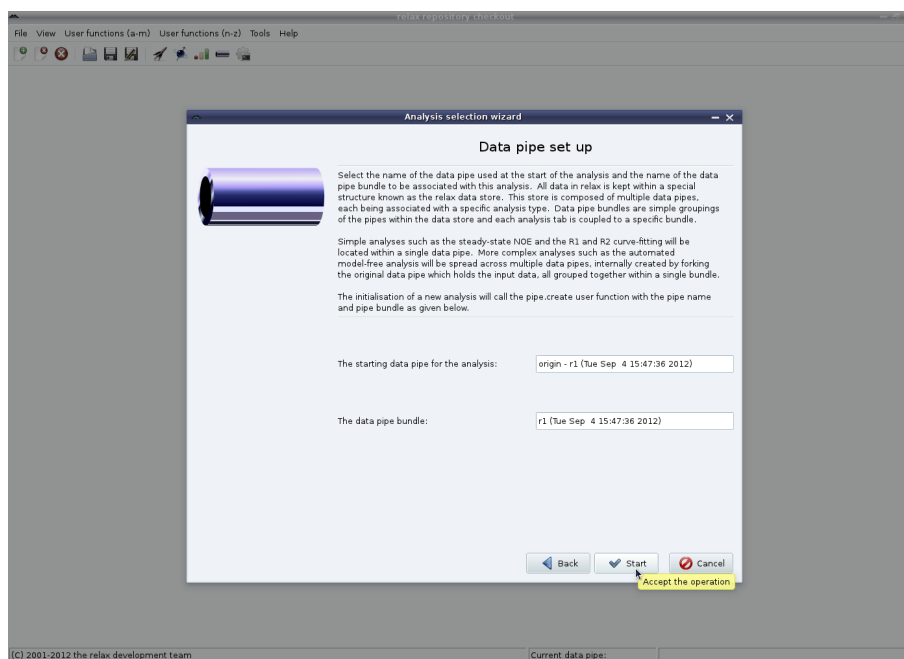
The messages will then appear both in the relax controller window (see Figure 1.9 on page 19) and in the log file.

### 5.4.1 Relax-fit GUI mode – initialisation of the data pipe

To begin the analysis, launch the analysis selection wizard (see Figure 1.4 on page 12). Select either the  $R_1$  or  $R_2$  analyses, and change the name of the analysis if you plan on running multiple analyses from different field strengths in one relax instance.

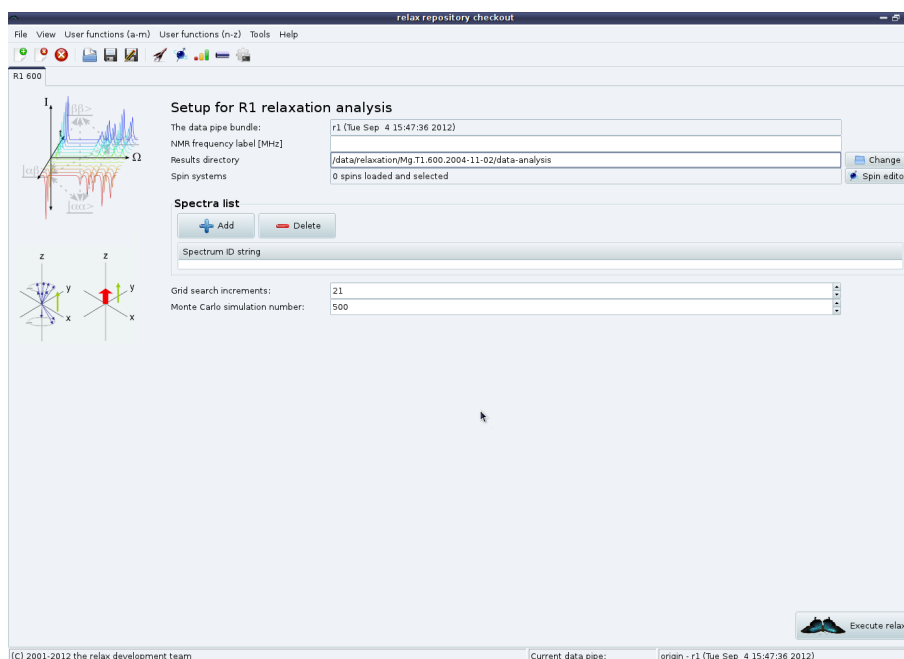


Then click on the “Next” button. On the second page click on “Start” to commence the analysis – this second part of the wizard does not need to be changed. For the  $R_1$  and  $R_2$  analyses in the GUI, a data pipe bundle containing only a single data pipe for that analysis will be created. This data pipe bundle can be safely ignored.



### 5.4.2 Relax-fit GUI mode – general setup

You will now be presented with a blank analysis tab:



Here there are two things unique to the GUI which need to be preformed:

**NMR frequency label:** First set the NMR frequency label. This is only used for the name of the output file. For example if you set the label to “1200”, the file `r1.1200.out` will be created at the end of the analysis.

**Results directory:** All of the automatically created results and Grace files will be placed into this directory. The “Results directory” can now be changed.

### 5.4.3 Relax-fit GUI mode – setting up the spin systems

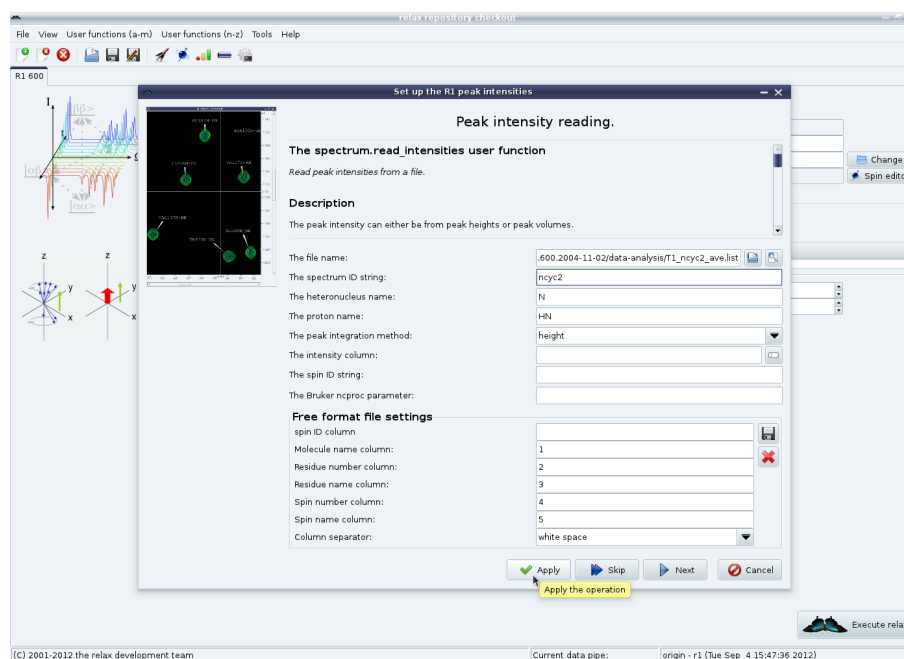
As the relaxation data is at the level of the spins, the molecule, residue and spin data structures need to be set up. In the  $R_1$  and  $R_2$  GUI analysis tabs, there is a special “Spin systems” GUI element designed for this. This will initially say “0 spins loaded and selected”. Click on the “Spin editor” button to launch the spin viewer window. The steps for setting up the spin containers using PDB files are described in section 4.5.2 on page 40 or for sequence files in section 4.5.3 on page 43.

### 5.4.4 Relax-fit GUI mode – unresolved spins

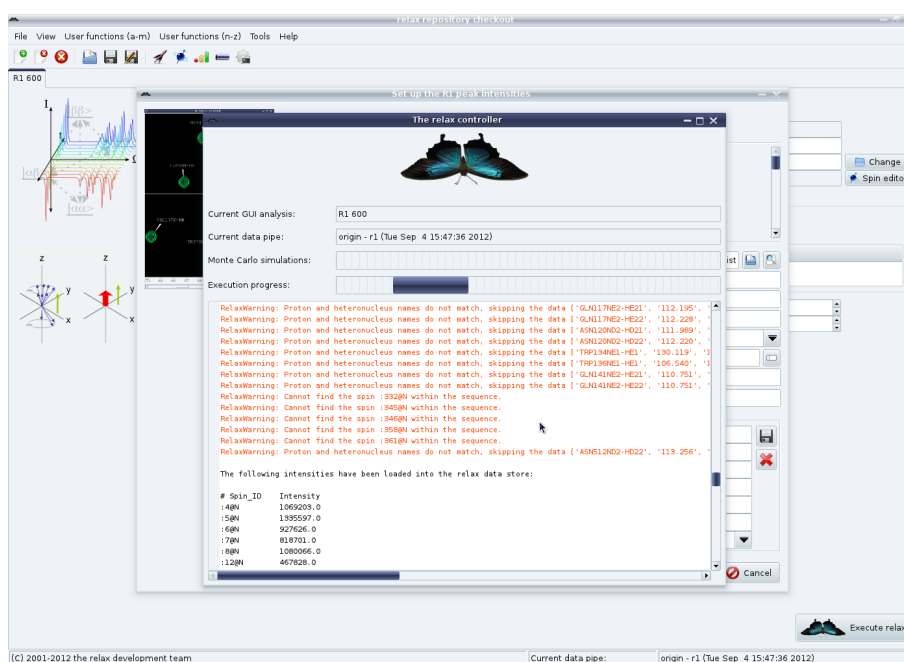
As in the prompt/script UI section 5.3.5, the spins can be deselected at this point using the same `unresolved` file. This is described in detail in section 4.5.5 on page 44.

### 5.4.5 Relax-fit GUI mode – loading the data

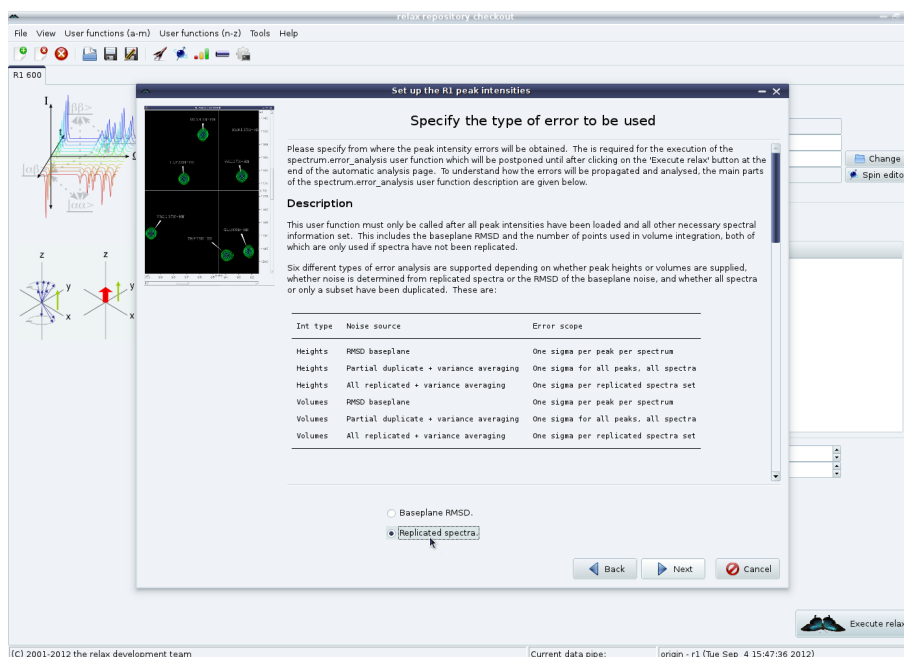
At this stage, the peak intensity data needs to be loaded. In both the  $R_1$  and  $R_2$  analysis tabs is a “Spectra list” GUI element. Click on the “Add” button to launch the peak intensity loading wizard:



In this example, a Sparky peak list containing the peak heights determined from the averaged chemical shift positions for all spectra will be loaded. Set the spectrum ID string to a unique value. Click on “Next”. This will most likely cause a `RelaxWarning` message to appear for all peak list elements which do not correspond to any spins loaded into the relax data store:

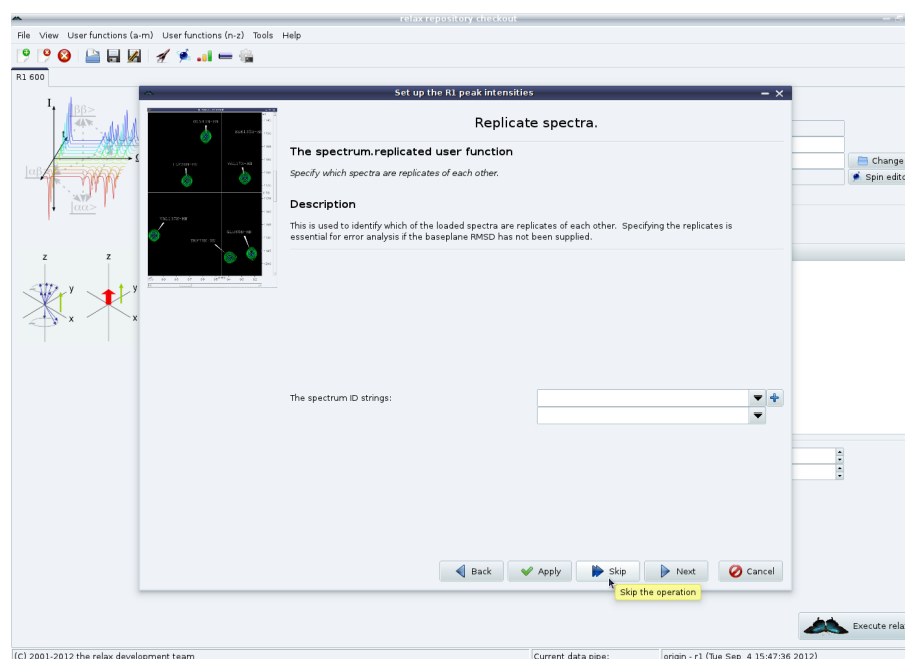


These messages must be carefully checked to be sure that the correct data has been loaded. A `RelaxError` might be thrown if the peak list is corrupted or if the dimension has been incorrectly given. In this case check the message, go “Back”, fix the problem, and click on “Next” again. Then click on “Next”. You should now see the error type page:

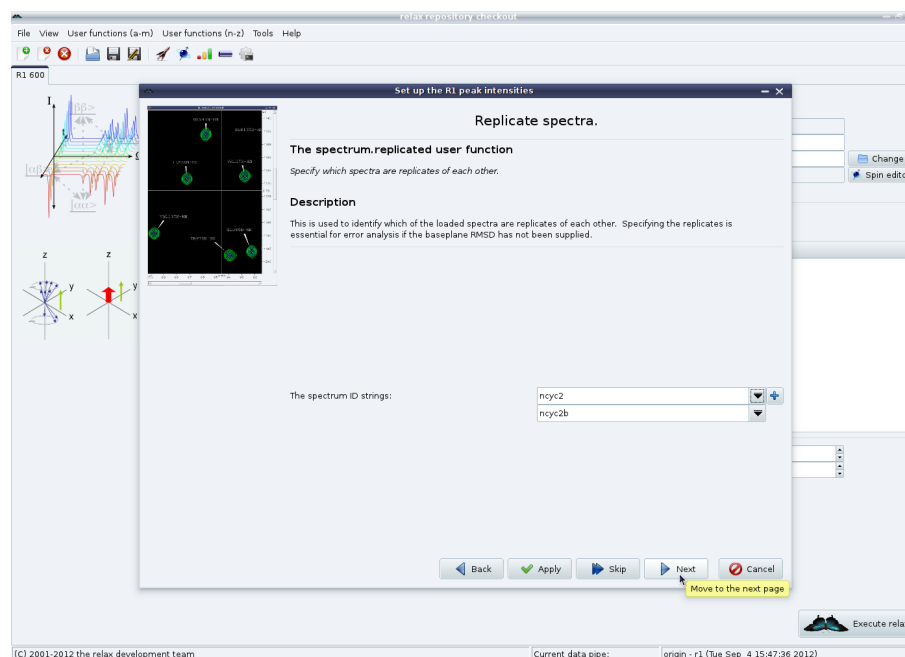


The description for this wizard page should be very carefully read – it will tell you about all of the error analysis options available and how these are implemented in relax. For the protein relaxation example, replicated spectra have been collected. Therefore the option “Replicated spectra” will be chosen. The “Baseplane RMSD” option is documented in the NOE chapter. After clicking on “Next” you will see:

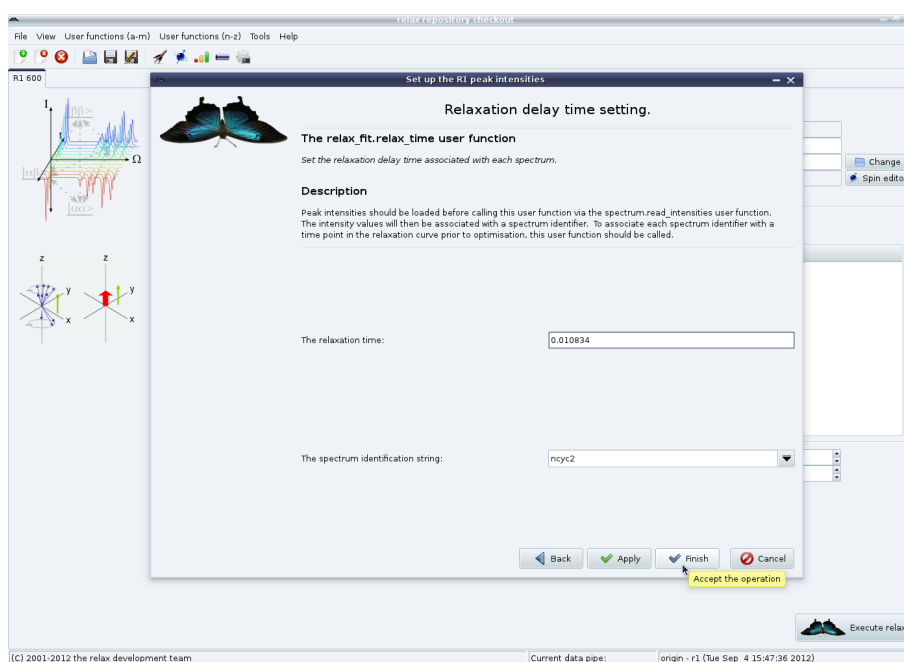




For the first of the duplicate spectra, or any spectrum without a duplicate, you can click on the “Skip” button. If this is the second spectrum you have loaded from a duplicated set, select the two replicated spectra and then click on “Next”:

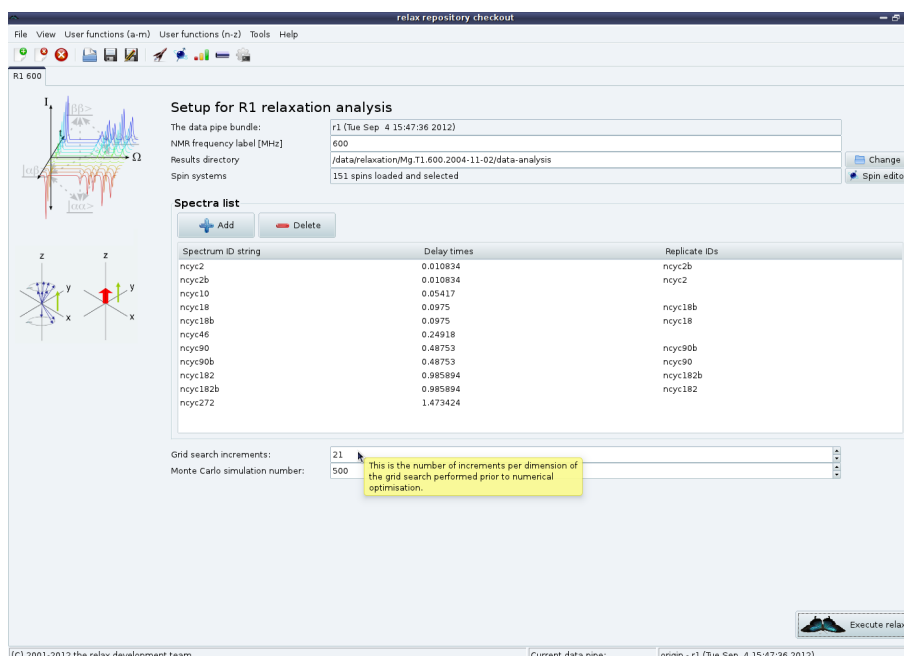


Finally set the relaxation time period for this experiment in seconds:



All delays and pulse lengths in the pulse sequence should be carefully checked to be sure that the time is exactly what you would expect – the estimated time may not match the real time. To set the time and close the wizard, click on the “Finish” button.

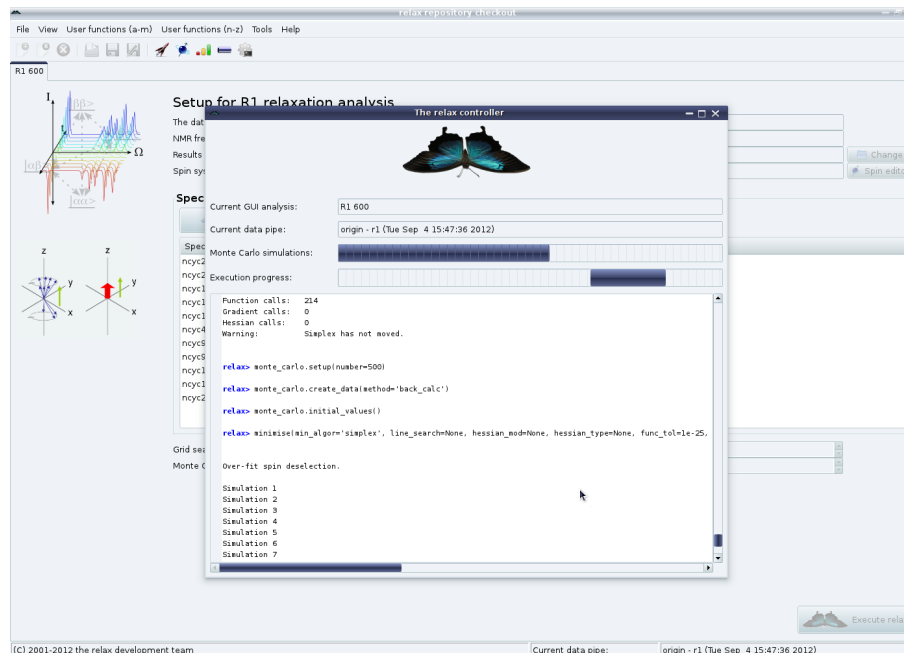
This procedure should be repeated for every experiment you have collected (you could, as an alternative, load all at the same time using the “Apply” button at each stage). In the end you should see something such as:



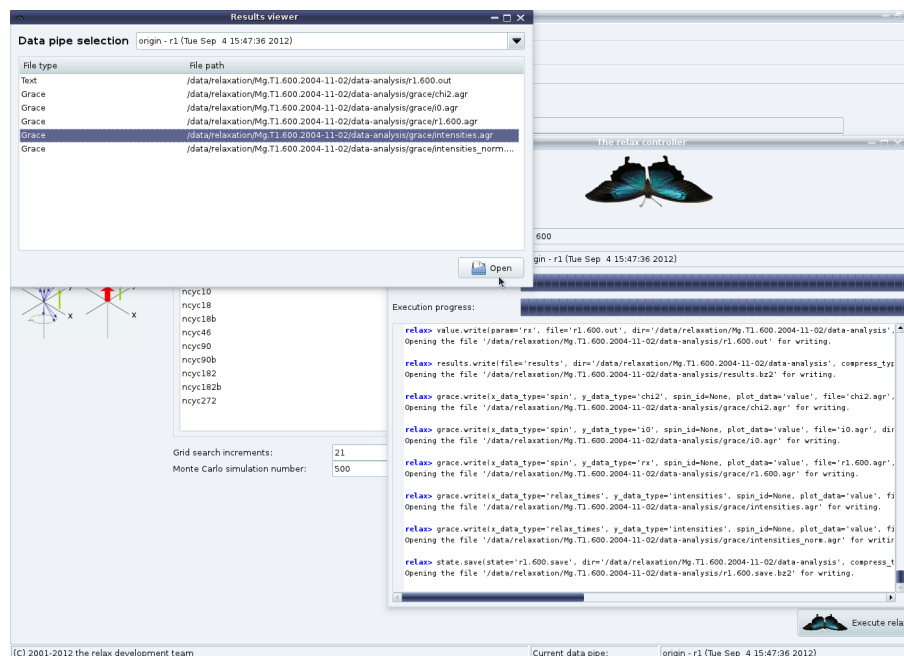
### 5.4.6 Relax-fit GUI mode – optimisation and error analysis

Back in the main  $R_1$  analysis tab, the grid search increments and number of Monte Carlo simulations can be changed. The default values of 21 grid search increments and 500 MC

simulations are optimal – lower values are not recommended. To perform the optimisation and error analysis, click on the “Execute relax” button. The relax controller will open to show you the progress of the optimisation and simulations:



Once finished, the “Results viewer” window will also appear:



This window can be used to open the text files in the default text editor for your operating system or the 2D Grace plots in *xmgrace* if available on your system.

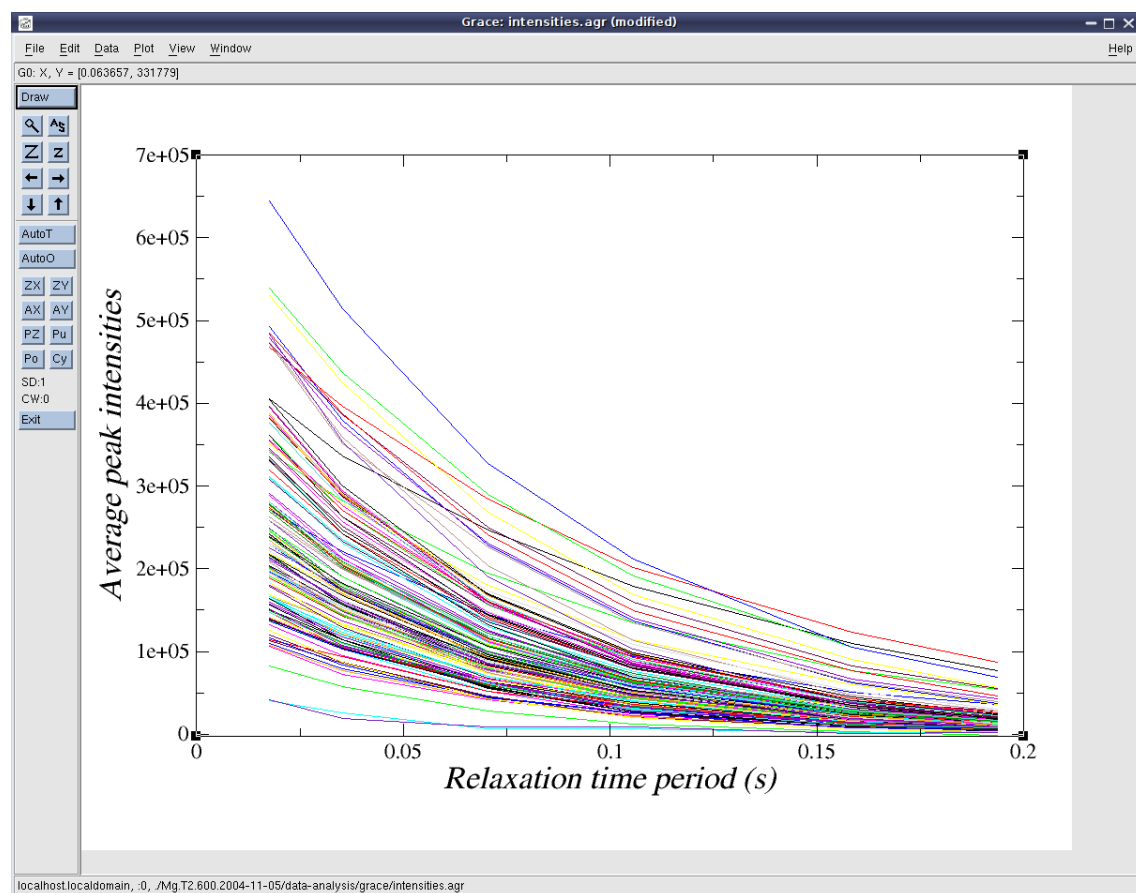


Figure 5.1: Screenshot of the 2D peak intensity plots for the exponential relaxation curves in Xmgrace.

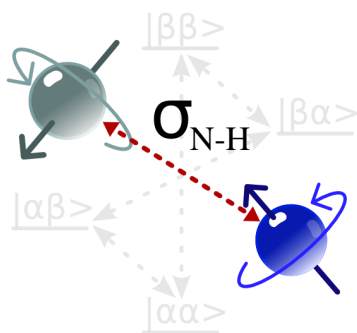
## 5.5 Final checks of the curve-fitting

To be sure that the data has been properly collected and that no instrumentation or pulse sequence timing errors have occurred, it is essential to carefully check the `intensities.agr` and `intensities_norm.agr` 2D Grace files. These are plots of the decay curves for each spin system analysed, and any non-exponential behaviour should be clearly visible (see Figure 5.1). If Xmgrace or a compatible program is not available for your operating system, the Grace files contain text representations of the curves at the end which can be opened, edited and visualised in any other 2D graphing software package.

Note that errors resulting in systematic bias in the data – for example if temperature control (single-scan interleaving or temperature compensation blocks) or per-experiment/per-spectrometer temperature calibration on MeOH or ethylene glycol have not been performed – will not be detected by looking at the decay curves. See section 5.2.1 or the `relax_data.temp_calibration` user function documentation on page 407 and the `relax_data.temp_control` user function documentation on page 408 for more details.

## Chapter 6

# Calculating the NOE



### 6.1 Introduction to the steady-state NOE

The calculation of NOE values is a straight forward and quick procedure which involves two components – the calculation of the value itself and the calculation of the errors. To understand the steps involved the execution of a sample NOE calculation script will be followed in detail. Then the same operations will be presented for the perspective of the graphical user interface.

### 6.2 From spectra to peak intensities for the NOE

For a set of recommendations for how to obtain the best quality relaxation rates, please see section 5.2 on page 49. In summary the following are important – temperature control (though the standard steady-state NOE single FID interleaved pulse sequences are fine), per-experiment temperature calibration, spectral processing with massive zero-filling and no baseplane rolling, and using an averaged peak list for determining the peak heights.

## 6.3 Calculation of the NOE in the prompt/script UI mode

### 6.3.1 NOE script mode – the sample script

This sample script can be found in the `sample_scripts` directory and will be used as the template for the next sections describing how to use relax.

```

1  # Script for calculating NOEs.
2
3  # Create the data pipe.
4  pipe.create('NOE', 'noe')
5
6  # Load the sequence from a PDB file.
7  structure.read_pdb('Ap4Aase_new_3.pdb')
8  structure.load_spins(spin_id='@N')
9  structure.load_spins(spin_id='@NE1')
10
11 # Load the reference spectrum and saturated spectrum peak intensities.
12 spectrum.read_intensities(file='ref.list', spectrum_id='ref_ave')
13 spectrum.read_intensities(file='sat.list', spectrum_id='sat_ave')
14
15 # Set the spectrum types.
16 noe.spectrum_type('ref', 'ref_ave')
17 noe.spectrum_type('sat', 'sat_ave')
18
19 # Set the errors.
20 spectrum.baseplane_rmsd(error=3600, spectrum_id='ref_ave')
21 spectrum.baseplane_rmsd(error=3000, spectrum_id='sat_ave')
22
23 # Individual residue errors.
24 spectrum.baseplane_rmsd(error=122000, spectrum_type='ref', res_num=114)
25 spectrum.baseplane_rmsd(error=8500, spectrum_type='sat', res_num=114)
26
27 # Peak intensity error analysis.
28 spectrum.error_analysis()
29
30 # Deselect unresolved spins.
31 deselect.read(file='unresolved', res_num_col=1, spin_name_col=2)
32
33 # Calculate the NOEs.
34 calc()
35
36 # Save the NOEs.
37 value.write(param='noe', file='noe.out', force=True)
38
39 # Create Grace files.
40 grace.write(y_data_type='ref', file='ref.agr', force=True)
41 grace.write(y_data_type='sat', file='sat.agr', force=True)
42 grace.write(y_data_type='noe', file='noe.agr', force=True)
43
44 # View the Grace files.
45 grace.view(file='ref.agr')
46 grace.view(file='sat.agr')
47 grace.view(file='noe.agr')
48
49 # Write the results.
50 results.write(file='results', dir=None, force=True)
51
52 # Save the program state.
```

```
53 state.save('save', force=True)
```

### 6.3.2 NOE script mode – initialisation of the data pipe

The start of this sample script is very similar to that of the relaxation curve-fitting calculation on page 55. The command

```
3 # Create the data pipe.
4 pipe.create('NOE', 'noe')
```

initialises the data pipe labelled “NOE”. The data pipe type is set to the NOE calculation by the argument “noe”.

### 6.3.3 NOE script mode – setting up the spin systems

The backbone amide nitrogen sequence is extracted from a PDB file using the same commands as the relaxation curve-fitting script (Chapter 5). The command

```
6 # Load the sequence from a PDB file.
7 structure.read_pdb('Ap4Aase_new_3.pdb')
```

will load the PDB file `Ap4Aase_new_3.pdb` into `relax`. Then the following commands will generate both the backbone amide and tryptophan indole  $^{15}\text{N}$  spins

```
8 structure.load_spins(spin_id='@N')
9 structure.load_spins(spin_id='@NE1')
```

### 6.3.4 NOE script mode – loading the data

The commands

```
11 # Load the reference spectrum and saturated spectrum peak intensities.
12 spectrum.read_intensities(file='ref.list', spectrum_id='ref_ave')
13 spectrum.read_intensities(file='sat.list', spectrum_id='sat_ave')
```

will load the peak heights of the reference and saturated NOE experiments (although the volume could be used instead). `relax` will automatically determine the format of the peak list. Currently only Sparky, XEasy, NMRView and a generic columnar formatted text file are supported.

In this example, `relax` will determine from the file contents that these are Sparky peak lists (saved after typing “lt”). The first column of the file should be the Sparky assignment string and it is assumed that the 4<sup>th</sup> column contains either the peak height or peak volume (though this can be in any column – the `int_col` argument is used to specify where the data is). Without specifying the `int_method` argument, peak heights will be assumed. See page 441 for a description of all the `spectrum.read_intensities` user function arguments. In this example, the peak list looks like:

| Assignment | w1      | w2    | Data Height |
|------------|---------|-------|-------------|
| LEU3N-HN   | 122.454 | 8.397 | 129722      |
| GLY4N-HN   | 111.999 | 8.719 | 422375      |
| SER5N-HN   | 115.085 | 8.176 | 384180      |
| MET6N-HN   | 120.934 | 8.812 | 272100      |
| ASP7N-HN   | 122.394 | 8.750 | 174970      |
| SER8N-HN   | 113.916 | 7.836 | 218762      |
| GLU11N-HN  | 122.194 | 8.604 | 30412       |
| GLY12N-HN  | 110.525 | 9.028 | 90144       |

For subsequent usage of the data in relax, assuming a 3D structure exists, it is currently advisable to use the same residue and atom numbering as found in the PDB file.

If you have any other format you would like read by relax please send an email to the relax development mailing list detailing the software used, the format of the file (specifically where the residue number and peak intensity are located), and possibly attaching an example of the file itself.

### 6.3.5 NOE script mode – setting the errors

In this example the errors were measured from the base plain noise. The Sparky RMSD function was used to estimate the maximal noise levels across the spectrum in regions containing no peaks. For the reference spectrum the RMSD was approximately 3600 whereas in the saturated spectrum the RMSD was 3000. These errors are set by the commands

```

21 # Set the errors.
22 spectrum.baseplane_rmsd(error=3600, spectrum_id='ref_ave')
23 spectrum.baseplane_rmsd(error=3000, spectrum_id='sat_ave')
```

For the residue G114, the noise levels are significantly increased compared to the rest of the protein as the peak is located close to the water signal. The higher errors for this residue are specified by the commands

```

25 # Individual residue errors.
26 spectrum.baseplane_rmsd(error=122000, spectrum_type='ref', res_num=114)
27 spectrum.baseplane_rmsd(error=8500, spectrum_type='sat', res_num=114)
```

There are many other ways of setting the errors, for example via spectrum duplication, triplication, etc. See the documentation for the `spectrum.error_analysis` user function on page 439 for all possible options. This user function needs to be executed at this stage to correctly set up the errors for all spin systems:

```

29 # Peak intensity error analysis.
30 spectrum.error_analysis()
```

### 6.3.6 NOE script mode – unresolved spins

As the peaks of certain spins overlap to such an extent that the heights or volumes cannot be resolved, a simple text file was created called “unresolved” in which each line consists of the residue number followed by the atom name. By using the command



```

32 # Deselect unresolved spins.
33 deselect.read(name, file='unresolved', res_num_col=1, spin_name_col=2)

```

all spins in the file “unresolved” are excluded from the analysis.

### 6.3.7 NOE script mode – the NOE calculation

At this point the NOE can be calculated. The user function

```

35 # Calculate the NOEs.
36 calc()

```

will calculate both the NOE and the errors. The NOE value will be calculated using the formula

$$NOE = \frac{I_{sat}}{I_{ref}}, \quad (6.1)$$

where  $I_{sat}$  is the intensity of the peak in the saturated spectrum and  $I_{ref}$  is that of the reference spectrum. The error is calculated by

$$\sigma_{NOE} = \sqrt{\frac{(\sigma_{sat} \cdot I_{ref})^2 + (\sigma_{ref} \cdot I_{sat})^2}{I_{ref}^2}}, \quad (6.2)$$

where  $\sigma_{sat}$  and  $\sigma_{ref}$  are the peak intensity errors in the saturated and reference spectra respectively. To create a file of the NOEs the command

```

38 # Save the NOEs.
39 value.write(param='noe', file='noe.out', force=True)

```

will create a file called `noe.out` with the NOE values and errors. The force flag will cause any file with the same name to be overwritten. An example of the format of `noe.out` is

| #                  | mol_name | res_num | res_name | spin_num | spin_name             | value                | error |
|--------------------|----------|---------|----------|----------|-----------------------|----------------------|-------|
| Ap4Aase_new_3_mol1 | 1        | GLY     | 1        | N        | None                  | None                 |       |
| Ap4Aase_new_3_mol1 | 2        | PRO     | 11       | N        | None                  | None                 |       |
| Ap4Aase_new_3_mol1 | 3        | LEU     | 28       | N        | None                  | None                 |       |
| Ap4Aase_new_3_mol1 | 4        | GLY     | 51       | N        | -0.038921946984531344 | 0.019031770246176943 |       |
| Ap4Aase_new_3_mol1 | 5        | SER     | 59       | N        | -0.312404225679127    | 0.018596937298386886 |       |
| Ap4Aase_new_3_mol1 | 6        | MET     | 71       | N        | -0.42850831873249773  | 0.02525856323041225  |       |
| Ap4Aase_new_3_mol1 | 7        | ASP     | 91       | N        | -0.5305492810313481   | 0.027990623144176396 |       |
| Ap4Aase_new_3_mol1 | 8        | SER     | 104      | N        | -0.5652842977581912   | 0.021706121467731133 |       |
| Ap4Aase_new_3_mol1 | 9        | PRO     | 116      | N        | None                  | None                 |       |
| Ap4Aase_new_3_mol1 | 10       | PRO     | 133      | N        | None                  | None                 |       |
| Ap4Aase_new_3_mol1 | 11       | GLU     | 150      | N        | None                  | None                 |       |
| Ap4Aase_new_3_mol1 | 12       | GLY     | 167      | N        | -0.7036626368123614   | 0.04681370194503697  |       |
| Ap4Aase_new_3_mol1 | 13       | TYR     | 175      | N        | -0.747464566367261    | 0.03594640051809186  |       |
| Ap4Aase_new_3_mol1 | 14       | ARG     | 200      | N        | -0.7524129557634996   | 0.04957018638401278  |       |

### 6.3.8 NOE script mode – viewing the results

Any two dimensional data set can be plotted in relax in conjunction with the program [Grace](#). The program is also known as Xmgrace and was previously known as ACE/gr or Xmgr. The highly flexible relax user function `grace.write` is capable of producing 2D plots of any x-y data sets. The three commands

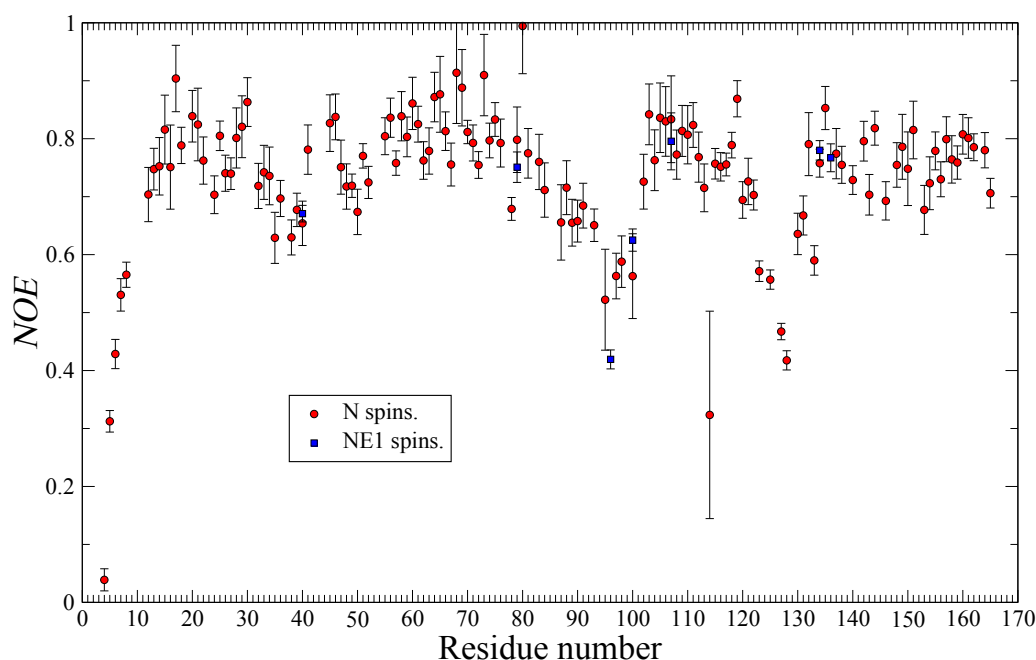


Figure 6.1: A Grace plot of the NOE value and error against the residue number. This is an example of the output of the user function `grace.write`.

```

41 # Create Grace files.
42 grace.write(y_data_type='ref', file='ref.agr', force=True)
43 grace.write(y_data_type='sat', file='sat.agr', force=True)
44 grace.write(y_data_type='noe', file='noe.agr', force=True)

```

will create three separate plots of the peak intensity of the reference and saturated spectra as well as the NOE. The x-axis in all three defaults to the residue number. As the x and y-axes can be any parameter the command

```
grace.write(x_data_type='ref', y_data_type='sat', file='ref_vs_sat.agr', force=True)
```

would create a plot of the reference verses the saturated intensity with one point per residue. Returning to the sample script three Grace data files are created `ref.agr`, `sat.agr`, and `noe.agr` and placed in the default directory `./grace`. These can be visualised by opening the file within Grace. However `relax` will do that for you with the commands

```

46 # View the Grace files.
47 grace.view(file='ref.agr')
48 grace.view(file='sat.agr')
49 grace.view(file='noe.agr')

```

An example of the output after modifying the axes is shown in figure 6.1.

## 6.4 The NOE auto-analysis in the GUI

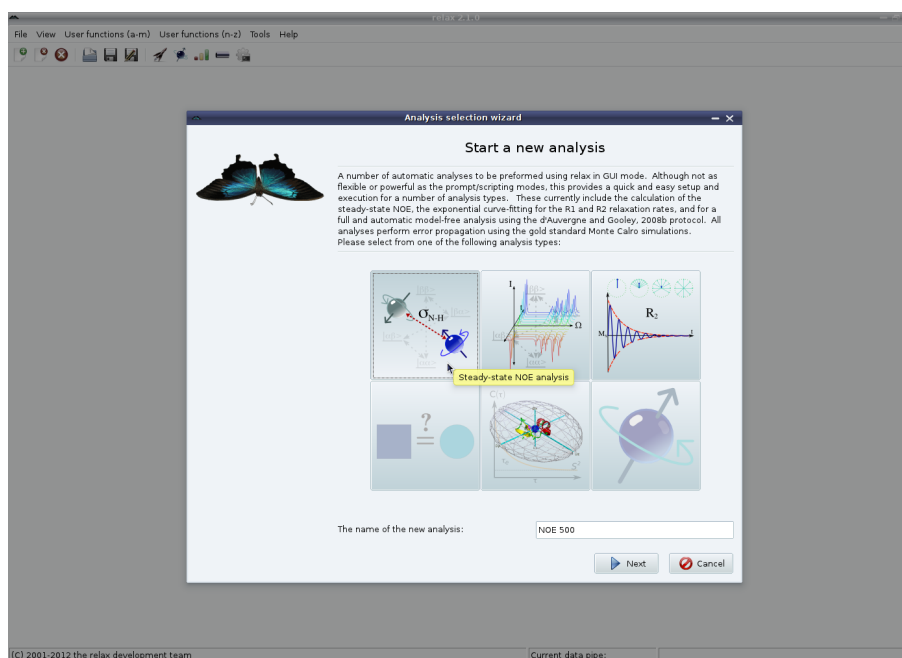
The relax graphical user interface provides access to an automated steady-state NOE analysis. This auto-analysis operates in the same way as the sample script described earlier in this chapter. In this example, relax will be launched with:

```
$ relax --log log --gui
```

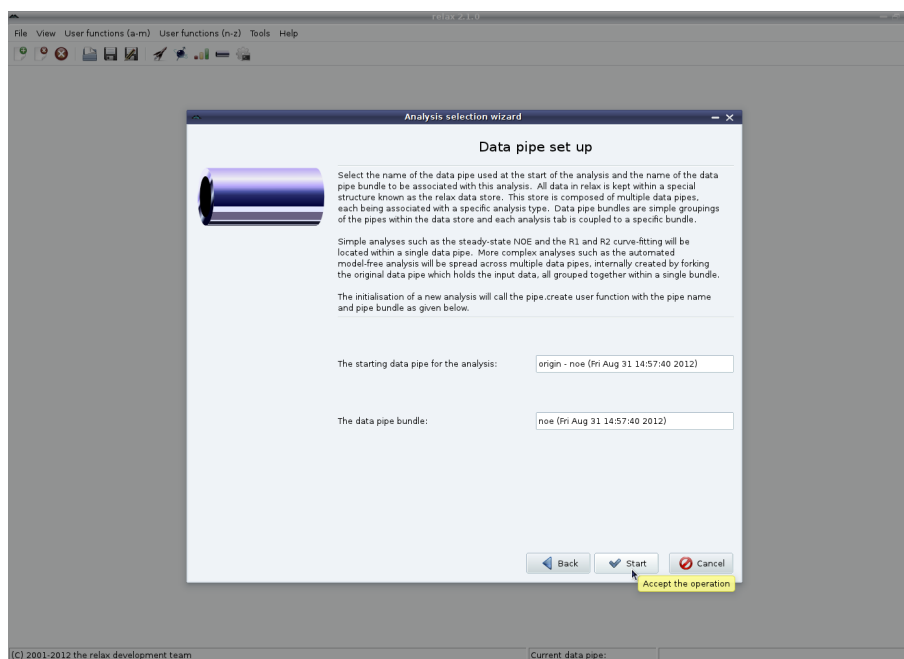
The `--log` command line argument will cause all of relax's text printouts to be placed into the `log` file which can serve as a record for later reference (the `--tee` command line argument could be used as well).

### 6.4.1 NOE GUI mode – initialisation of the data pipe

First launch the analysis selection wizard (see Figure 1.4 on page 12). Select the NOE analysis and, if you plan on running steady-state NOE analyses from multiple fields in one relax instance, change the name of the analysis:

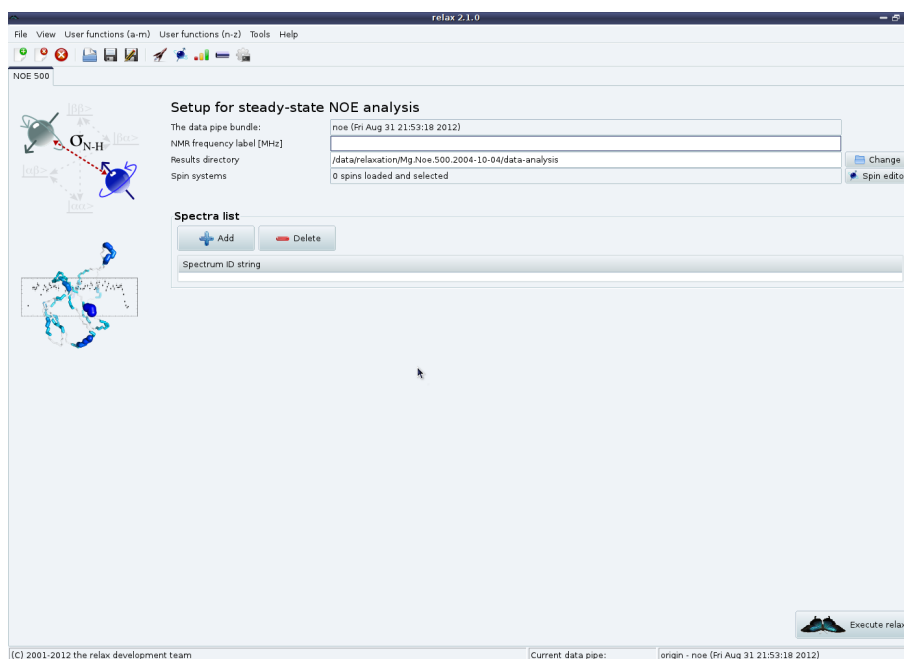


The second part of the wizard need not be modified, just click on “Start” to begin. This will create a dedicated data pipe for the analysis. A data pipe bundle will also be created, but for the steady-state NOE will only contain a single data throughout the analysis.



### 6.4.2 NOE GUI mode – general setup

You should then see the blank analysis tab:



The first thing to do now is to set the NMR frequency label. This is only used for the name of the NOE output file. For example if you set the label to “500”, the file `noe.500.out` will be created at the end of the analysis.

You can also choose to change the “Results directory” where all of the automatically created results files will be placed. These two steps are unique to the GUI mode.

### 6.4.3 NOE GUI mode – setting up the spin systems

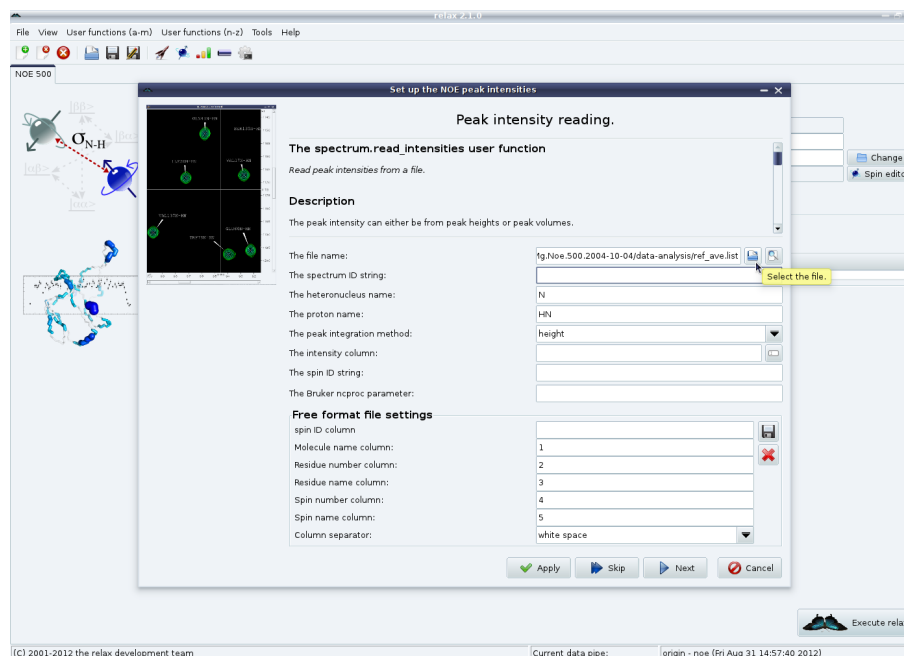
Just as in the prompt and scripting UI modes, the molecule, residue and spin data structures need to be set up prior to the loading of any spin specific data. The “Spin systems” GUI element is used for this purpose. Before any spin systems have been set up, this should say something like “0 spins loaded and selected”. To fix this, click on the “Spin editor” button and you should then see the spin viewer window. The next steps are fully described in section 4.5.2 on page 40 for PDB files or section 4.5.3 on page 43 for a sequence file. The spin viewer window can now be closed.

### 6.4.4 NOE GUI mode – unresolved spins

Using the unresolved spins file as described in the prompt/script UI sections, the same spins can be deselected at this point. See Section 4.5.5 on page 44 for the details of how to deselect the spins in the GUI.

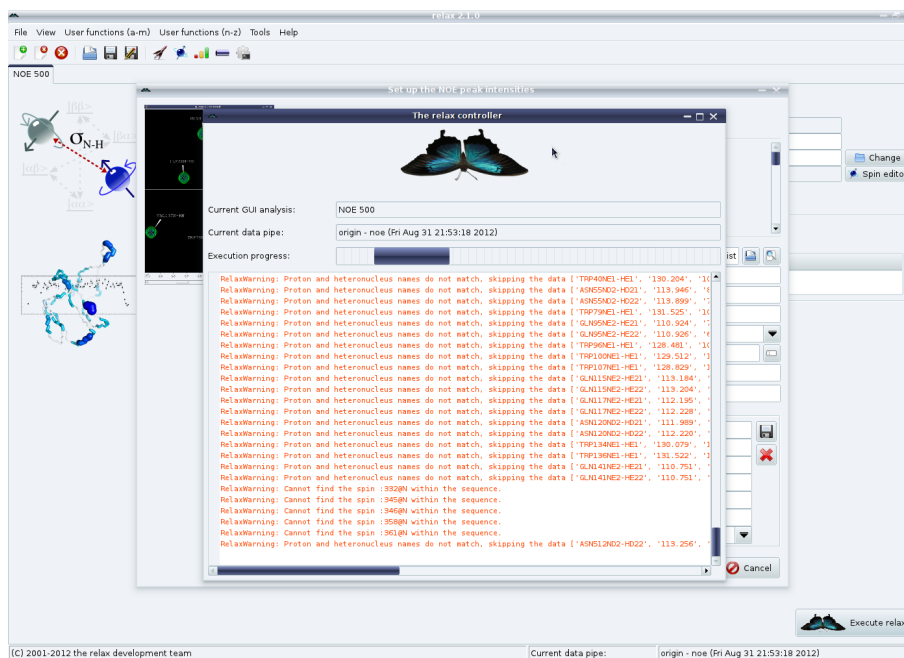
### 6.4.5 NOE GUI mode – loading the data

The next step is to load the saturated and reference NOE peak lists. From the main NOE auto-analysis tab, click on the “Add” button in the “Spectra list” GUI element. This will launch the NOE peak intensity loading wizard. From the first wizard page, select the peak list file containing the reference intensities (from the averaged shift list):

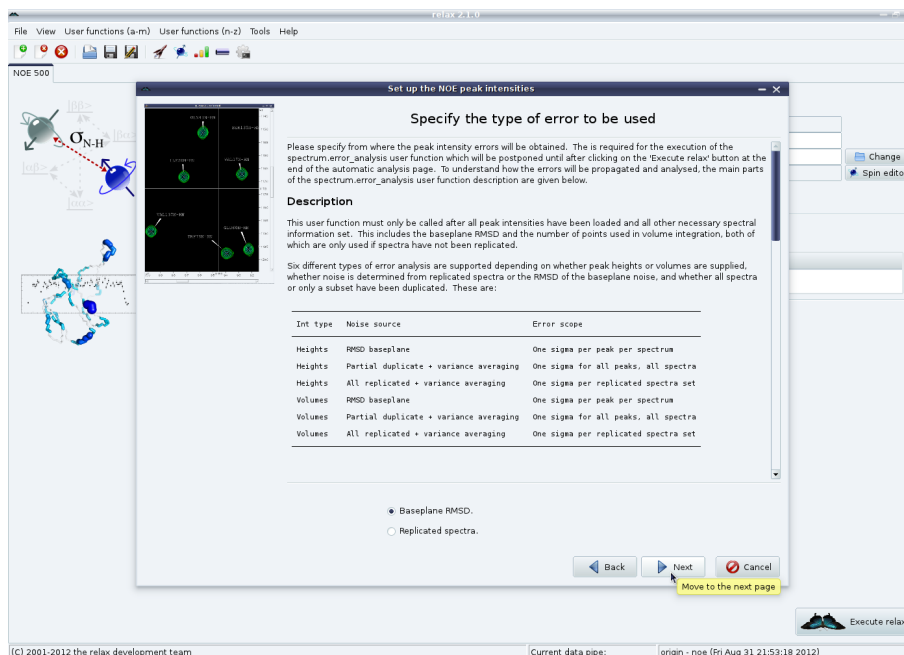


Then set the obligatory spectrum ID string to a unique value (in this case “ref”). The spectral dimension may need to be changed so that the peak intensities are associated with the correct atom of the pair. In case you have forgotten the spin names or the format of the peak list next to the file name selection button is a preview button which can be used to open the peak list in the default text editor. Set the other fields as needed. Click on “Next” Note that a **RelaxWarning** will be thrown for all peak list entries which do

not match a spin system within the relax data store. This will cause the relax controller window to appear:

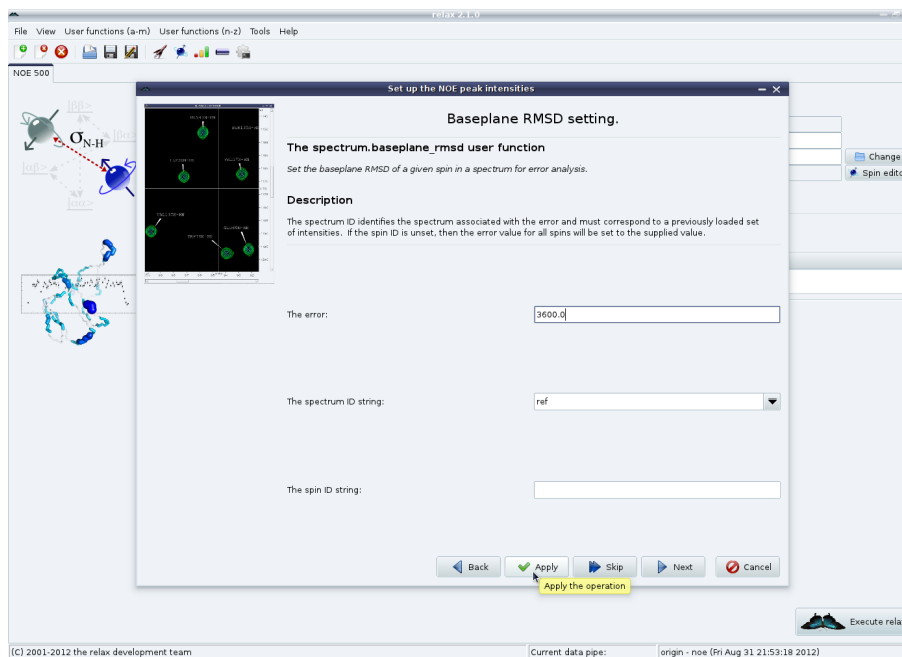


Carefully check these warnings to be sure that the data is correctly loaded and, if everything is fine, the relax controller window can be closed. If the dimension has been wrongly specified or some other setting is incorrect a **RelaxError** might appear saying that no data was loaded – you will then need to fix the settings and click on “Apply” again. The error type page should now appear.

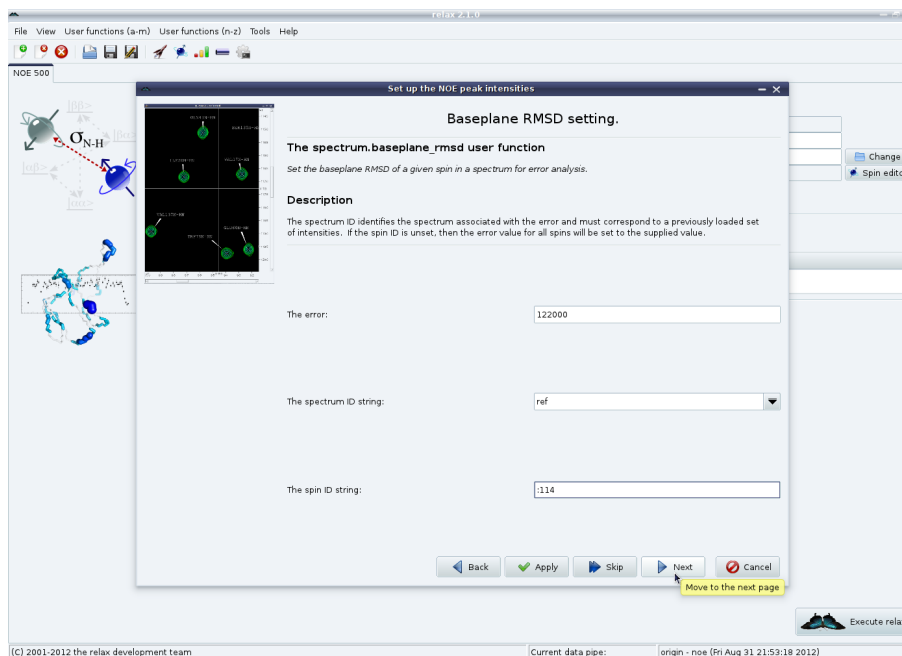


Please read the description in this window very carefully to know what to do next. In this example, we will choose “Baseplane RMSD”. For this specific example, Sparky’s “Extensions→Spectrum→Spectrum baseplane RMSD” option in the “F1” selection mode was used to measure empty regions of the spectrum (mainly in the random coil region) to

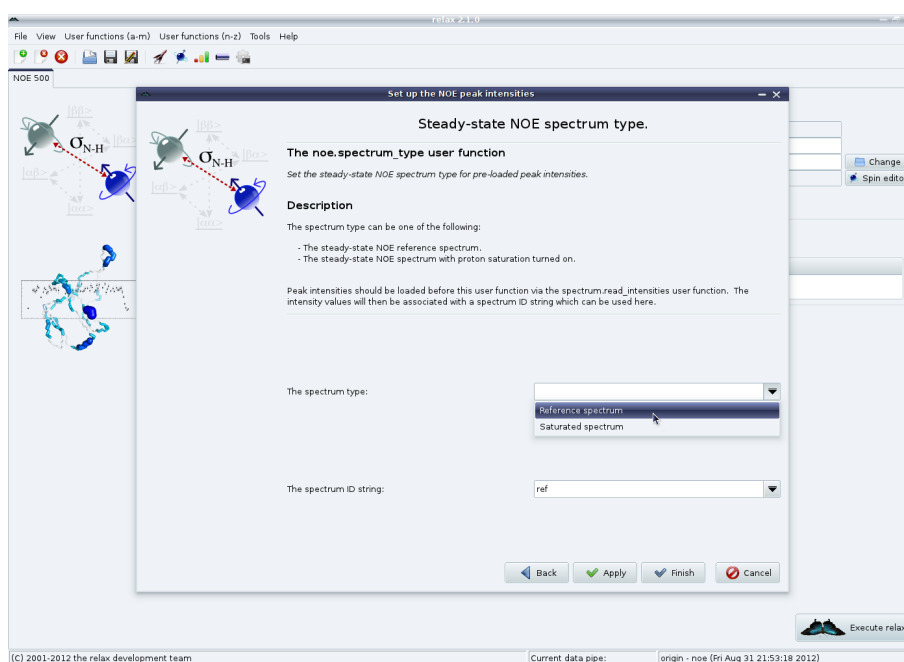
determine an average RMSD of approximately 3600. Set the value and click on “Apply”.



As glycine 114 is located close to the noise signal, its error was much higher at 122000. Individual spin errors can be set via the spin ID string (see section 4.2.2 on page 36 for information about spin IDs):

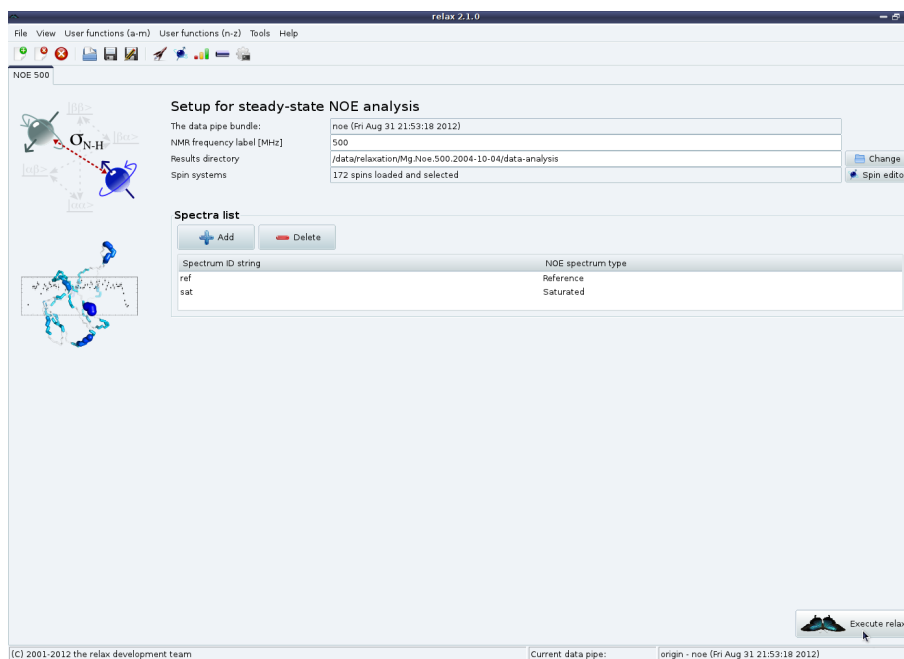


Finally select which type of spectrum this is and click on “Finish”:



The entire procedure should be repeated for the saturated spectrum (or you may have worked out that both can be loaded simultaneously by using the “Apply” button more often). For this example, the spectrum ID was set to “sat” and the baseplane RMSD to 3000 for all spins (except for G114 which had an error of 8500).

The NOE analysis tab should now look like:

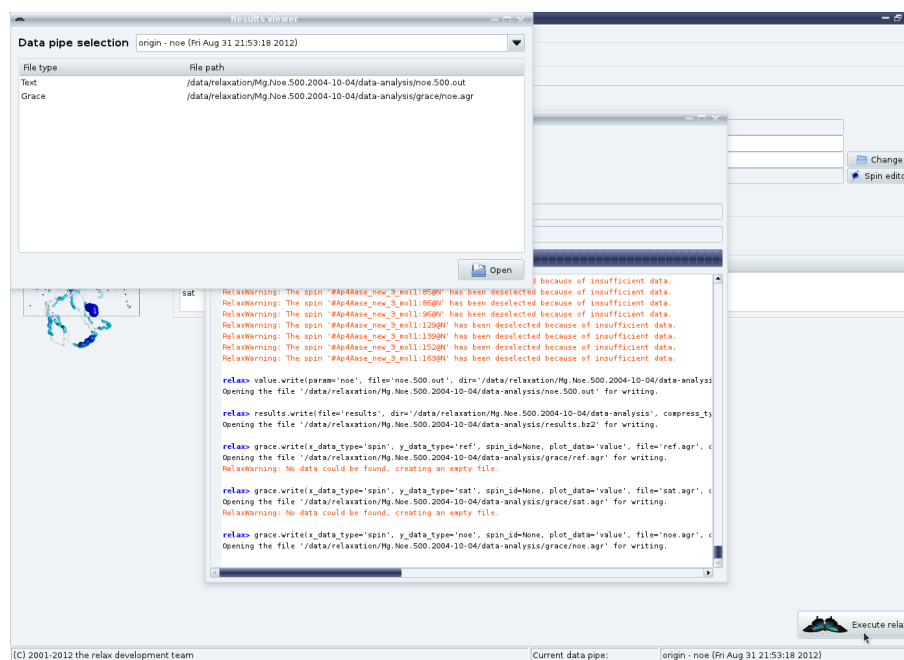


#### 6.4.6 NOE GUI mode – the NOE calculation

Now that everything is set up, simply click on “Execute relax” in the NOE analysis tab. The relax controller window will appear displaying many messages. These should all be



checked very carefully to make sure that everything has executed as you expected. The “Results viewer” window will also appear:



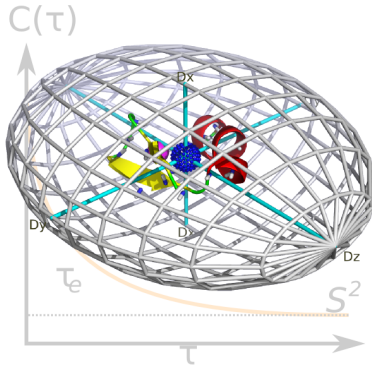
The results viewer window can be used to launch a text editor to see the NOE values and error or Grace to visualise the results (see Figure 6.1 on page 74).

As a last step, the relax state can be saved (via the “File” menu) and relax closed. Take one last look at the `noe.out` log file to be certain that there are no strange warnings or errors.



# Chapter 7

## Model-free analysis



### 7.1 Model-free theory

#### 7.1.1 The chi-squared function – $\chi^2(\theta)$

The chi-squared equation is itself dependent on the relaxation equations through the back-calculated relaxation data  $R(\theta)$ . Letting the relaxation values of the set  $R(\theta)$  be the  $R_1(\theta)$ ,  $R_2(\theta)$ , and  $\text{NOE}(\theta)$  an additional layer of abstraction can be used to simplify the calculation of the gradients and Hessians. This involves decomposing the NOE equation into the cross relaxation rate constant  $\sigma_{\text{NOE}}(\theta)$  and the auto relaxation rate  $R_1(\theta)$ . Taking equation (7.5) below the transformed relaxation equations are

$$R_1(\theta) = R'_1(\theta), \quad (7.1a)$$

$$R_2(\theta) = R'_2(\theta), \quad (7.1b)$$

$$\text{NOE}(\theta) = 1 + \frac{\gamma_H}{\gamma_X} \frac{\sigma_{\text{NOE}}(\theta)}{R_1(\theta)}. \quad (7.1c)$$

whereas the relaxation equations are the  $R_1(\theta)$ ,  $R_2(\theta)$ ,  $\sigma_{\text{NOE}}(\theta)$ .

### 7.1.2 The relaxation equations – $R'_i(\theta)$

The relaxation values of the set  $R'(\theta)$  include the spin-lattice, spin-spin, and cross-relaxation rates at all field strengths. These rates are respectively (Abragam, 1961)

$$R_1(\theta) = d \left( J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H + \omega_X) \right) + cJ(\omega_X), \quad (7.2a)$$

$$R_2(\theta) = \frac{d}{2} \left( 4J(0) + J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H) + 6J(\omega_H + \omega_X) \right) + \frac{c}{6} \left( 4J(0) + 3J(\omega_X) \right) + R_{ex}, \quad (7.2b)$$

$$\sigma_{\text{NOE}}(\theta) = d \left( 6J(\omega_H + \omega_X) - J(\omega_H - \omega_X) \right), \quad (7.2c)$$

where  $J(\omega)$  is the power spectral density function and  $R_{ex}$  is the relaxation due to chemical exchange. The dipolar and CSA constants are defined in SI units as

$$d = \frac{1}{4} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^6 \rangle}, \quad (7.3)$$

$$c = \frac{(\omega_H \Delta\sigma)^2}{3}, \quad (7.4)$$

where  $\mu_0$  is the permeability of free space,  $\gamma_H$  and  $\gamma_X$  are the gyromagnetic ratios of the  $H$  and  $X$  spins respectively,  $\hbar$  is Plank's constant divided by  $2\pi$ ,  $r$  is the bond length, and  $\Delta\sigma$  is the chemical shift anisotropy measured in ppm. The cross-relaxation rate  $\sigma_{\text{NOE}}$  is related to the steady state NOE by the equation

$$\text{NOE}(\theta) = 1 + \frac{\gamma_H}{\gamma_X} \frac{\sigma_{\text{NOE}}(\theta)}{R_1(\theta)}. \quad (7.5)$$

### 7.1.3 The spectral density functions – $J(\omega)$

The relaxation equations are themselves dependent on the calculation of the spectral density values  $J(\omega)$ . Within model-free analysis these are modelled by the original model-free formula (Lipari and Szabo, 1982a,b)

$$J(\omega) = \frac{2}{5} \sum_{i=-k}^k c_i \cdot \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2} \right), \quad (7.6)$$

where  $S^2$  is the square of the Lipari and Szabo generalised order parameter and  $\tau_e$  is the effective correlation time. The order parameter reflects the amplitude of the motion and the correlation time in an indication of the time scale of that motion. The theory was extended by Clore et al. (1990) by the modelling of two independent internal motions using the equation

$$J(\omega) = \frac{2}{5} \sum_{i=-k}^k c_i \cdot \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i)\tau_f}{(\tau_f + \tau_i)^2 + (\omega\tau_f\tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i)\tau_s}{(\tau_s + \tau_i)^2 + (\omega\tau_s\tau_i)^2} \right). \quad (7.7)$$

where  $S_f^2$  and  $\tau_f$  are the amplitude and timescale of the faster of the two motions whereas  $S_s^2$  and  $\tau_s$  are those of the slower motion.  $S_f^2$  and  $S_s^2$  are related by the formula  $S^2 = S_f^2 \cdot S_s^2$ .

If these forms of the model-free spectral density functions are unfamiliar, that is because these are the numerically stabilised forms presented in [d’Auvergne and Gooley \(2008a\)](#). The original model-free spectral density functions presented in [Lipari and Szabo \(1982a\)](#) and [Clore et al. \(1990\)](#) are not the most numerically stable form of these equations. An important problem encountered in optimisation is round-off error in which machine precision influences the result of mathematical operations. The double reciprocal  $\tau^{-1} = \tau_m^{-1} + \tau_e^{-1}$  used in the equations are operations which are particularly susceptible to round-off error, especially when  $\tau_e \ll \tau_m$ . By incorporating these reciprocals into the model-free spectral density functions and then simplifying the equations this source of round-off error can be eliminated, giving relax an edge over other model-free optimisation software.

#### 7.1.4 Brownian rotational diffusion

In equations (7.6) and (7.7) the generic Brownian diffusion NMR correlation function presented in [d’Auvergne \(2006\)](#) has been used. This function is

$$C(\tau) = \frac{1}{5} \sum_{i=-k}^k c_i \cdot e^{-\tau/\tau_i}, \quad (7.8)$$

where the summation index  $i$  ranges over the number of exponential terms within the correlation function. This equation is generic in that it can describe the diffusion of an ellipsoid, a spheroid, or a sphere.

#### Diffusion as an ellipsoid

For the ellipsoid defined by the parameter set  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$  the variable  $k$  is equal to two and therefore the index  $i \in \{-2, -1, 0, 1, 2\}$ . The geometric parameters  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r\}$  are defined as

$$\mathfrak{D}_{iso} = \frac{1}{3}(\mathfrak{D}_x + \mathfrak{D}_y + \mathfrak{D}_z), \quad (7.9a)$$

$$\mathfrak{D}_a = \mathfrak{D}_z - \frac{1}{2}(\mathfrak{D}_x + \mathfrak{D}_y), \quad (7.9b)$$

$$\mathfrak{D}_r = \frac{\mathfrak{D}_y - \mathfrak{D}_x}{2\mathfrak{D}_a}, \quad (7.9c)$$

and are constrained by

$$0 < \mathfrak{D}_{iso} < \infty, \quad (7.10a)$$

$$0 \leq \mathfrak{D}_a < \frac{\mathfrak{D}_{iso}}{\frac{1}{3} + \mathfrak{D}_r} \leq 3\mathfrak{D}_{iso}, \quad (7.10b)$$

$$0 \leq \mathfrak{D}_r \leq 1. \quad (7.10c)$$

The orientational parameters  $\{\alpha, \beta, \gamma\}$  are the Euler angles using the z-y-z rotation notation.

The five weights  $c_i$  are defined as

$$c_{-2} = \frac{1}{4}(d - e), \quad (7.11a)$$

$$c_{-1} = 3\delta_y^2\delta_z^2, \quad (7.11b)$$

$$c_0 = 3\delta_x^2\delta_z^2, \quad (7.11c)$$

$$c_1 = 3\delta_x^2\delta_y^2, \quad (7.11d)$$

$$c_2 = \frac{1}{4}(d + e), \quad (7.11e)$$

where

$$d = 3(\delta_x^4 + \delta_y^4 + \delta_z^4) - 1, \quad (7.12)$$

$$e = \frac{1}{\Re} \left[ (1 + 3\mathfrak{D}_r) (\delta_x^4 + 2\delta_y^2\delta_z^2) + (1 - 3\mathfrak{D}_r) (\delta_y^4 + 2\delta_x^2\delta_z^2) - 2(\delta_z^4 + 2\delta_x^2\delta_y^2) \right], \quad (7.13)$$

and where

$$\Re = \sqrt{1 + 3\mathfrak{D}_r^2}. \quad (7.14)$$

The five correlation times  $\tau_i$  are

$$1/\tau_{-2} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\Re, \quad (7.15a)$$

$$1/\tau_{-1} = 6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r), \quad (7.15b)$$

$$1/\tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r), \quad (7.15c)$$

$$1/\tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a, \quad (7.15d)$$

$$1/\tau_2 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\Re. \quad (7.15e)$$

### Diffusion as a spheroid

The variable  $k$  is equal to one in the case of the spheroid defined by the parameter set  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \theta, \phi\}$ , hence  $i \in \{-1, 0, 1\}$ . The geometric parameters  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a\}$  are defined as

$$\mathfrak{D}_{iso} = \frac{1}{3}(\mathfrak{D}_{\parallel} + 2\mathfrak{D}_{\perp}), \quad (7.16a)$$

$$\mathfrak{D}_a = \mathfrak{D}_{\parallel} - \mathfrak{D}_{\perp}. \quad (7.16b)$$

and are constrained by

$$0 < \mathfrak{D}_{iso} < \infty, \quad (7.17a)$$

$$-\frac{3}{2}\mathfrak{D}_{iso} < \mathfrak{D}_a < 3\mathfrak{D}_{iso}. \quad (7.17b)$$

The orientational parameters  $\{\theta, \phi\}$  are the spherical angles defining the orientation of the major axis of the diffusion frame within the lab frame.

The three weights  $c_i$  are

$$c_{-1} = \frac{1}{4}(3\delta_z^2 - 1)^2, \quad (7.18a)$$

$$c_0 = 3\delta_z^2(1 - \delta_z^2), \quad (7.18b)$$

$$c_1 = \frac{3}{4}(\delta_z^2 - 1)^2. \quad (7.18c)$$

The five correlation times  $\tau_i$  are

$$1/\tau_{-1} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a, \quad (7.19a)$$

$$1/\tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a, \quad (7.19b)$$

$$1/\tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a. \quad (7.19c)$$

### Diffusion as a sphere

In the situation of a molecule diffusing as a sphere either described by the single parameter  $\tau_m$  or  $\mathfrak{D}_{iso}$ , the variable  $k$  is equal to zero. Therefore  $i \in \{0\}$ . The single weight  $c_0$  is equal to one and the single correlation time  $\tau_0$  is equivalent to the global tumbling time  $\tau_m$  given by

$$1/\tau_m = 6\mathfrak{D}_{iso}. \quad (7.20)$$

This is diffusion equation presented in [Bloembergen et al. \(1948\)](#).

### 7.1.5 The model-free models

Extending the list of models given in [Mandel et al. \(1995\)](#); [Fushman et al. \(1997\)](#); [Orekhov et al. \(1999a\)](#); [Korzhnev et al. \(2001\)](#); [Zhuravleva et al. \(2004\)](#), the models built into relax include

$$m0 = \{\}, \quad (7.21.0)$$

$$m1 = \{S^2\}, \quad (7.21.1)$$

$$m2 = \{S^2, \tau_e\}, \quad (7.21.2)$$

$$m3 = \{S^2, R_{ex}\}, \quad (7.21.3)$$

$$m4 = \{S^2, \tau_e, R_{ex}\}, \quad (7.21.4)$$

$$m5 = \{S^2, S_f^2, \tau_s\}, \quad (7.21.5)$$

$$m6 = \{S^2, \tau_f, S_f^2, \tau_s\}, \quad (7.21.6)$$

$$m7 = \{S^2, S_f^2, \tau_s, R_{ex}\}, \quad (7.21.7)$$

$$m8 = \{S^2, \tau_f, S_f^2, \tau_s, R_{ex}\}, \quad (7.21.8)$$

$$m9 = \{R_{ex}\}. \quad (7.21.9)$$

The parameter  $R_{ex}$  is scaled quadratically with field strength in these models as it is assumed to be fast. In the set theory notation, the model-free model for the spin system  $i$  is represented by the symbol  $\mathfrak{F}_i$ . Through the addition of the local  $\tau_m$  to each of these models, only the component of Brownian rotational diffusion experienced by the spin

system is probed. These models, represented in set notation by the symbol  $\mathfrak{T}_i$ , are

$$tm0 = \{\tau_m\}, \quad (7.22.0)$$

$$tm1 = \{\tau_m, S^2\}, \quad (7.22.1)$$

$$tm2 = \{\tau_m, S^2, \tau_e\}, \quad (7.22.2)$$

$$tm3 = \{\tau_m, S^2, R_{ex}\}, \quad (7.22.3)$$

$$tm4 = \{\tau_m, S^2, \tau_e, R_{ex}\}, \quad (7.22.4)$$

$$tm5 = \{\tau_m, S^2, S_f^2, \tau_s\}, \quad (7.22.5)$$

$$tm6 = \{\tau_m, S^2, \tau_f, S_f^2, \tau_s\}, \quad (7.22.6)$$

$$tm7 = \{\tau_m, S^2, S_f^2, \tau_s, R_{ex}\}, \quad (7.22.7)$$

$$tm8 = \{\tau_m, S^2, \tau_f, S_f^2, \tau_s, R_{ex}\}, \quad (7.22.8)$$

$$tm9 = \{\tau_m, R_{ex}\}. \quad (7.22.9)$$

### 7.1.6 Model-free optimisation theory

The implementation of optimisation in relax is discussed in detail in Chapter 12. To understand the concepts in this subsection, it is best to look at that chapter first.

#### The model-free space

In model-free analysis the target function  $f(\theta)$  is the chi-squared equation

$$\chi^2(\theta) = \sum_{i=1}^n \frac{(R_i - R_i(\theta))^2}{\sigma_i^2}, \quad (7.23)$$

where  $i$  is the summation index,  $R_i$  is the experimental relaxation data which belongs to the data set  $R$  and includes the  $R_1$ ,  $R_2$ , and NOE values at all field strengths,  $R_i(\theta)$  is the back calculated relaxation data belonging to the set  $R(\theta)$ , and  $\sigma_i$  is the experimental error. For the optimisation of the model-free parameters while the diffusion tensor is held fixed, the summation index ranges over the relaxation data of an individual spin. If the diffusion parameters are optimised simultaneously with the model-free parameters the summation index ranges over all relaxation data of all selected spins of the macromolecule.

Given the current parameter values the model-free function provided to the algorithm will calculate the value of the model-free spectral density function  $J(\omega)$  at the five frequencies which induce NMR relaxation by using Equations (7.6) and (7.7). The theoretical  $R_1$ ,  $R_2$ , and NOE values are then back-calculated using Equations (7.2a), (7.2b), (7.2c), and (7.5). Finally, the chi-squared value is calculated using Equation (7.23).

To produce the gradient and Hessian required for model-free optimisation a large chain of first and second partial derivatives needs to be calculated. Firstly the partial derivatives of the spectral density functions (7.6) and (7.7) are necessary. Then the partial derivatives of the relaxation equations (7.2a) to (7.2c) followed by the NOE equation (7.5) are needed. Finally the partial derivative of the chi-squared formula (7.23) is required. These first and second partial derivatives, as well as those of the components of the Brownian diffusion correlation function for non-isotropic tumbling, are presented as Chapter 13.



### Grid search

Due to the complexity of the curvature of the model-free space, the grid point with the lowest chi-squared value may in fact be on the opposite side of the space to the local minimum. Therefore the model-free space renders many optimisation algorithms ineffective (d'Auvergne and Gooley, 2008a).

### Parameter constraints

To understand this section, please see Section 12.5 on page 222. For model-free analysis, linear constraints are the most useful type of constraint as the correlation time  $\tau_f$  can be restricted to being less than  $\tau_s$  by using the inequality  $\tau_s - \tau_f \geq 0$ .

For the parameters specific to individual spins the linear constraints in the notation of (12.18) are

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 \end{pmatrix} \cdot \begin{pmatrix} S^2 \\ S_f^2 \\ S_s^2 \\ \tau_e \\ \tau_f \\ \tau_s \\ R_{ex} \\ r \\ CSA \end{pmatrix} \geq \begin{pmatrix} 0 \\ -1 \\ 0 \\ -1 \\ 0 \\ -1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0.9e^{-10} \\ 2e^{-10} \\ 300e^{-6} \\ 0 \end{pmatrix}. \quad (7.24)$$

Through the isolation of each individual element, the constraints can be seen to be equivalent to

$$0 \leq S^2 \leq 1, \quad (7.25a)$$

$$0 \leq S_f^2 \leq 1, \quad (7.25b)$$

$$0 \leq S_s^2 \leq 1, \quad (7.25c)$$

$$S^2 \leq S_f^2, \quad (7.25d)$$

$$S^2 \leq S_s^2, \quad (7.25e)$$

$$\tau_e \geq 0, \quad (7.25f)$$

$$\tau_f \geq 0, \quad (7.25g)$$

$$\tau_s \geq 0, \quad (7.25h)$$

$$\tau_s \geq 0, \quad (7.25i)$$

$$\tau_f \leq \tau_s, \quad (7.25j)$$

$$R_{ex} \geq 0, \quad (7.25k)$$

$$0.9e^{-10} \leq r \leq 2e^{-10}, \quad (7.25l)$$

$$-300e^{-6} \leq CSA \leq 0. \quad (7.25m)$$

To prevent the computationally expensive optimisation of failed models in which the internal correlation times minimise to infinity (d'Auvergne and Gooley, 2006), the constraint  $\tau_e, \tau_f, \tau_s \leq 2\tau_m$  was implemented. When the global correlation time is fixed the constraints in the matrix notation of (12.18) are

$$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \cdot \begin{pmatrix} \tau_e \\ \tau_f \\ \tau_s \end{pmatrix} \geq \begin{pmatrix} -2\tau_m \\ -2\tau_m \\ -2\tau_m \end{pmatrix}. \quad (7.26)$$

However when the global correlation time  $\tau_m$  is one of the parameters being optimised the constraints become

$$\begin{pmatrix} 2 & -1 & 0 & 0 \\ 2 & 0 & -1 & 0 \\ 2 & 0 & 0 & -1 \end{pmatrix} \cdot \begin{pmatrix} \tau_m \\ \tau_e \\ \tau_f \\ \tau_s \end{pmatrix} \geq \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}. \quad (7.27)$$

For the parameters of the diffusion tensor the constraints utilised are

$$0 \leq \tau_m \leq 200.0e^{-9}, \quad (7.28a)$$

$$\mathfrak{D}_a \geq 0, \quad (7.28b)$$

$$0 \leq \mathfrak{D}_r \leq 1, \quad (7.28c)$$

which in the matrix notation of (12.18) become

$$\begin{pmatrix} 1 & 0 & 0 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & -1 \end{pmatrix} \cdot \begin{pmatrix} \tau_m \\ \mathfrak{D}_a \\ \mathfrak{D}_r \end{pmatrix} \geq \begin{pmatrix} 0 \\ -200.0e^{-9} \\ 0 \\ 0 \\ -1 \end{pmatrix}. \quad (7.29)$$

The upper limit of 200 ns on  $\tau_m$  prevents the parameter from heading towards infinity when model failure occurs (see d'Auvergne and Gooley (2006)). This can significantly decrease the computation time. To isolate the prolate spheroid the constraint

$$(1) \cdot (\mathfrak{D}_a) \geq (0), \quad (7.30)$$

is used whereas to isolate the oblate spheroid the constraint used is

$$(-1) \cdot (\mathfrak{D}_a) \geq (0). \quad (7.31)$$

Dependent on the model optimised, the matrix  $A$  and vector  $b$  are constructed from combinations of the above linear constraints.

### Diagonal scaling

The concept of diagonal scaling is explained in Section 12.6 on page 224.

For the model-free analysis the scaling factor of one is used for the order parameter and a scaling factor of  $1e^{-12}$  is used for the correlation times. The  $R_{ex}$  parameter is scaled to be the chemical exchange rate of the first field strength. The scaling matrix for the parameters  $\{S^2, S_f^2, S_s^2, \tau_e, \tau_f, \tau_s, R_{ex}, r, CSA\}$  of individual spins is

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1e^{-12} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1e^{-12} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1e^{-12} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & (2\pi\omega_H)^{-2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^{-10} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^{-4} \end{pmatrix}. \quad (7.32)$$

For the ellipsoidal diffusion parameters  $\{\tau_m, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$  the scaling matrix is

$$\begin{pmatrix} 1e^{-12} & 0 & 0 & 0 & 0 & 0 \\ 0 & 1e^7 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}. \quad (7.33)$$

For the spheroidal diffusion parameters  $\{\tau_m, \mathfrak{D}_a, \theta, \phi\}$  the scaling matrix is

$$\begin{pmatrix} 1e^{-12} & 0 & 0 & 0 \\ 0 & 1e^7 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}. \quad (7.34)$$

## 7.2 Optimisation of a single model-free model

### 7.2.1 Single model-free model script mode – the sample script

The sample script which demonstrates the optimisation of model-free model *m4* which consists of the parameters  $\{S^2, \tau_e, R_{ex}\}$  is `model_free/single_model.py`. The text of the script is:

```

1 # Script for model-free analysis.
2
3 # Create the data pipe.
4 name = 'm4'
5 pipe.create(name, 'mf')
6
```

```

7  # Set up the 15N spins.
8  sequence.read('noe.500.out', res_num_col=1, res_name_col=2)
9  spin.name('N')
10 spin.element(element='N', spin_id='@N')
11 spin.isotope('15N', spin_id='@N')
12
13 # Load the relaxation data.
14 relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
15                 res_num_col=1, data_col=3, error_col=4)
16 relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
17                 res_num_col=1, data_col=3, error_col=4)
18 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
19                 res_num_col=1, data_col=3, error_col=4)
20
21 relax_data.read(ri_id='R1_500', ri_type='R1', frq=500.0*1e6, file='r1.500.out',
22                 res_num_col=1, data_col=3, error_col=4)
23 relax_data.read(ri_id='R2_500', ri_type='R2', frq=500.0*1e6, file='r2.500.out',
24                 res_num_col=1, data_col=3, error_col=4)
25 relax_data.read(ri_id='NOE_500', ri_type='NOE', frq=500.0*1e6, file='noe.500.out',
26                 res_num_col=1, data_col=3, error_col=4)
27
28 # Initialise the diffusion tensor.
29 diffusion_tensor.init(10e-9, fixed=True)
30
31 # Create all attached protons.
32 sequence.attach_protons()
33
34 # Define the magnetic dipole-dipole relaxation interaction.
35 interatom.define(spinid1='@N', spin_id2='@H', direct_bond=True)
36 interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)
37 #interatom.unit_vectors()
38
39 # Define the CSA relaxation interaction.
40 value.set(-172 * 1e-6, 'csa')
41
42 # Select the model-free model.
43 model_free.select_model(model=name)
44
45 # Grid search.
46 grid_search(inc=11)
47
48 # Minimise.
49 minimise('newton')
50
51 # Monte Carlo simulations.
52 monte_carlo.setup(number=100)
53 monte_carlo.create_data()
54 monte_carlo.initial_values()
55 minimise('newton')
56 eliminate()
57 monte_carlo.error_analysis()
58
59 # Finish.
60 results.write(file='results', force=True)
61 state.save('save', force=True)

```

## 7.2.2 Single model-free model script mode – explanation

The above script consists of three major sections:

**Loading of data** Firstly a data pipe called “m4” is created to hold all of the analysis data. Then the  $^{15}\text{N}$  spin system data consisting of molecule, residue, and spin information is loaded into relax from the columns of the `noe.500.out` file, assuming that only residue numbers and names are present and are in the first and second columns respectively. The options of this `sequence.read` user function allow the molecule name, residue number, residue name, spin number, or spin name columns to be specified if desired. The  $^{15}\text{N}$  spin is then set up using the `spin` user functions. The next part is to load all of the relaxation data, to set up the initial diffusion tensor, create the  $^1\text{H}$  spins required for the magnetic dipole-dipole interaction, and to set up the magnetic dipole-dipole and CSA relaxation mechanisms. Finally the model-free model “m4” is chosen.

**Optimisation** The optimisation of model-free models requires an initial grid search to find a position close to the minimum, followed by the high precision Newton optimisation together with the Method of Multipliers constraint algorithm (d’Auvergne and Gooley, 2008a). Errors are propagated from the relaxation data to the model-free parameters via Monte Carlo simulations which is a multi-step process in relax (designed for flexibility and to teach how the simulations are constructed and carried out).

**Data output** The last stage consists of writing out the XML formatted results file which contains all of the data in the current data pipe, as well as the XML formatted save file which contains not only the current data pipe data but all of the relax data store data. Both files can be loaded back into relax later on.

## 7.3 Optimisation of all model-free models

### 7.3.1 All model-free models script mode – the sample script

The sample script which demonstrates the optimisation of all model-free models from *m0* to *m9* of individual spins is `model_free/mf_multimodel.py`. The important parts of the script are:

```

1  # Set the data pipe names (also the names of preset model-free models).
2  pipes = ['m0', 'm1', 'm2', 'm3', 'm4', 'm5', 'm6', 'm7', 'm8', 'm9']
3
4  # Loop over the pipes.
5  for name in pipes:
6      # Create the data pipe.
7      pipe.create(name, 'mf')
8
9      # Set up the 15N spins.
10     sequence.read('noe.500.out', res_num_col=1)
11     spin.name('N')
12     spin.element(element='N', spin_id='@N')
13     spin.isotope('15N', spin_id='@N')
14
15     # Load a PDB file.
16     structure.read_pdb('example.pdb')
17
18     # Load the relaxation data.
19     relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
        res_num_col=1, data_col=3, error_col=4)

```

```

20 relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
21 res_num_col=1, data_col=3, error_col=4)
22 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
23 res_num_col=1, data_col=3, error_col=4)
24 relax_data.read(ri_id='R1_500', ri_type='R1', frq=500.0*1e6, file='r1.500.out',
25 res_num_col=1, data_col=3, error_col=4)
26 relax_data.read(ri_id='R2_500', ri_type='R2', frq=500.0*1e6, file='r2.500.out',
27 res_num_col=1, data_col=3, error_col=4)
28 relax_data.read(ri_id='NOE_500', ri_type='NOE', frq=500.0*1e6, file='noe.500.out',
29 res_num_col=1, data_col=3, error_col=4)
30
31 # Set up the diffusion tensor.
32 diffusion_tensor.init(1e-8, fixed=True)
33
34 # Generate the 1H spins for the magnetic dipole-dipole relaxation interaction.
35 sequence.attach_protons()
36
37 # Define the magnetic dipole-dipole relaxation interaction.
38 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
39 interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)
40 structure.get_pos('@N')
41 structure.get_pos('@H')
42 interatom.unit_vectors()
43
44 # Define the chemical shift relaxation interaction.
45 value.set(-172 * 1e-6, 'csa', spin_id='@N')
46
47 # Select the model-free model.
48 model_free.select_model(model=name)
49
50 # Minimise.
51 grid_search(inc=11)
52 minimise('newton')
53
54 # Write the results.
55 results.write(file='results', force=True)
56
57 # Save the program state.
58 state.save('save', force=True)

```

### 7.3.2 All model-free models script mode – explanation

The above script is very similar in spirit to the previous single model script in section 7.2 on page 91. The major difference is that this script loops over all of the model-free models, saving all of the results in the `save.bz2` file.

## 7.4 Model-free model selection

### 7.4.1 Model-free model selection script mode – the sample script

The sample script which demonstrates both model-free model elimination and model-free model selection between models from  $m0$  to  $m9$  is `model_free/modsel.py`. The text of the script is:

```

1  # Set the data pipe names.
2  pipes = ['m0', 'm1', 'm2', 'm3', 'm4', 'm5', 'm6', 'm7', 'm8', 'm9']
3
4  # Loop over the data pipe names.
5  for name in pipes:
6      print("\n\n# " + name + " #")
7
8      # Create the data pipe.
9      pipe.create(name, 'mf')
10
11     # Reload precalculated results from the file 'm1/results', etc.
12     results.read(file='results', dir=name)
13
14 # Model elimination.
15 eliminate()
16
17 # Model selection.
18 model_selection(method='AIC', modsel_pipe='aic')
19
20 # Write the results.
21 state.save('save', force=True)
22 results.write(file='results', force=True)

```

#### 7.4.2 Model-free model selection script mode – explanation

This script is designed to be used in conjunction with the `model_free/mf_multimodel.py` script in the previous section. It will load all of the results files from the previous script and then perform the following:

**Model-free model elimination** The optimisation of model-free models performed by the previous script will fail for certain data sets together with certain models. To ensure that these models are never selected, they are removed from the analysis (see [d’Auvergne and Gooley \(2006\)](#)).

**Model-free model selection** The AIC model selection as described in [d’Auvergne and Gooley \(2003\)](#) will be used to determine which model-free model best describes the relaxation data.

**Data output** Finally both a save state and result file will be created.

These three sample scripts describe the basic components of model-free analysis. However a full analysis requires the construction of a much more complex iterative procedure. The following sections will describe both the original diffusion seeded approaches as well as the new model-free protocol built into relax.

## 7.5 The methodology of Mandel et al., 1995

By presenting a systematic methodology for obtaining a consistent model-free description of the dynamics of the system, the manuscript of [Mandel et al. \(1995\)](#) revolutionised the application of model-free analysis. The full protocol is presented in Figure 7.1.

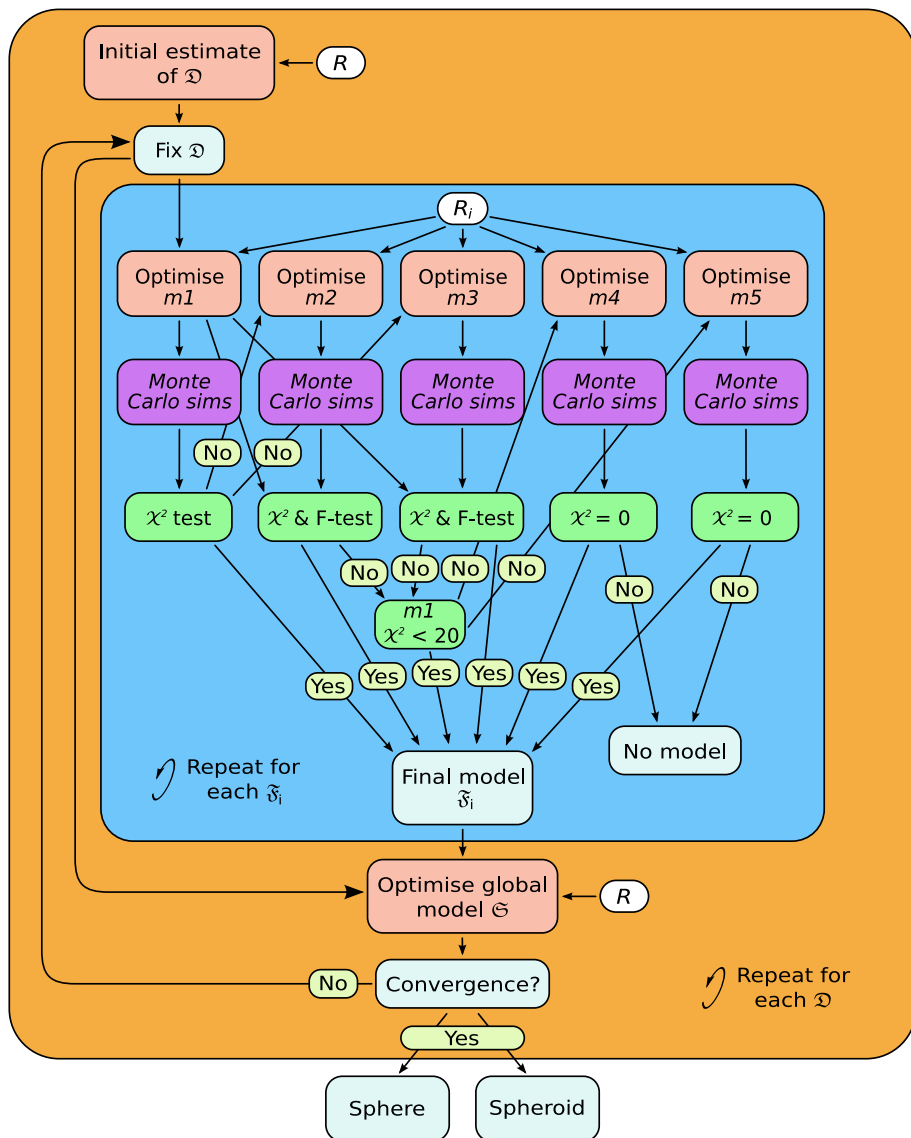


Figure 7.1: A schematic of the model-free optimisation protocol of Mandel et al. (1995). This specific protocol is for single field strength data. The initial diffusion tensor estimate is calculated using the  $R_2/R_1$  ratio. The diffusion parameters of  $\mathcal{D}$  are held constant while model-free models  $m_1$  to  $m_5$  (7.21.1–7.21.5) of the set  $\mathfrak{F}_i$  for each spin  $i$  are optimised and 500 Monte Carlo simulations executed. Using a web of ANOVA statistical tests, specifically  $\chi^2$  and F-tests, a step-up hypothesis testing model selection procedure is used to choose the best model-free model. These steps are repeated for all spins of the molecule. The global model  $\mathfrak{S}$ , the union of  $\mathcal{D}$  and all  $\mathfrak{F}_i$ , is then optimised. These steps are repeated until convergence of the global model. The iterative process is repeated for both isotropic diffusion (sphere) and anisotropic diffusion (spheroid).



All of the data analysis techniques required for this protocol can be implemented within relax. The chi-squared distributions required for the chi-squared tests are constructed by Modelfree4 from the Monte Carlo simulations. If the optimisation algorithms and Monte Carlo simulations built into relax are utilised, then the relax script will need to construct the chi-squared distributions from the results as this is not yet coded into relax. The specific step-up hypothesis testing model selection of Mandel et al. (1995) is available through the `model_selection` user function. Coding the rest of the protocol into a script should be straightforward.

To implement this analysis, a number of scripts would need to be written. There is no sample script in relax for performing this analysis. The simple sample scripts from above would need to be extended. For example a starting script for determining the initial diffusion tensor estimates based on the R1/R2 ratio of Kay et al. (1989) would have to be written. The tensor from this script could then be feed into the `model_free/mf_multimodel.py` script, followed by the `model_free/modsel.py` script, and then a third script written to optimise the diffusion tensor. A master script could be written first run the initial diffusion tensor script, then to iteratively execute the last three scripts until convergence, and finally to select the best diffusion model (see Figure 7.1). Alternatively, these could all be combined into one super script.

## 7.6 The diffusion seeded paradigm

Ever since the original Lipari and Szabo papers (Lipari and Szabo, 1982a,b), the question of how to obtain the model-free description of the system has followed the route in which the diffusion tensor is initially estimated. Using this rough estimate, the model-free models are optimised for each spin system  $i$ , the best model selected, and then the global model  $\mathfrak{S}$  of the diffusion model  $\mathfrak{D}$  with each model-free model  $\mathfrak{F}_i$  is optimised. This procedure is then repeated using the diffusion tensor parameters of  $\mathfrak{S}$  as the initial input. Finally the global model is selected. The full protocol, when combined with AIC model selection (d’Auvergne and Gooley, 2003), is illustrated in Figure 7.2.

Again this protocol is not implemented in the relax sample scripts. This would have to be implemented in exactly the same manner as described in the previous section, but using the AIC model selection build into relax. Constructing this set of scripts, or a single master script, would be much easier than the Mandel et al. (1995) protocol as Modelfree4 would not need to be used, and the handling of F-tests and chi-squared tests is avoided.

## 7.7 The new model-free optimisation protocol

Here a new, fully automated model-free optimisation protocol will be presented. This protocol, defined in d’Auvergne and Gooley (2007) and d’Auvergne and Gooley (2008b), is significantly different from all those that came before, reversing the diffusion seeded paradigm as detailed below. Within relax it is referred to as the “new protocol” or the “d’Auvergne protocol”. The later name is to allow for more advanced protocols to be developed and added to relax by adventurous users in the future.

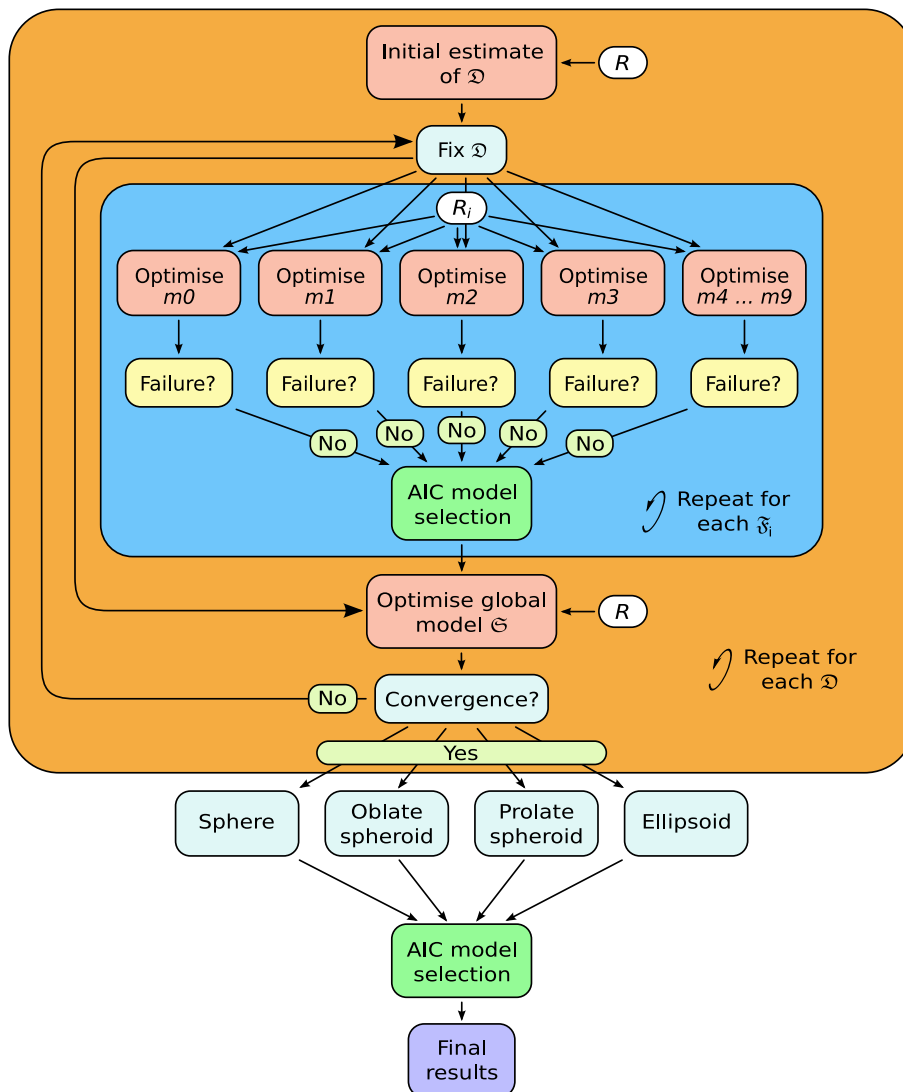


Figure 7.2: A schematic of model-free analysis using the diffusion seeded paradigm – the initial diffusion tensor estimate – together with AIC model selection and model elimination. The initial estimates of the parameters of  $\mathcal{D}$  are held constant while model-free models  $m_0$  to  $m_9$  (7.21.0–7.21.9) of the set  $\mathfrak{F}_i$  for each spin system  $i$  are optimised, model elimination applied to remove failed models, and AIC model selection used to determine the best model. The global model  $\mathfrak{S}$ , the union of  $\mathcal{D}$  and all  $\mathfrak{F}_i$ , is then optimised. These steps are repeated until convergence of the global model. The entire iterative process is repeated for each of the Brownian diffusion models. Finally AIC model selection is used to determine the best description of the dynamics of the molecule by selecting between the global models  $\mathfrak{S}$  including the sphere, oblate spheroid, prolate spheroid, and ellipsoid. Once the solution has been found, Monte Carlo simulations can be utilised for error analysis.

### 7.7.1 The new protocol – model-free models

The study of the dynamics of a macromolecule using model-free analysis to interpret the  $R_1$  and  $R_2$  relaxation rates together with the steady-state heteronuclear NOE brings two distinct, yet linked physical theories into play. The Brownian rotational diffusion of the molecule is the major contributor to relaxation. Although having less of an influence on relaxation the internal dynamics of individual nuclei within the molecule is nevertheless significant. The model-free description of the internal motion and the global diffusion of the entire molecule are theories which are linked due to their dependence on the same relaxation data. The model-free models for individual spin system constructed from the original and extended model-free theories (Lipari and Szabo, 1982a,b; Clore et al., 1990) are assembled using parametric restrictions, the dropping of insignificant parameters, and the addition of the chemical exchange parameter  $R_{ex}$ . Labelled as  $m0$  to  $m9$  (Models 7.21.0–7.21.9 on page 87) these models are an extended list of those in (Fushman et al., 1997; Orekhov et al., 1999a; Korzhnev et al., 2001; Zhuravleva et al., 2004).

### 7.7.2 The new protocol – the diffusion tensor

#### The ellipsoid

The most general form of Brownian rotational diffusion of macromolecules is the diffusion of an ellipsoid, a diffusion also labelled as asymmetric or fully anisotropic. This diffusion tensor can be fully specified by the geometric parameters  $\mathfrak{D}_x$ ,  $\mathfrak{D}_y$ , and  $\mathfrak{D}_z$ , the eigenvalues of the tensor, as well as three orientational parameters, the Euler angles  $\alpha$ ,  $\beta$ , and  $\gamma$ . The diffusion equation for an ellipsoid was derived using the reasoning of Einstein (1905) in the two papers of Perrin (1934) and Perrin (1936). Following this, Favro (1960) unknowingly derived the same equations as presented in Perrin (1936) using a pseudo quantum mechanical approach. Borrowing heavily from Perrin (1936), Woessner (1962) derived the correlation function relevant for NMR relaxation of a bond vector rigidly attached to an ellipsoid. However these equations are not fully simplified and the parameter set  $\{\mathfrak{D}_x, \mathfrak{D}_y, \mathfrak{D}_z, \alpha, \beta, \gamma\}$ , the eigenvalues and Euler angles defining the tensor, is not optimally constructed for minimisation. A parameter shift to the set  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$ , whereby the three geometric parameters are respectively the isotropic, anisotropic, and rhombic components of the diffusion tensor, drastically simplifies optimisation and is how the diffusion tensor is implemented within relax.

#### The spheroid

When two of the eigenvalues of the diffusion tensor are equal the molecule diffuses as a spheroid. This is also called axially symmetric anisotropic diffusion and can be described by the two geometric parameters  $\mathfrak{D}_{iso}$  and  $\mathfrak{D}_a$  together with the polar angle  $\theta$  and azimuthal angle  $\phi$  which define the unique axis of the diffusion tensor. Two classes of spheroid can be distinguished dependent on the relative values of the eigenvalues – the prolate and oblate spheroids. By using parametric constraints, both tensor types can be optimised within relax.

## The sphere

The simplest form of diffusion occurs when all three eigenvalues are equal and the molecule diffuses as a sphere. This isotropic rotation can be characterised by the single parameter  $\mathfrak{D}_{iso}$  which is related to the global correlation time by the formula  $1/\tau_m = 6\mathfrak{D}_{iso}$  (Bloembergen et al., 1948).

## The local $\tau_m$ model-free models

Not only can the diffusion tensor be optimised as a global model affecting all spins of the molecule but a set of model-free models can be constructed in which each spin is assumed to diffuse independently. In these models a single local  $\tau_m$  parameter approximates the true, multiexponential description of the Brownian rotational diffusion of the molecule. Each spin of the macromolecule is treated independently. Another set of model-free models which include the local  $\tau_m$  parameter can be created and include *tm0* to *tm9* (Models 7.22.0–7.22.9 on page 88). These are simply models *m0* to *m9* with the local  $\tau_m$  parameter added. These models are an extension of the ideas introduced in Barbato et al. (1992) and Schurr et al. (1994) whereby the model *tm2*, the original Lipari and Szabo model-free equation with a local  $\tau_m$  parameter, is optimised to avoid issues with inaccurate diffusion tensor approximations.

## Determination of the diffusion tensor from the local $\tau_m$ parameter

In Brüschweiler et al. (1995) and further investigated in Lee et al. (1997), a methodology for determining the diffusion tensor from the local  $\tau_m$  parameter together with the orientation of the XH bond represented by the unit vector  $\mu_i$  was presented. A local  $\tau_m$  value was obtained for each spin  $i$  by optimising model *tm2*. The  $\tau_{m,i}$  values were approximated using the quadric model

$$(6\tau_{m,i})^{-1} = \mu_i^T Q \mu_i, \quad (7.35)$$

where the eigenvalues of the matrix  $Q$  are defined as  $Q_x = (\mathfrak{D}_y + \mathfrak{D}_z)/2$ ,  $Q_y = (\mathfrak{D}_x + \mathfrak{D}_z)/2$ , and  $Q_z = (\mathfrak{D}_x + \mathfrak{D}_y)/2$ . The diffusion tensor is then found by linear least-squares fitting.

### 7.7.3 The universal solution $\mathfrak{U}$

The complex model-free problem, in which the motions of each spin are both mathematically and statistically dependent on the diffusion tensor and vice versa, was formulated using set theory in d’Auvergne and Gooley (2007). This paper is important for understanding the entire concept of the new protocol in relax and for truly grasping the complexity of the model-free problem. The solution  $\hat{\mathfrak{U}}$  to the model-free problem was derived as an element of the universal set  $\mathfrak{U}$ , the union of the diverse model-free parameter spaces  $\mathfrak{S}$ . Each set  $\mathfrak{S}$  was constructed from the union of the model-free models  $\mathfrak{F}$  for all spins and the diffusion parameter set  $\mathfrak{D}$ . A single parameter loss on a single spin shifts optimisation to a different space  $\mathfrak{S}$ . Ever since the seminal work of Kay et al. (1989) the model-free problem has been tackled by first finding an initial estimate of the diffusion tensor and then determining the model-free dynamics of the system (see Sections 7.5 on page 95 and 7.6

on page 97). This diffusion seeded paradigm is now highly evolved and much theory has emerged to improve this path to the solution  $\hat{\mathfrak{U}}$ . The technique can, at times, suffer from a number of issues including the two minima problem of the spheroid diffusion tensor parameter space, the appearance of artificial chemical exchange (Tjandra et al., 1996), the appearance of artificial nanosecond motions (Schurr et al., 1994), and the hiding of internal nanosecond motions caused by the violation of the rigidity assumption (Orekhov et al., 1995b, 1999a,b).

#### 7.7.4 Model-free analysis in reverse

A different approach was proposed in d’Auvergne and Gooley (2008b) for finding the universal solution  $\hat{\mathfrak{U}}$  of the extremely complex, convoluted model-free optimisation and modelling problem (d’Auvergne and Gooley, 2007), defined as

$$\hat{\mathfrak{U}} = \hat{\theta} \in \left\{ \mathfrak{S} : \min_{\hat{\theta} \in \mathfrak{U}} \Delta_{\text{K-L}}(\hat{\theta}) \right\}, \quad \text{s.t. } \hat{\theta} = \arg \min \{ \chi^2(\theta) : \theta \in \mathfrak{S} \}. \quad (7.36)$$

This notation says that the minimised parameter vector within the space  $\mathfrak{S}$  which minimises the common Kullback-Leibler discrepancy  $\Delta_{\text{K-L}}$  is selected from the universal set  $\mathfrak{U}$  as the universal solution  $\hat{\mathfrak{U}}$ . The discrepancy of Kullback and Leibler (1951) is a measure of how well the model fits the data, in this case how well the global model  $\mathfrak{S}$  of the diffusion tensor together with the model-free models of all residues fits the relaxation data. This selection is subject to the condition that  $\hat{\theta}$  is the argument or specific parameter vector which minimises the chi-squared function  $\chi^2(\theta)$  such that  $\theta$  is an element of the space  $\mathfrak{S}$ . Whereas the minimisation of the continuous chi-squared function within the single space  $\mathfrak{S}$  belongs to the mathematical field of optimisation (Nocedal and Wright, 1999), the selection of the universe  $\mathfrak{S}$  which minimises the discrepancy belongs to the statistical field of model selection (Akaike, 1973; Schwarz, 1978; Linhart and Zucchini, 1986; Zucchini, 2000; d’Auvergne and Gooley, 2003).

This new model-free optimisation protocol incorporates the ideas of the local  $\tau_m$  model-free model (Barbato et al., 1992; Schurr et al., 1994) and the optimisation of the diffusion tensor using information from these models, analogously to the linear least-squares fitting of the quadric model (Brüschweiler et al., 1995; Lee et al., 1997). The protocol also follows the lead of the model-free optimisation protocol presented in Butterwick et al. (2004) whereby the diffusion seeded paradigm was reversed. Rather than starting with an initial estimation of the global diffusion tensor from the set  $\mathfrak{D}$  the protocol starts with the model-free parameters from  $\mathfrak{F}$ .

The first step of the Butterwick et al. (2004) protocol is the reduced spectral density mapping of Farrow et al. (1995). As  $R_{ex}$  has been eliminated from the analysis, three model-free models corresponding to  $tm1$ ,  $tm2$ , and  $tm5$  (Models 7.22.1, 7.22.2, and 7.22.5 on page 88) are employed. The model-free parameters are optimised using the reduced spectral density values and the best model is selected using F-tests. The spherical, spheroidal, and ellipsoidal diffusion tensors are obtained by linear least-squares fitting of the quadric model of Equation (7.35) using the local  $\tau_m$  values (Brüschweiler et al., 1995; Lee et al., 1997). The best diffusion model is selected via F-tests and refined by iterative elimination of spins systems with high chi-squared values. This tensor is used to calculate local  $\tau_m$  values for each spin system, approximating the multiexponential sum of the Brownian rotational diffusion correlation function with a single exponential, using the quadric model

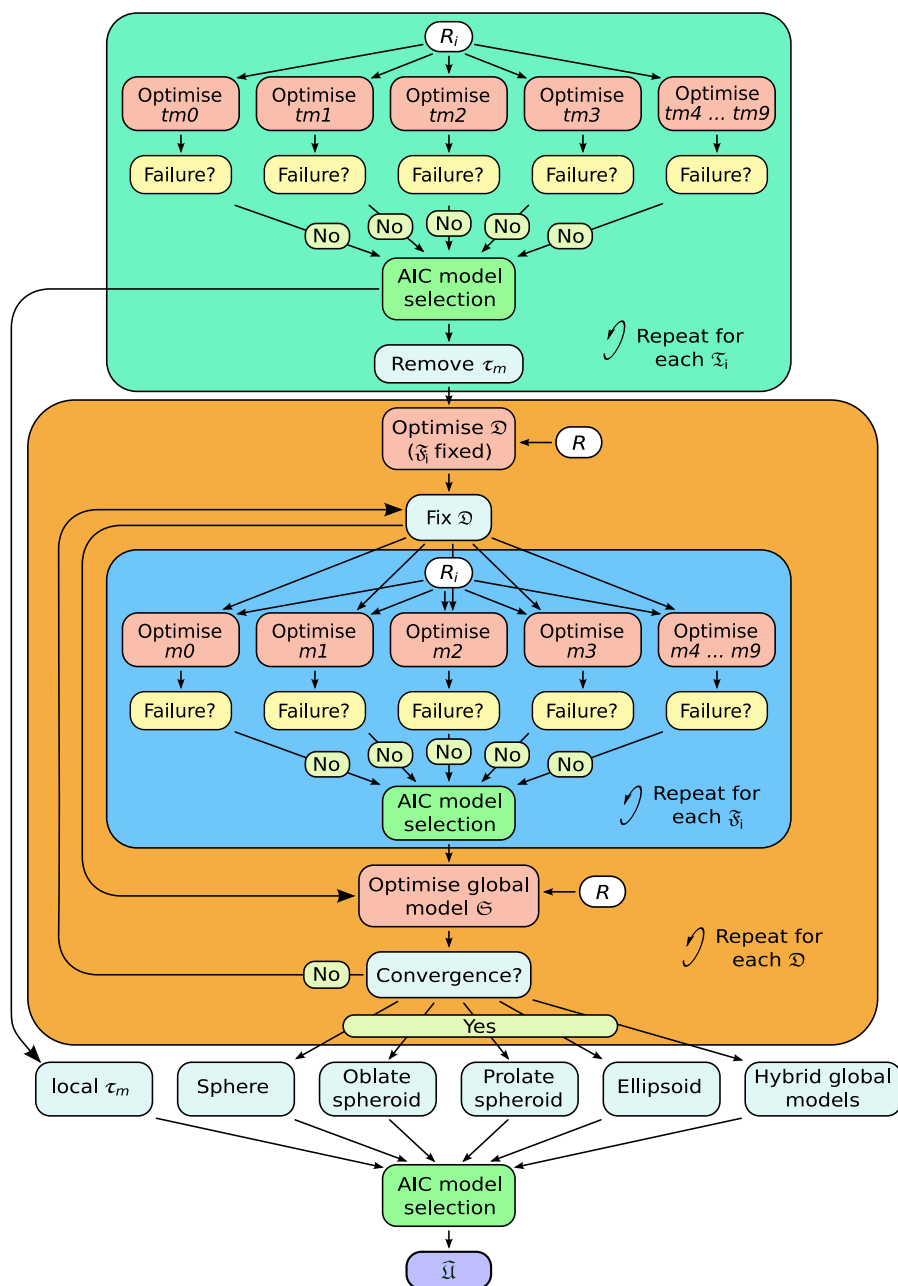


Figure 7.3: A schematic of the new model-free optimisation protocol. Initially models  $tm_0$  to  $tm_9$  (7.22.0–7.22.9) of the set  $\mathfrak{T}_i$  for each spin system  $i$  are optimised, model elimination used to remove failed models, and AIC model selection used to pick the best model. Once all the  $\mathfrak{T}_i$  have been determined for the system the the local  $\tau_m$  parameter is removed, the model-free parameters are held fixed, and the global diffusion parameters of  $\mathfrak{D}$  are optimised. These parameters are used as input for the central part of the schematic which follows the same procedure as that of Figure 7.2. Convergence is however precisely defined as identical models  $\mathfrak{S}$ , identical  $\chi^2$  values, and identical parameters  $\theta$  between two iterations. The universal solution  $\hat{\mathfrak{U}}$ , the best description of the dynamics of the molecule, is determined using AIC model selection to select between the local  $\tau_m$  models for all spins, the sphere, oblate spheroid, prolate spheroid, ellipsoid, and possibly hybrid models whereby multiple diffusion tensors have been applied to different parts of the molecule.

of Equation (7.35). In the final step of the protocol these  $\tau_m$  values are fixed and  $m1$ ,  $m2$ , and  $m5$  (Models 7.21.1, 7.21.2, and 7.21.5 on page 87) are optimised and the best model-free model selected using F-tests.

The new model-free protocol built into relax utilises the core foundation of the Butterwick et al. (2004) protocol yet its divergent implementation is designed to solve the universal equation of d’Auvergne and Gooley (2007) to find  $\hat{\mathfrak{U}}$  (Equation 7.36). Models  $tm0$  to  $tm9$  (7.22.0–7.22.9 on page 88) in which no global diffusion parameters exist are employed to significantly collapse the complexity of the problem. Model-free minimisation (d’Auvergne and Gooley, 2008a), model elimination (d’Auvergne and Gooley, 2006), and then AIC model selection (Akaike, 1973; d’Auvergne and Gooley, 2003) can be carried out in the absence of the influence of global parameters. By removing the local  $\tau_m$  parameter and holding the model-free parameter values constant these models can then be used to optimise the diffusion parameters of  $\mathfrak{D}$ . Model-free optimisation, model elimination, AIC model selection, and optimisation of the global model  $\mathfrak{S}$  is iterated until convergence. The iterations allow for sliding between different universes  $\mathfrak{S}$  to enable the collapse of model complexity, to refine the diffusion tensor, and to find the solution within the universal set  $\mathfrak{U}$ . The last step is the AIC model selection between the different diffusion models. Because the AIC criterion approximates the Kullback-Leibler discrepancy (Kullback and Leibler, 1951), central to the universal solution of Equation (7.36), it was chosen for all three model selection steps over BIC model selection (Schwarz, 1978; d’Auvergne and Gooley, 2003; Chen et al., 2004). The new protocol avoids the problem of under-fitting whereby artificial motions appear, avoids the problems involved in finding the initial diffusion tensor within  $\mathfrak{D}$ , and avoids the problem of hidden internal nanosecond motions and the inability to slide between universes to get to  $\hat{\mathfrak{U}}$  (see d’Auvergne and Gooley (2007) for more details). The full protocol is summarised in Figure 7.3.



## 7.8 The new protocol in the prompt/script UI mode

### 7.8.1 d'Auvergne protocol script mode – the sample script

The sample script for performing this new analysis is `sample_scripts/model_free/dauvergne_protocol.py`. The full script is replicated below. The docstring at the start of the script explains the practical implementation of the full protocol. If your copy of the `dauvergne_protocol.py` script taken from the same relax version as this manual does not match the text below, please contact the relax developers via the relax-devel mailing list (see section 3.2.3 on page 30). To use this script, copy it to a dedicated directory containing your PDB file and relaxation data files. The protocol will produce many files and directories, so it is best that these are placed within a dedicated and results directory. The contents of the script are:

```

1  """Script for black-box model-free analysis.
2
3  This script is designed for those who appreciate black-boxes or those who appreciate
    complex code. Importantly data at multiple magnetic field strengths is essential for
    this analysis. The script will need to be heavily tailored to the molecule in
    question by changing the variables just below this documentation. If you would like
    to change how model-free analysis is performed, the code in the class Main can be
    changed as needed. For a description of object-oriented coding in python using
    classes, functions/methods, self, etc., see the python tutorial.
4
5  If you have obtained this script without the program relax, please visit http://www.nmr-relax.com.
6
7
8  References
9  =====
10
11 The model-free optimisation methodology herein is that of:
12
13     d'Auvergne, E. J. and Gooley, P. R. (2008b). Optimisation of NMR dynamic models II. A
        new methodology for the dual optimisation of the model-free parameters and the
        Brownian rotational diffusion tensor. J. Biomol. NMR, 40(2), 121-133
14
15 Other references for features of this script include model-free model selection using
    Akaike's Information Criterion:
16
17     d'Auvergne, E. J. and Gooley, P. R. (2003). The use of model selection in the model-
        free analysis of protein dynamics. J. Biomol. NMR, 25(1), 25-39.
18
19 The elimination of failed model-free models and Monte Carlo simulations:
20
21     d'Auvergne, E. J. and Gooley, P. R. (2006). Model-free model elimination: A new step
        in the model-free dynamic analysis of NMR relaxation data. J. Biomol. NMR, 35(2),
        117-135.
22
23 Significant model-free optimisation improvements:
24
25     d'Auvergne, E. J. and Gooley, P. R. (2008a). Optimisation of NMR dynamic models I.
        Minimisation algorithms and their performance within the model-free and Brownian
        rotational diffusion spaces. J. Biomol. NMR, 40(2), 107-109.
26
27 Rather than searching for the lowest chi-squared value, this script searches for the model
    with the lowest AIC criterion. This complex multi-universe, multi-dimensional search
    is formulated using set theory as the universal solution:

```



```

28
29     d'Auvergne, E. J. and Gooley, P. R. (2007). Set theory formulation of the model-free
30     problem and the diffusion seeded model-free paradigm. 3(7), 483-494.
31
32 The basic three references for the original and extended model-free theories are:
33
34     Lipari, G. and Szabo, A. (1982a). Model-free approach to the interpretation of nuclear
35     magnetic-resonance relaxation in macromolecules I. Theory and range of validity. J.
36     Am. Chem. Soc., 104(17), 4546-4559.
37
38     Lipari, G. and Szabo, A. (1982b). Model-free approach to the interpretation of nuclear
39     magnetic-resonance relaxation in macromolecules II. Analysis of experimental results.
40     J. Am. Chem. Soc., 104(17), 4559-4570.
41
42     Clore, G. M., Szabo, A., Bax, A., Kay, L. E., Driscoll, P. C., and Gronenborn, A.M.
43     (1990). Deviations from the simple 2-parameter model-free approach to the
44     interpretation of N-15 nuclear magnetic-relaxation of proteins. J. Am. Chem. Soc.,
45     112(12), 4989-4991.
46
47
48 How to use this script
49 =====
50
51 The value of the variable DIFF_MODEL will determine the behaviour of this script. The
52 five diffusion models used in this script are:
53
54     Model I   (MI)   - Local tm.
55     Model II  (MII)  - Sphere.
56     Model III (MIII) - Prolate spheroid.
57     Model IV  (MIV)  - Oblate spheroid.
58     Model V   (MV)   - Ellipsoid.
59
60 Model I must be optimised prior to any of the other diffusion models, while the Models II
61 to V can be optimised in any order. To select the various models, set the variable
62 DIFF_MODEL to the following strings:
63
64     MI   - 'local_tm'
65     MII  - 'sphere'
66     MIII - 'prolate'
67     MIV  - 'oblate'
68     MV   - 'ellipsoid'
69
70 This approach has the advantage of eliminating the need for an initial estimate of a
71 global diffusion tensor and removing all the problems associated with the initial
72 estimate.
73
74 It is important that the number of parameters in a model does not exceed the number of
75 relaxation data sets for that spin. If this is the case, the list of models in the
76 MF_MODELS and LOCAL_TM_MODELS variables will need to be trimmed.
77
78
79 Model I - Local tm
80 ~~~~~
81
82 This will optimise the diffusion model whereby all spin of the molecule have a local tm
83 value, i.e. there is no global diffusion tensor. This model needs to be optimised
84 prior to optimising any of the other diffusion models. Each spin is fitted to the
85 multiple model-free models separately, where the parameter tm is included in each
86 model.
87
88
89 AIC model selection is used to select the models for each spin.

```

## Model II - Sphere

This will optimise the isotropic diffusion model. Multiple steps are required, an initial optimisation of the diffusion tensor, followed by a repetitive optimisation until convergence of the diffusion tensor. Each of these steps requires this script to be rerun. For the initial optimisation, which will be placed in the directory './sphere/init/', the following steps are used:

The model-free models and parameter values for each spin are set to those of diffusion model MI.

The local tm parameter is removed from the models.

The model-free parameters are fixed and a global spherical diffusion tensor is minimised.

For the repetitive optimisation, each minimisation is named from 'round\_1' onwards. The initial 'round\_1' optimisation will extract the diffusion tensor from the results file in './sphere/init/', and the results will be placed in the directory './sphere/round\_1/'. Each successive round will take the diffusion tensor from the previous round. The following steps are used:

The global diffusion tensor is fixed and the multiple model-free models are fitted to each spin.

AIC model selection is used to select the models for each spin.

All model-free and diffusion parameters are allowed to vary and a global optimisation of all parameters is carried out.

## Model III - Prolate spheroid

The methods used are identical to those of diffusion model MII, except that an axially symmetric diffusion tensor with  $D_a \geq 0$  is used. The base directory containing all the results is './prolate/'.

## Model IV - Oblate spheroid

The methods used are identical to those of diffusion model MII, except that an axially symmetric diffusion tensor with  $D_a \leq 0$  is used. The base directory containing all the results is './oblate/'.

## Model V - Ellipsoid

The methods used are identical to those of diffusion model MII, except that a fully anisotropic diffusion tensor is used (also known as rhombic or asymmetric diffusion). The base directory is './ellipsoid/'.

## Final run

```

114
115 Once all the diffusion models have converged, the final run can be executed. This is done
    by setting the variable DIFF_MODEL to 'final'. This consists of two steps, diffusion
    tensor model selection, and Monte Carlo simulations. Firstly AIC model selection is
    used to select between the diffusion tensor models. Monte Carlo simulations are then
    run solely on this selected diffusion model. Minimisation of the model is bypassed as
    it is assumed that the model is already fully optimised (if this is not the case the
    final run is not yet appropriate).
116
117 The final black-box model-free results will be placed in the file 'final/results'.
118 """
119
120 # Python module imports.
121 from time import asctime, localtime
122
123 # relax module imports.
124 from auto_analyses.dauvergne_protocol import dAuvergne_protocol
125
126
127 # Analysis variables.
128 #####
129
130 # The diffusion model.
131 DIFF_MODEL = 'local_tm'
132
133 # The model-free models. Do not change these unless absolutely necessary, the protocol is
    likely to fail if these are changed.
134 MF_MODELS = ['m0', 'm1', 'm2', 'm3', 'm4', 'm5', 'm6', 'm7', 'm8', 'm9']
135 LOCAL_TM_MODELS = ['tm0', 'tm1', 'tm2', 'tm3', 'tm4', 'tm5', 'tm6', 'tm7', 'tm8', 'tm9']
136
137 # The grid search size (the number of increments per dimension).
138 GRID_INC = 11
139
140 # The optimisation technique.
141 MIN_ALGOR = 'newton'
142
143 # The number of Monte Carlo simulations to be used for error analysis at the end of the
    analysis.
144 MC_NUM = 500
145
146 # Automatic looping over all rounds until convergence (must be a boolean value of True or
    False).
147 CONV_LOOP = True
148
149
150
151 # Set up the data pipe.
152 #####
153
154 # The following sequence of user function calls can be changed as needed.
155
156 # Create the data pipe.
157 pipe_bundle = "mf (%s)" % asctime(localtime())
158 name = "origin - " + pipe_bundle
159 pipe.create(name, 'mf', bundle=pipe_bundle)
160
161 # Load the PDB file.
162 structure.read_pdb('1f3y.pdb', set_mol_name='Ap4Aase', read_model=3)
163
164 # Set up the 15N and 1H spins (both backbone and Trp indole sidechains).
165 structure.load_spins('@N', ave_pos=True)

```

```

166 structure.load_spins('@NE1', ave_pos=True)
167 structure.load_spins('@H', ave_pos=True)
168 structure.load_spins('@HE1', ave_pos=True)
169 spin.isotope('15N', spin_id='@N*')
170 spin.isotope('1H', spin_id='@H*')
171
172 # Set up the 15N spins (alternative to the structure-based approach).
173 #sequence.read(file='noe.500.out', dir=None, mol_name_col=1, res_num_col=2, res_name_col
    =3, spin_num_col=4, spin_name_col=5)
174 #spin.element(element='N', spin_id='@N*')
175 #spin.isotope('15N', spin_id='@N*')
176
177 # Generate the 1H spins for the magnetic dipole-dipole relaxation interaction (alternative
    to the structure-based approach).
178 #sequence.attach_protons()
179
180 # Load the relaxation data.
181 relax_data.read(ri_id='R1_600', ri_type='R1', frq=599.719*1e6, file='r1.600.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
182 relax_data.read(ri_id='R2_600', ri_type='R2', frq=599.719*1e6, file='r2.600.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
183 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=599.719*1e6, file='noe.600.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
184 relax_data.read(ri_id='R1_500', ri_type='R1', frq=500.208*1e6, file='r1.500.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
185 relax_data.read(ri_id='R2_500', ri_type='R2', frq=500.208*1e6, file='r2.500.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
186 relax_data.read(ri_id='NOE_500', ri_type='NOE', frq=500.208*1e6, file='noe.500.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
187
188 # Deselect spins to be excluded (including unresolved and specifically excluded spins).
189 deselect.read(file='unresolved', dir=None, spin_id_col=None, mol_name_col=1, res_num_col
    =2, res_name_col=3, spin_num_col=4, spin_name_col=5, sep=None, spin_id=None, boolean='
    AND', change_all=False)
190 deselect.read(file='exclude', spin_id_col=1)
191
192 # Define the magnetic dipole-dipole relaxation interaction.
193 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
194 interatom.define(spin_id1='@NE1', spin_id2='@HE1', direct_bond=True)
195 interatom.set_dist(spin_id1='@N*', spin_id2='@H*', ave_dist=1.02 * 1e-10)
196 interatom.unit_vectors()
197
198 # Define the chemical shift relaxation interaction.
199 value.set(-172 * 1e-6, 'csa', spin_id='@N*')
200
201
202
203 # Execution.
204 #####
205
206 # Do not change!
207 dAuvergne_protocol(pipe_name=name, pipe_bundle=pipe_bundle, diff_model=DIFF_MODEL,
    mf_models=MF_MODELS, local_tm_models=LOCAL_TM_MODELS, grid_inc=GRID_INC, min_algor=
    MIN_ALGOR, mc_sim_num=MC_NUM, conv_loop=CONV_LOOP)

```

### 7.8.2 d’Auvergne protocol script mode – analysis variables

At the start of the script you will notice a number of **Analysis variables**. Unless you know what you are doing, you should only change the `DIFF_MODEL` variable to the following:

**‘local\_tm’:** This is the first diffusion model which must be optimised prior to optimising any of the other diffusion models. It consists of the local  $\tau_m$  models (equations 7.22.0 to 7.22.9 on page 88).

**‘sphere’:** This second diffusion model is that of isotropic Brownian diffusion.

**‘prolate’:** This third diffusion model is that of the prolate axially-symmetric rotor.

**‘oblate’:** This fourth diffusion model is that of the oblate axially-symmetric rotor.

**‘ellipsoid’:** This fifth diffusion model is that of fully rhombic Brownian diffusion (see Perrin (1934, 1936) for the original theory).

**‘final’:** This is a special value which will finalise the analysis by selecting the best diffusion model to describe your system and to perform Monte Carlo simulations for error propagation.

The `MF_MODELS` and `LOCAL_TM_MODELS` variables specify which model-free models will be used in the analysis. But, as the full protocol behind this script which is designed to find the solution of the universal set  $\mathfrak{U}$  (see section 7.7.2 on page 100) expects that all these models are present, you should not change these variables. If you do remove some model-free models, you should fully expect to see artificial motions which you will not be able to distinguish from the real molecular motions.

The next variables `GRID_INC` and `MIN_ALGOR` are related to the optimisation of the model-free models. These should also not be touched unless you fully understand the consequences (and have read d’Auvergne and Gooley (2008a)). The variable `MC_NUM` specifies the number of Monte Carlo simulations. This number can be increased but, for realistic parameter errors in your publication, it should not set lower than 500 simulations.

Finally the `CONV_LOOP` variable is designed to make your life easier. If left at the value of `True`, the script will iterate until convergence (see Figure 2 in d’Auvergne and Gooley (2008b) to understand this concept). If changed to `False`, then you will need to run the script manually for the 15 or so iterations of each diffusion model, and then repeat this for all diffusion models II to V.

### 7.8.3 d’Auvergne protocol script mode – data pipe initialisation

The next part of the script between the **Analysis variables** and execution sets up a data pipe with all of the spin information and relaxation data to pass into the automated protocol. The data pipe is created in the lines:

```
156 # Create the data pipe.
157 pipe_bundle = "mf (%s)" % asctime(localtime())
158 name = "origin - " + pipe_bundle
159 pipe.create(name, 'mf', bundle=pipe_bundle)
```

Firstly a data pipe bundle name is created containing the date and time at the point the script is first executed. This pipe bundle is used to group together all of the data pipes created automatically by the protocol. See section 4.2.1 on page 34 for more details.

The data pipe name used for this initial setup is set to `origin - mf (x)` where `x` is the date and time again. This name is unique and will not clash with the data pipes created within the protocol. The `pipe.create` command will create the data pipe and add it to a new pipe bundle.

#### 7.8.4 d’Auvergne protocol script mode – setting up the spin systems

To see how to set up the spin system data in all possible situations, please see Chapter 4 for a thorough description. Here two different methods are presented. The first is by extracting the spins from a PDB file which is first loaded with:

```
161 # Load the PDB file.
162 structure.read_pdb('1f3y.pdb', set_mol_name='Ap4Aase', read_model=3)
```

This will read the 3<sup>rd</sup> model from the 1F3Y PDB file and name the single molecule as ‘Ap4Aase’. The <sup>15</sup>N and <sup>1</sup>H spins for the backbone and tryptophan indole sidechain are extracted from the structure with the user functions:

```
164 # Set up the 15N and 1H spins (both backbone and Trp indole sidechains).
165 structure.load_spins('@N', ave_pos=True)
166 structure.load_spins('@NE1', ave_pos=True)
167 structure.load_spins('@H', ave_pos=True)
168 structure.load_spins('@HE1', ave_pos=True)
```

As the PDB file does not contain isotope information, this is set with the user functions:

```
169 spin.isotope('15N', spin_id='@N*')
170 spin.isotope('1H', spin_id='@H*')
```

The spin ID ‘@N\*’ uses regular expression and will match both the ‘N’ and ‘NE1’ spins.

The alternative approach is if a structure is missing. This is the commented out code:

```
172 # Set up the 15N spins (alternative to the structure-based approach).
173 sequence.read(file='noe.500.out', dir=None, mol_name_col=1, res_num_col=2, res_name_col=3,
174               spin_num_col=4, spin_name_col=5)
175 spin.element(element='N', spin_id='@N*')
176 spin.isotope('15N', spin_id='@N*')
177 # Generate the 1H spins for the magnetic dipole-dipole relaxation interaction (alternative
178   to the structure-based approach).
179 sequence.attach_protons()
```

To use this, you will need to place comments (the # character) in front of the previous `structure.read_pdb`, `structure.load_spins` and `spin.isotope` user functions. Then uncomment the `sequence.read`, `spin.element`, `spin.isotope` and `sequence.attach_protons` user functions. The <sup>15</sup>N spins will be extracted from the `noe.500.out` file. The `spin.element` and `spin.isotope` user functions set the information required for relax to understand which relaxation mechanisms are active. Finally the `sequence.attach_protons` user function will automatically attach protons to all nitrogen spin systems. As

this method is devoid of atomic positional information, the N-H bonds are absent and the diffusion models requiring structural information (the spheroids and ellipsoid) must be skipped.

### 7.8.5 d'Auvergne protocol script mode – loading the data

The next step is to load the relaxation data for each spin system. The sample script assumes that the NOE,  $R_1$  and  $R_2$  data was generated using relax. One of the six user function calls is:

```
180 # Load the relaxation data.
181 relax_data.read(ri_id='R1_600', ri_type='R1', frq=599.719*1e6, file='r1.600.out',
    mol_name_col=1, res_num_col=2, res_name_col=3, spin_num_col=4, spin_name_col=5,
    data_col=6, error_col=7)
```

This pattern is repeated for all of the relaxation data files loaded. The important points are that each relaxation data set must have its own unique identification string (`ri_id`), the relaxation data type specified (`ri_type`) and the frequency in Hertz (not MHz) specified. Note that the frequency must be the exact value – see the `sfrq` parameter in the Varian `procp` file or the `SF01` parameter in the Bruker `acqus` file.

### 7.8.6 d'Auvergne protocol script mode – deselection

The sample script now presents the deselection of spins using two different files:

```
188 # Deselect spins to be excluded (including unresolved and specifically excluded spins).
189 deselect.read(file='unresolved', dir=None, spin_id_col=None, mol_name_col=1, res_num_col
    =2, res_name_col=3, spin_num_col=4, spin_name_col=5, sep=None, spin_id=None, boolean='
    AND', change_all=False)
190 deselect.read(file='exclude', spin_id_col=1)
```

The `unresolved` file contains a list of spins which are unresolved in all spectra. If `relax` has been used for calculating the NOE and fitting the relaxation curves, then this step is not needed as the relaxation data files will not have any data for the spins deselected in those analyses. The second file `exclude` is a list of spin ID strings (see section 4.2.2 on page 36) of spins that for which ever reason are to be excluded from the analysis.

### 7.8.7 d'Auvergne protocol script mode – relaxation interactions

The next step is to fully specify all of the relaxation interactions active on the spins of interest. Firstly the magnetic dipole-dipole interaction is defined between directly bonded nitrogens and protons:

```
192 # Define the magnetic dipole-dipole relaxation interaction.
193 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
194 interatom.define(spin_id1='@NE1', spin_id2='@HE1', direct_bond=True)
195 interatom.set_dist(spin_id1='@N*', spin_id2='@H*', ave_dist=1.02 * 1e-10)
196 interatom.unit_vectors()
```

The regular expression '@N\*' and '@H\*' cannot be used with the `dipole_pair`. define user function as otherwise @N spins will be connected to @HE1 spins of the same tryptophan residue and @H spins to @NE1 spins. The average interatomic distance is set to 1.02 Ångstrom (though the `dipole_pair.set_dist` user function expects the units of meters). The `dipole_pair.unit_vectors` is used to calculate the averaged unit vector between the two atoms.

Secondly the chemical shift anisotropy (CSA) relaxation mechanism is defined via the single command:

```
198 # Define the chemical shift relaxation interaction.
199 value.set(-172 * 1e-6, 'csa', spin_id='@N*')
```

If your system does not experience CSA relaxation, the value can be set to zero.

### 7.8.8 d'Auvergne protocol script mode – execution

Once the data is set up and you have modified your script to match your analysis needs, then the data pipe, pipe bundle and analysis variables are passed into the `dAuvergne_protocol` class. This is the final line of the script:

```
203 # Execution.
204 #####
205
206 # Do not change!
207 dAuvergne_protocol(pipe_name=name, pipe_bundle=pipe_bundle, diff_model=DIFF_MODEL,
    mf_models=MF_MODELS, local_tm_models=LOCAL_TM_MODELS, grid_inc=GRID_INC, min_algor=
    MIN_ALGOR, mc_sim_num=MC_NUM, conv_loop=CONV_LOOP)
```

This script needs to be executed multiple times, once for each of the diffusion models. For example if the `DIFF_MODEL` variable is set to 'ellipsoid', you can run relax with:

```
$ relax --tee log.ellipsoid dauvergne_protocol.py
```

You should use a different log file for each diffusion model, though relax will prevent you from overwriting an old log file. Note that the `log.*` files for each diffusion model may end up being a few gigabytes in size.

For a full analysis of a protein system, the analysis may require between one to two weeks to complete. This can be speed up using Gary Thompson's multi-processor code (see section 1.3 on page 17). The analysis is performed as described in the previous sections and summarised in Figure 7.3. If you are curious, the implementation is within a very large relax script called `auto_analyses/dauvergne_protocol.py` (which must never be changed). This automatic analysis script hides all of the complexity of the full protocol from the sample script.



## 7.9 The new protocol in the GUI

A model-free analysis can be performed within the GUI (see Figure 1.8 on page 18). This analysis is that of the fully automated d’Auvergne protocol which can be chosen via the analysis selection wizard (Figure 1.4 on page 12). Please see Section 7.7 on page 97 for a description of this new model-free protocol.

The GUI is designed to be robust – you should be able to set up all the input data and parameters in any order with relax returning you warnings if something is missing. The analysis will only execute once everything is correctly set up. If this is not the case, clicking on the “Execute relax” button will display a warning window explaining what the issue is rather than initialising the analysis. Despite the self-explanatory nature of the GUI a tutorial on how to use the GUI, with screenshots, will be presented below.

If the “Protocol mode” field is left to the “Fully automated” setting then, after clicking on “Execute relax”, the calculation can be left to complete. It is highly recommended to check the log messages in the relax controller window, at least at the start of the analysis, to make sure that all the data is being read correctly and everything is set up as desired. All warnings should be carefully checked as these can indicate a fatal problem. If you would like to log all the messages into a file, relax can be run with:

```
$ relax -g --log log
```

Note that the size of this log file could end up being in the gigabyte range for a model-free analysis.

For the full analysis to complete, for a protein system this may take about a week. Depending on the nature of the problem and the speed of the computer, the calculation time may be significantly shorter or longer. To speed up the calculations, if you have access to multiple cores and/or hyper-threading, the GUI can be run using Gary Thompson’s multi-processor framework (see section 1.3 on page 17). For example on a dual-core, dual-CPU system, four calculations can be run simultaneously. In this case, the GUI can be launched with:

```
$ mpirun -np 5 /usr/local/bin/relax --multi='mpi4py' --gui --log log
```

This assumes that OpenMPI and the Python mpi4py module have been installed on your system, and relax is installed into the `/usr/local/bin/` directory. If this is successful, you should only see a single relax GUI window (and not five windows) and in the relax controller, you should see text similar to:

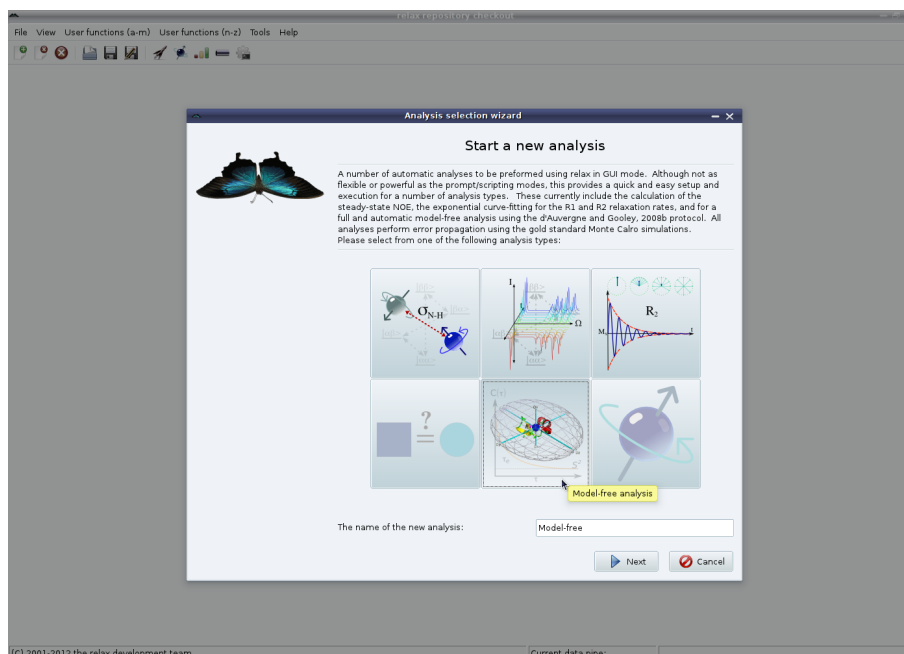
```
Processor fabric: MPI 2.1 running via mpi4py with 4 slave processors & 1 master. Using
Open MPI 1.4.3.
```

If you are using a different MPI implementation, please see the documentation of that implementation to see how to launch a program in MPI mode. Finally as the calculation takes so long, we will run the calculations at a lower priority so that the computer is not slowed down too much and remains responsive. Therefore this model-free GUI analysis tutorial will be launched with the full command:

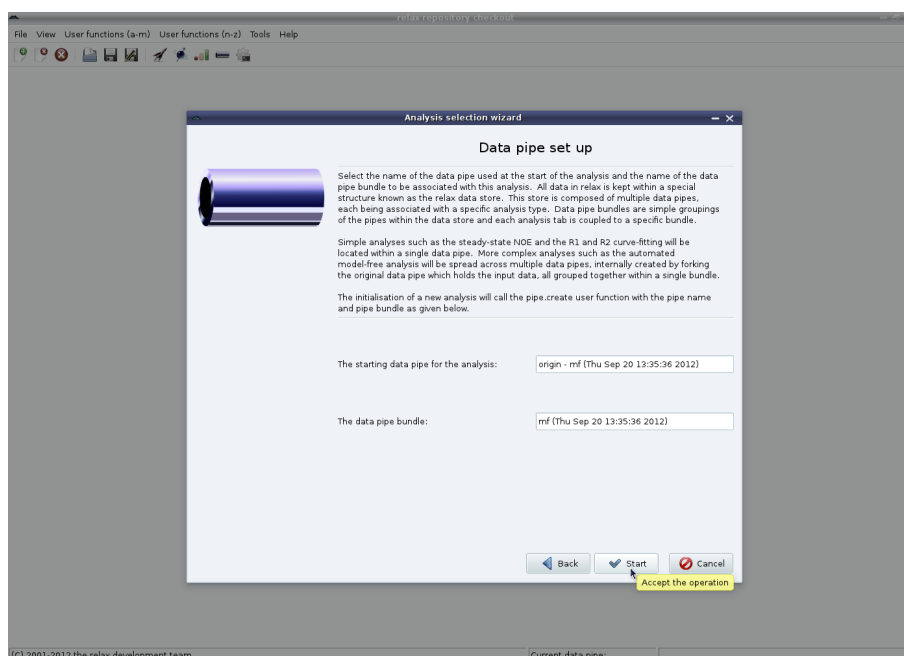
```
$ nice -n 15 mpirun -np 5 /usr/local/bin/relax --multi='mpi4py' --gui --log log
```

### 7.9.1 d'Auvergne protocol GUI mode – data pipe initialisation

First launch the analysis selection wizard (see Figure 1.4 on page 12) and click on the model-free analysis button.

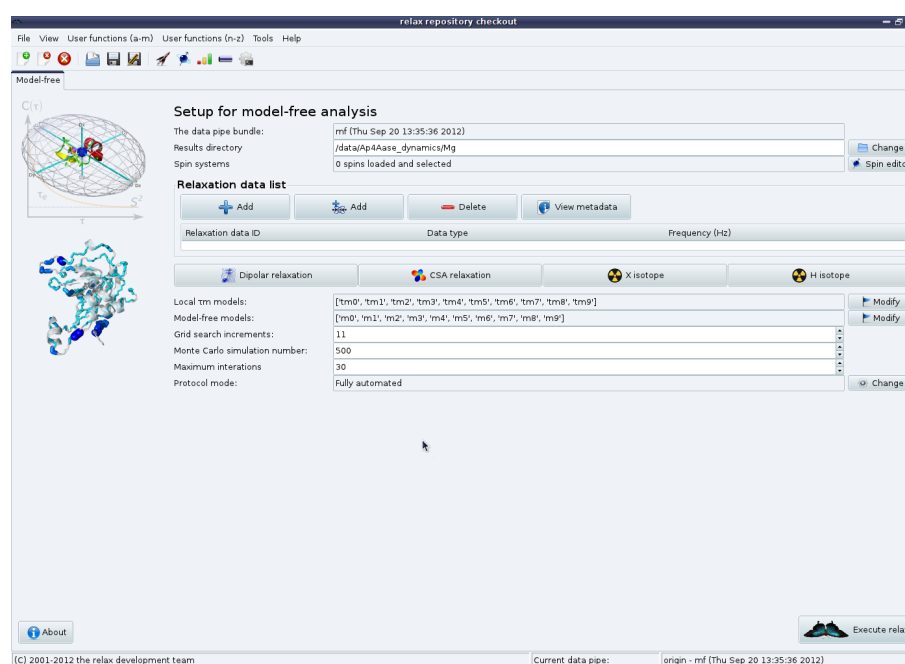


Click on the “Next” button and on the second page click on the “Start” button. The text in the second page need not be changed.

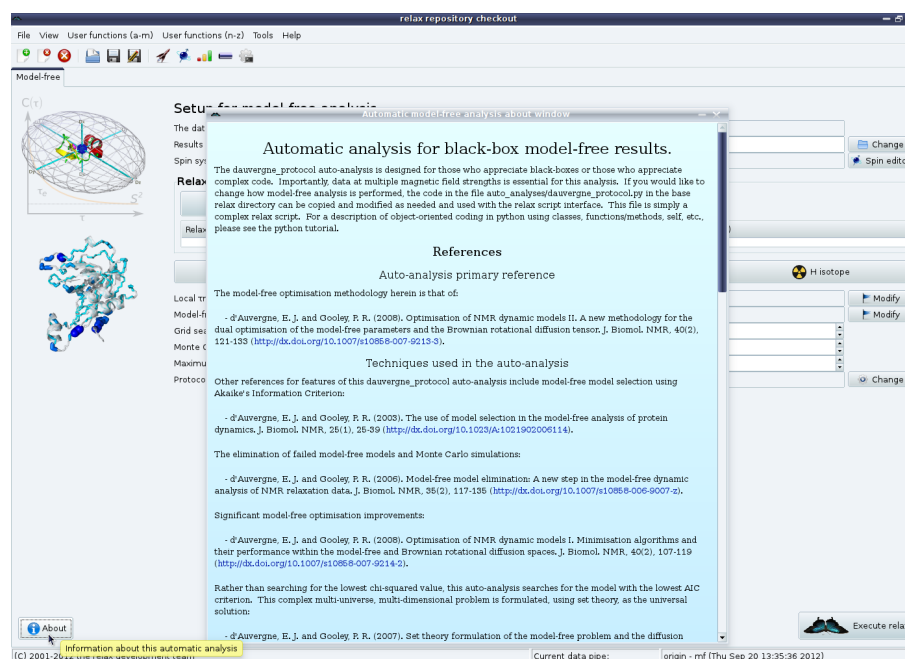


### 7.9.2 d'Auvergne protocol GUI mode – general setup

Once the analysis is initialised, the screen should look like:



The “About” button in the bottom left will bring up a window with the same description as given in the sample script:



At this point, back in the main relax window, the results directory where all of the output files and directories will be saved can be changed.

### 7.9.3 d’Auvergne protocol GUI mode – setting up the spin systems

The model-free dynamics is at the level of the spins – relaxation affects individual nuclei. In the main model-free tab you will see the “Spin systems” GUI element. Clicking on the “Spin editor” button to the right of this element will launch the spin editor window.

In this tutorial, the 3<sup>rd</sup> model of the PDB file 1f3y.pdb will be used to extract the spin system information. The molecule will be named “Ap4Aase”. For details on how to create the spin containers necessary for this analysis, please see section 4.5.2 on page 40 (or analyses lacking structural data in section 4.5.3 on page 43 for sequence files).

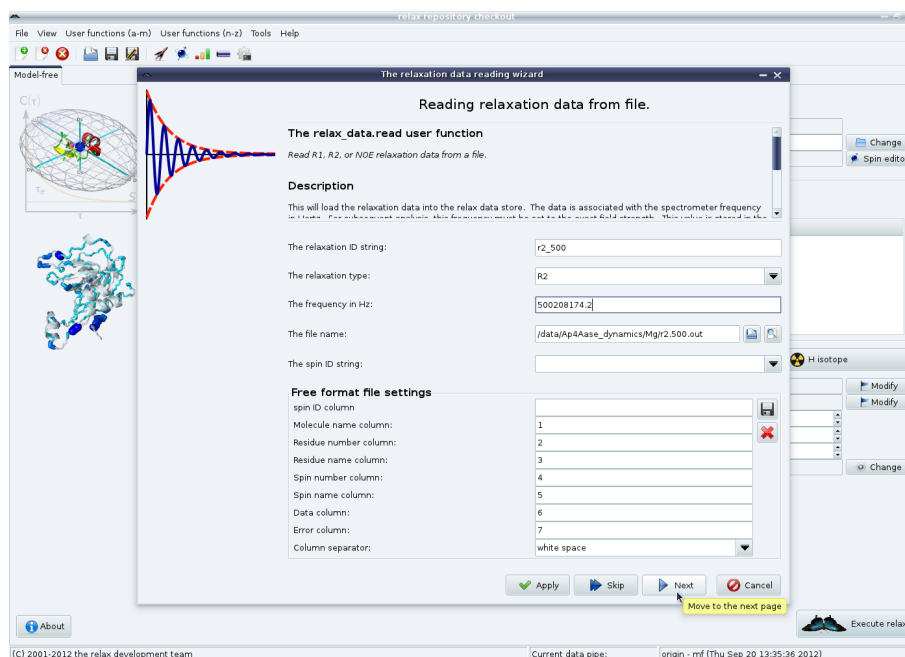
Note that for this tutorial, the protein backbone spins “@N” and “@H” as well as the tryptophan sidechain indole “@NE1” and “@HE1” spins should be loaded in the spin viewer window.

### 7.9.4 d’Auvergne protocol GUI mode – unresolved spins

To deselect all unwanted spins, please read section 4.5.5 on page 44 for all the necessary instructions for how to do this in the GUI.

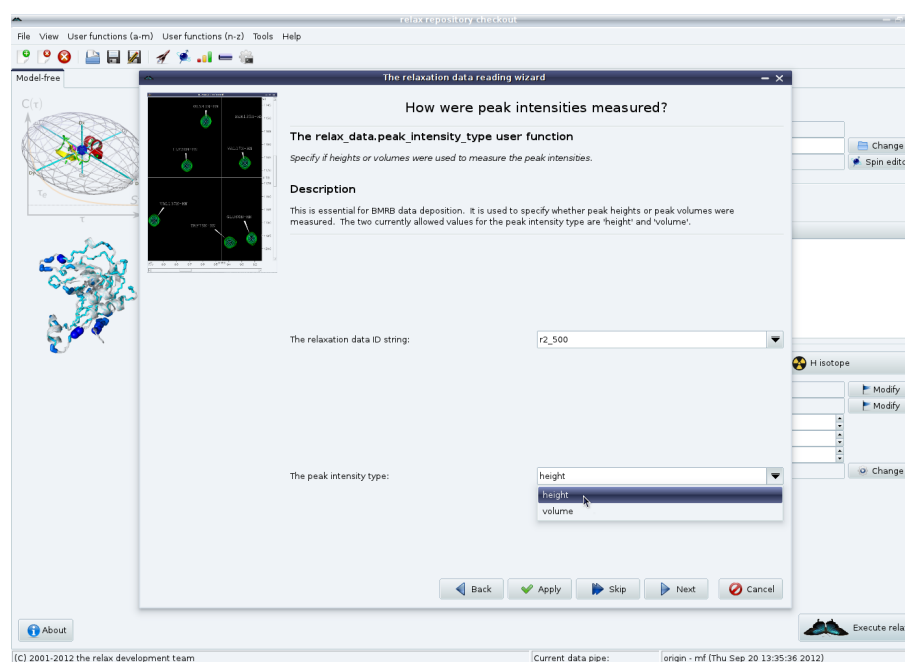
### 7.9.5 d’Auvergne protocol GUI mode – loading the data

The relaxation data can either come from plain columnar formatted text files (such as if relax was used for the NOE,  $R_1$  and  $R_2$  analyses) or from the Bruker Dynamics Centre. For the former, click on the “Add” button in the “Relaxation data list” GUI element. This route will be used for this tutorial. For the later, click on the “Add Bruker” button. After clicking on “Add”, you will see the relaxation data loading wizard:

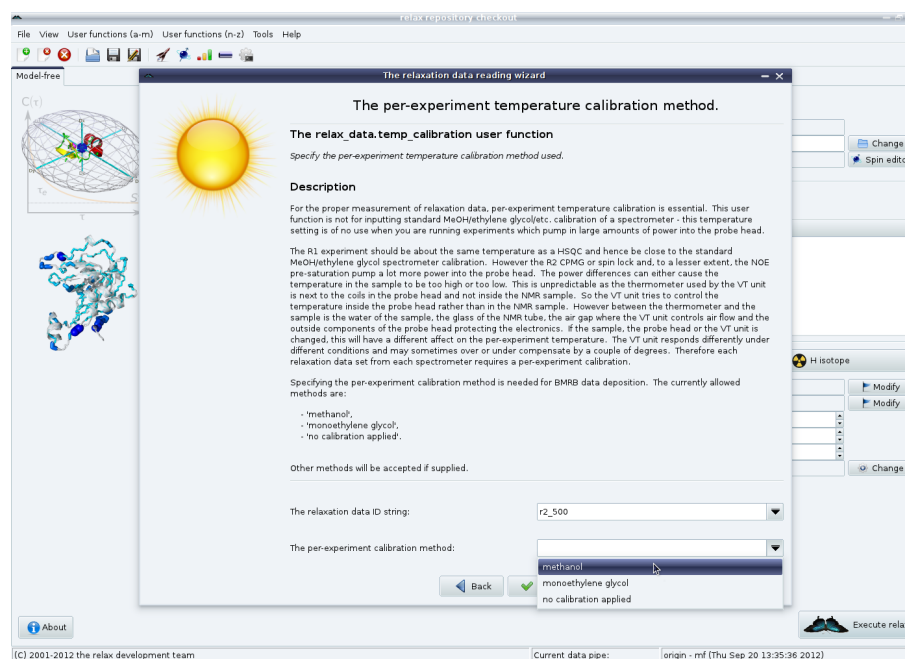


In this first page, the unique relaxation data identification string (“r2.500”), the relaxation data type (“R2”), the frequency in Hertz (“500208174.2”) and the file (“r2.500.out”) are specified. If your data comes from another program, you may need to change the values in the “Free format file settings” element. Click on “Next” to load the data from the file.

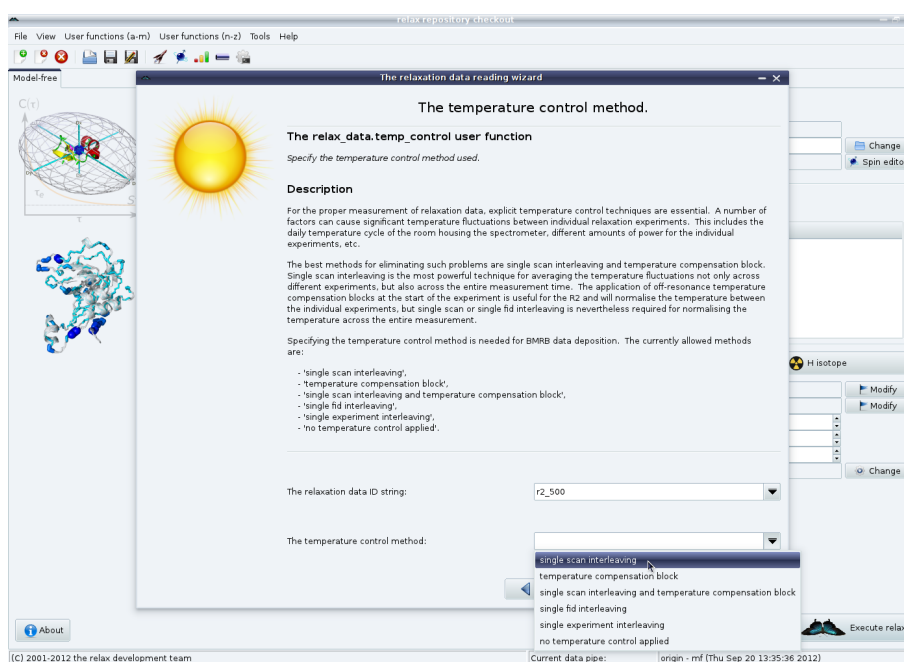
The next wizard pages are for loading the metadata which is used in the BioMagResBank deposition of your final results. The first is how the peak intensities were measured, either peak heights or volumes. Select the appropriate value, then click on “Next”.



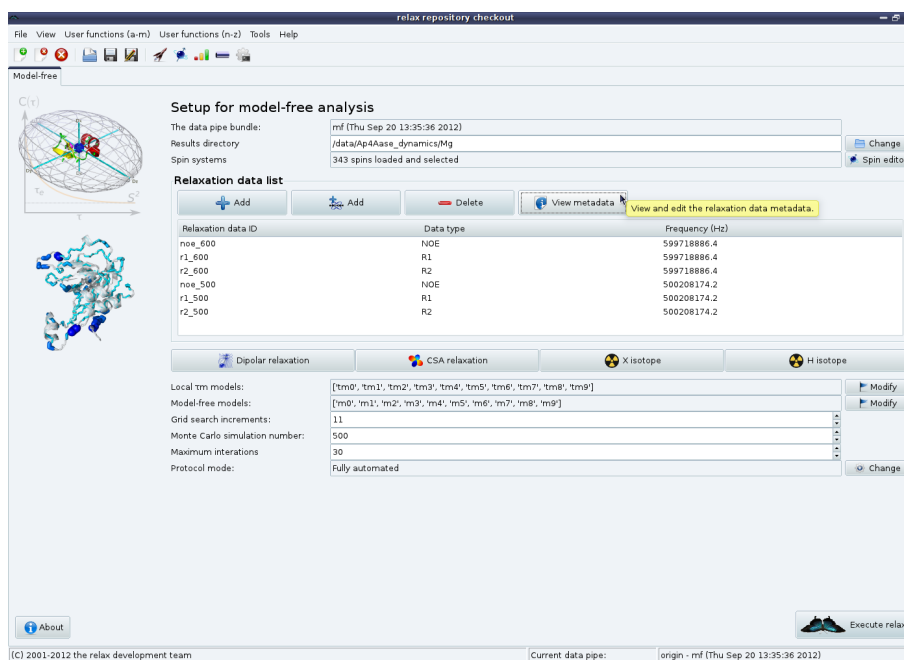
Then the temperature control method is given. For more details, please read the documentation provided in the wizard and see section 5.2.1 on page 50. Click on “Next” to continue.



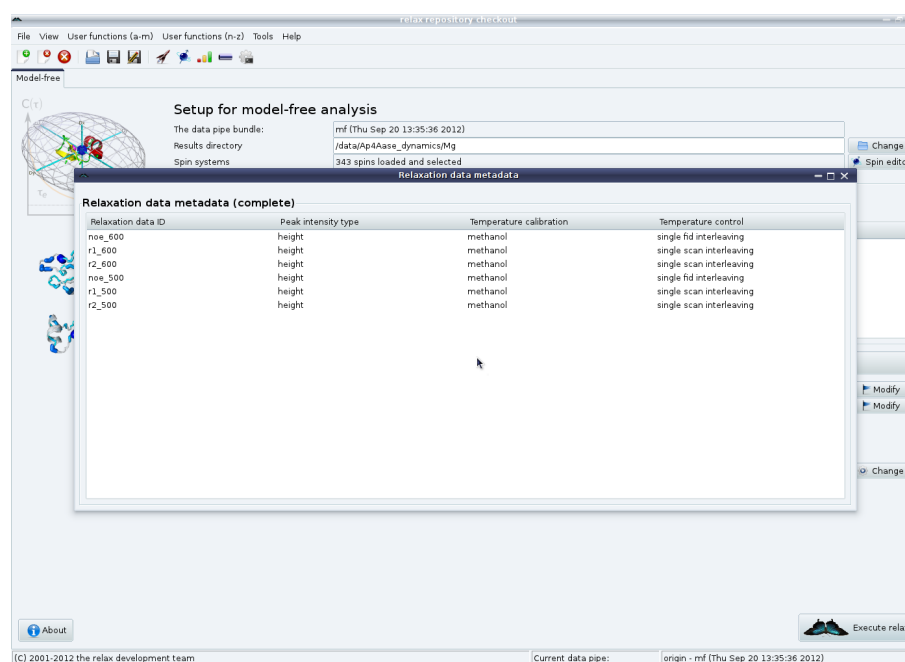
The temperature calibration method can finally be specified. Again, see section 5.2.1 on page 50 for the full details. Click on the “Finish” button to close the wizard.



After you have repeated this for the NOE,  $R_1$  and  $R_2$  at both 500 and 600 MHz, you should now see:

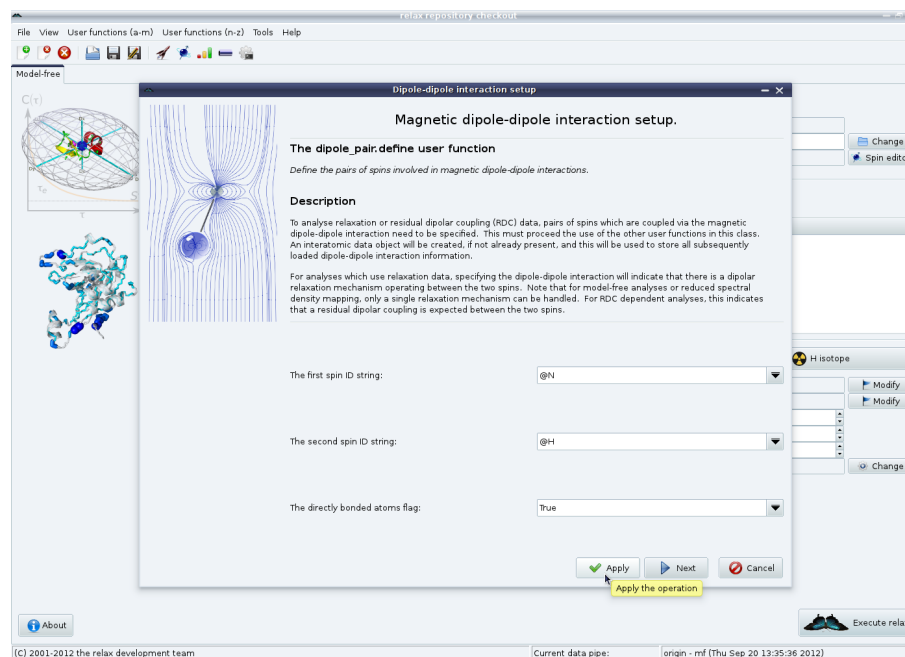


Check that the metadata has been properly entered by clicking on the “View metadata” button in the “Relaxation data list” GUI element:



### 7.9.6 d'Auvergne protocol GUI mode – relaxation interactions

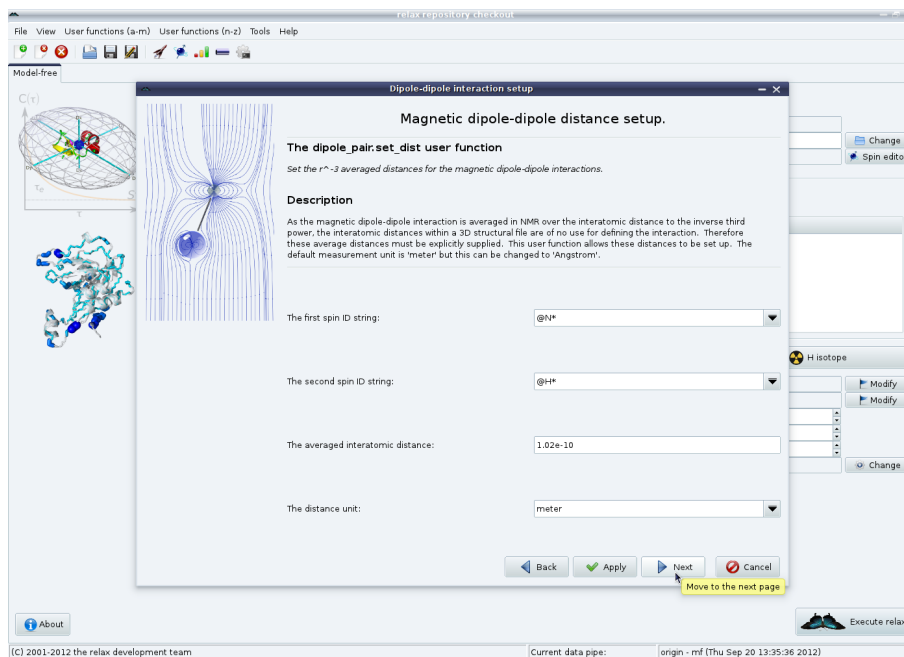
Just as in the scripting mode, the relaxation interactions need to now be defined. The first is the magnetic dipole-dipole interaction. All coupled nitrogen and proton spins should already be loaded at this point. Click on the “Dipolar relaxation” button in the model-free tab in the main relax window to launch the magnetic dipole-dipole interaction wizard:



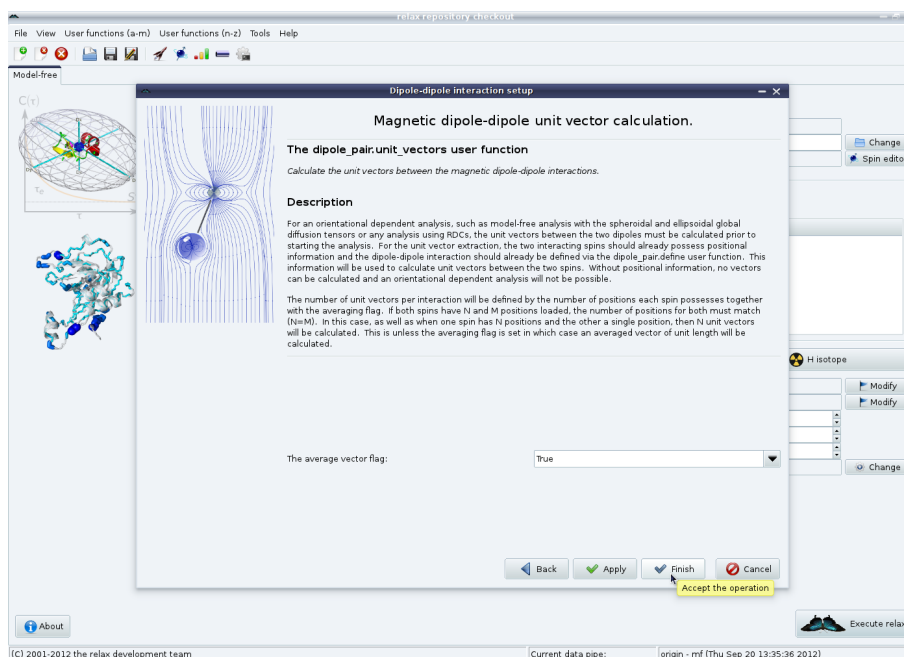
For this example, directly bonded nitrogens and protons will be analysed. To start with, the backbone NH pairs will be defined. Leave the values at “@N” and “@H” and click on the “Apply” button. Then change the two spin ID strings to “@NE1” and “@HE1” to set up the tryptophan sidechain indole NH pairs and click on the “Next” button. Note that

the regular expression “@N\*” and “@H\*” should not be used in this first wizard page as otherwise @N spins will be connected to @HE1 spins of the same tryptophan residue and @H spins to @NE1 spins.

Now the  $\langle r^{-3} \rangle$  averaged distance of 1.02 Å will be set. Leave all settings as they are and click on “Next”:

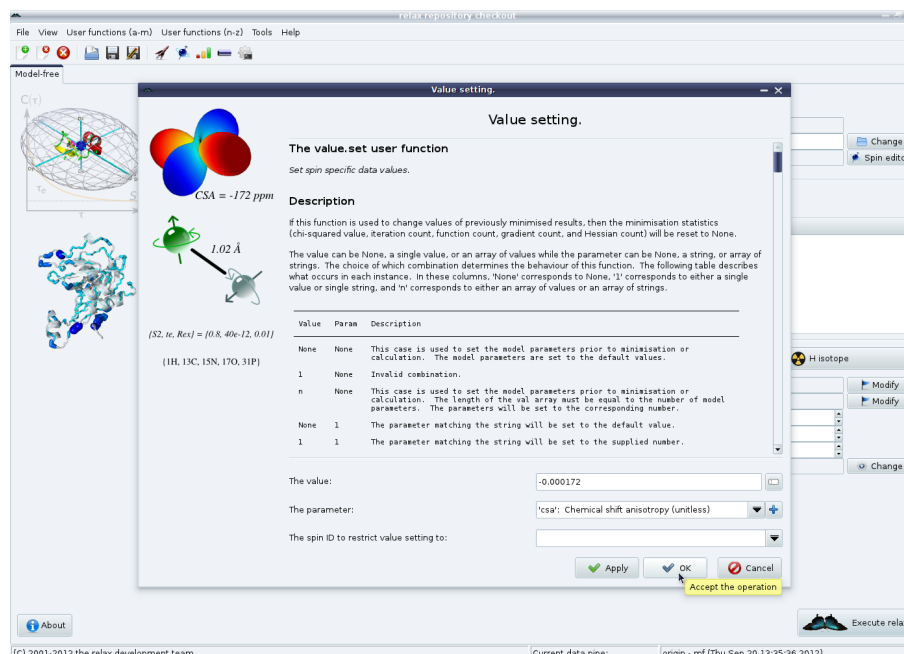


If multiple models have been loaded in the previous steps, then the unit vectors between each model need to be calculated. For a model-free analysis multiple unit vectors must be averaged to a single vector – current model-free theory is based on the assumption of a single vector orientation. Therefore the averaged vector flag must be left on “True”. Click on “Finish” to terminate the set up of the magnetic dipole-dipole interactions:



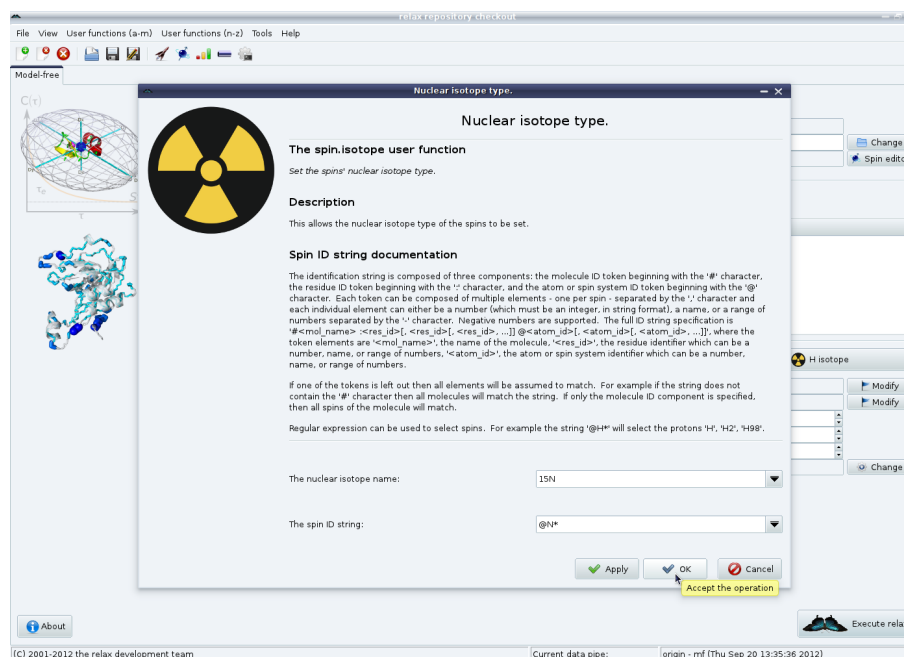


Secondly the chemical shift anisotropy (CSA) relaxation mechanism needs to be defined. Click on the “CSA relaxation” button in the model-free tab in the main relax window. An averaged CSA value of -172 ppm will be used for all spins, so simply click on “Ok” to finish.



### 7.9.7 d'Auvergne protocol GUI mode – spin isotopes

As the PDB file contains no isotope information, this needs to now be specified. First click on the “X isotope” button to set the nuclear isotope type of the heteronuclei:



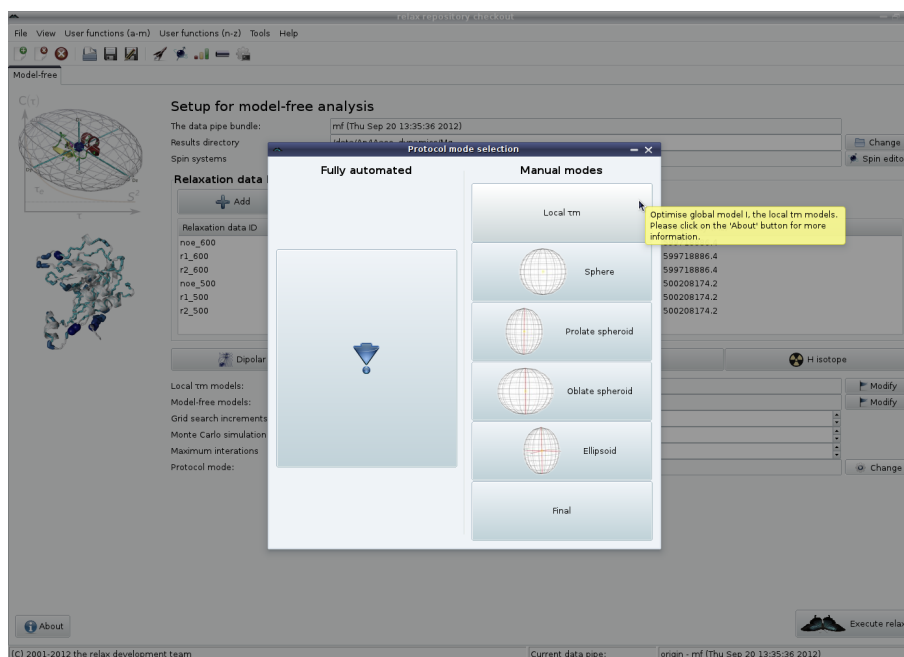
As nitrogen relaxation is being studied, the nuclear isotope name can be left as “15N” and the spin ID string to “@N\*”. Therefore simply click on the “Ok” button. Exactly the same

procedure can be used for the proton with the “H isotope” button.

### 7.9.8 d’Auvergne protocol GUI mode – the rest of the setup

The local  $\tau_m$  models and model-free models should not be modified, the reason for this is explained in section 7.8.2 on page 109. The grid search increments defaults to “11”. This is used in the optimisation of the individual model-free models for each spin. This value should also not be touched unless you know what you are doing (and have read [d’Auvergne and Gooley \(2008a\)](#)). The number of Monte Carlo simulations can be increased but, for accurate error estimates, it should not be less than 500 simulations. One additional setting is the “Maximum iterations”. This is a maximum number of times the protocol will iterate before terminating. This allows infinite loops to be broken. The value of 30 iterations should be fine for most analyses.

The “Protocol mode” GUI element setting of “Fully automated” will not be changed for the analysis of this tutorial. However if you are studying a system without a 3D structure, you can execute each individual component of the analysis by clicking on the “Change” button. This will make the protocol mode selection window appear:



From this you can first select the “Local  $\tau_m$ ” model, then the “Sphere” and finally the “Final” mode, clicking on “Execute relax” between each selection.

### 7.9.9 d’Auvergne protocol GUI mode – execution

Prior to executing relax, you should very carefully check the relax controller window for any strange messages, warnings or errors. You can open this window in three ways:

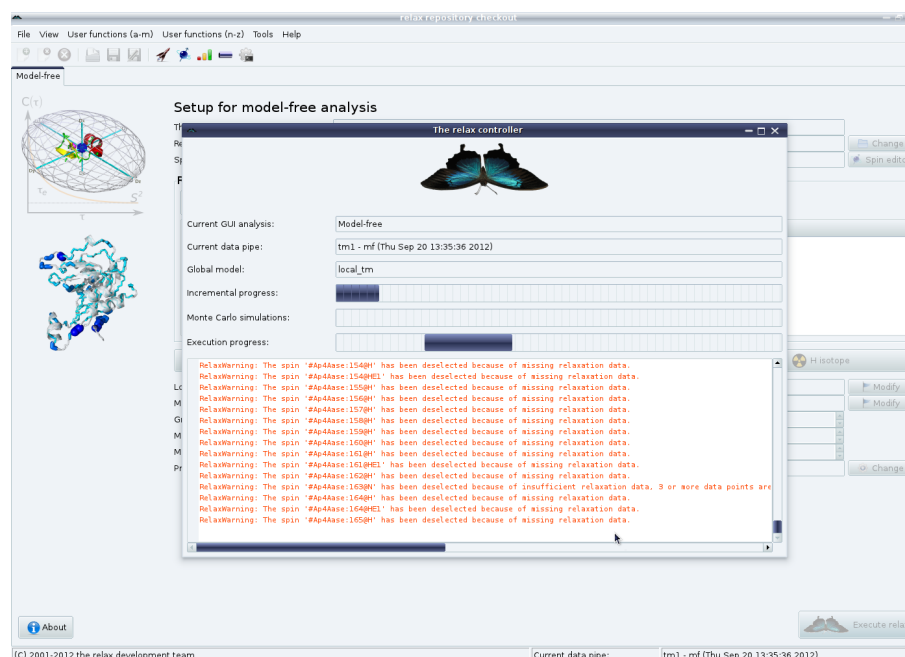
- Selecting the “View→Controller” menu item.

- Typing “[Ctrl+Z]” within the main relax window.
- Clicking on the “relax controller” button on the toolbar.

These messages are very important and will indicate to you if there are any problems prior to starting the very long model-free calculation. This information should be stored in the `log` file as well. As the execution of a fully iterative and complete model-free protocol takes a very long time to finish, it is advisable to save the current relax state. This will allow you restart the calculation without performing all of the steps detailed above. Just in case you cannot work out how to do this yourself, here is a list of the different ways you can do this (if this is not enough for you, please email the relax-users mailing list with your suggestions):

- Selecting the “File→Save relax state” menu item.
- Typing “[Ctrl+S]” within the main relax window.
- Clicking on the “Save relax state” button on the toolbar.
- Selecting the “File→Save as...” menu item.
- Typing “[Shift+Ctrl+S]” within the main relax window.
- Clicking on the “Save as” button on the toolbar.
- Selecting the “User functions→state→save” menu item.
- Opening up the relax prompt window with “View→relax prompt” or “[Ctrl+P]” and using the `state.save` user function.

If all the messages in the relax controller or `log` file appear to be fine and you have saved the current relax state, then click on “Execute relax”. This will start the calculations, freeze most of the GUI and open up the relax controller to give you feedback on the progress of the calculations:



At the start of the protocol, you should again check the messages carefully to be sure that relax is operating as you would expect. There may be very important **RelaxWarnings** that will require you to quit relax and start the analysis all over again.

### 7.9.10 d’Auvergne protocol GUI mode – completion

Upon completion of the analysis, the save and results files for the final result will be located in the **final** directory within the selected results directory. The results files will consist of text files for each of the spin specific model-free parameters, 2D Grace plots of the model-free parameters, PyMOL and MOLMOL macros for superimposing the model-free parameter values onto the 3D structure of the molecule, and a PDB representation of the final diffusion tensor.

Further visualisations of the results are possible via the “User functions” menu entry. For example to generate a 2D plot of order parameters for one of the other diffusion tensor results, the pipe editor window can be used to switch data pipes to the other diffusion models and then the “User functions→grace→write” menu item can be selected to create the plot.

### 7.9.11 d’Auvergne protocol GUI mode – BMRB deposition

Once you are ready to publish your results, the very last step of the model-free analysis is to create a NMR-STAR formatted file for [BioMagResBank](#) submission for each model-free analysis you perform. This can be accomplished using the BMRB export window. Simply select the “File→Export for BMRB deposition” menu item. You will then see the BMRB export window:

**BMRB export window**

**Data export for BMRB deposition**

This wizard will help in executing all of the relevant user functions required to convert the contents of the selected data pipe to the NMR-STAR format for deposition within the BioMagResBank. Note that this is currently only for the deposition of model-free analysis results or simple NMR relaxation data.

The data pipe to export: `origin - mf (Thu Sep 20 13:35:36)`

**Relaxation data metadata (complete)**

| Relaxation data ID | Peak intensity type | Temperature calibration | Temperature control      |
|--------------------|---------------------|-------------------------|--------------------------|
| noe_600            | height              | methanol                | single fid interleaving  |
| r1_600             | height              | methanol                | single scan interleaving |
| r2_600             | height              | methanol                | single scan interleaving |
| noe_500            | height              | methanol                | single fid interleaving  |
| r1_500             | height              | methanol                | single scan interleaving |
| r2_500             | height              | methanol                | single scan interleaving |

**Molecule information (incomplete)**

| ID string | Name    | Type | Thiol state |
|-----------|---------|------|-------------|
| #Ap4Aase  | Ap4Aase |      |             |

**Software**

| Program name |
|--------------|
| relax        |

**Scripts**

| Script name |
|-------------|
|-------------|

**Citations**

| Citation ID |
|-------------|
| relax_ref1  |
| relax_ref2  |

Buttons: Add, Select, Add, Add, Preview, Export, Preview the NMR-STAR formatted data.

From here you can complete the relaxation data metadata if needed, set up all the molecule information needed for a BMRB deposition, specify the software you have used running up

to the model-free analysis and any spectral processing or relax scripts you have used. You can also add as many citations relevant to your analysis as you wish. The NMR-STAR formatted file can be previewed in the relax controller window via the “Preview” button and the final file created using the “Export” button.

Once you are in the stage of writing up, simply go to the ADIT-NMR webpage at <http://deposit.bmrwisc.edu/bmrw-adit/>, create a new BMRB deposition, upload the file you have created, complete the deposition as needed, and add the BMRB deposition number to your paper.



## Chapter 8

# Reduced spectral density mapping

### 8.1 Introduction to reduced spectral density mapping

The reduced spectral density mapping analysis is often performed when the system under study is not suitable for model-free analysis, or as a last resort if a model-free analysis fails. The aim is to convert the relaxation data into three  $J(\omega)$  values for the given field strength. Interpretation of this data, although slightly less convoluted than the relaxation data, is still plagued by problems related to non-spherical diffusion and much care must be taken when making conclusions. A full understanding of the model-free analysis and the effect of diffusion tensor anisotropy and rhombicity allows for better interpretation of the raw numbers.

To understand how reduced spectral density mapping is implemented in relax, the sample script will be worked through. This analysis type is not implemented in the GUI yet, though it shouldn't be too hard if anyone would like to contribute this and have a reference added to Chapter , the citations chapter.

### 8.2 $J(\omega)$ mapping script mode – the sample script

```
1  """Script for reduced spectral density mapping."""
2
3
4  # Create the data pipe.
5  pipe.create(pipe_name='my_protein', pipe_type='jw')
6
7  # Set up the 15N spins.
8  sequence.read(file='noe.600.out', res_num_col=1, res_name_col=2)
9  spin.name(name='N')
10 spin.element(element='N')
11 spin.isotope(isotope='15N', spin_id='@N')
12
13 # Load the 15N relaxation data.
14 relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
15                res_num_col=1, data_col=3, error_col=4)
16 relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
17                res_num_col=1, data_col=3, error_col=4)
```

```

16 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
    res_num_col=1, data_col=3, error_col=4)
17
18 # Generate 1H spins for the magnetic dipole-dipole relaxation interaction.
19 sequence.attach_protons()
20
21 # Define the magnetic dipole-dipole relaxation interaction.
22 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
23 interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)
24
25 # Define the chemical shift relaxation interaction.
26 value.set(val=-172 * 1e-6, param='csa')
27
28 # Select the frequency.
29 jw_mapping.set_frq(frq=600.0 * 1e6)
30
31 # Reduced spectral density mapping.
32 calc()
33
34 # Monte Carlo simulations (well, bootstrapping as this is a calculation and not a fit!).
35 monte_carlo.setup(number=500)
36 monte_carlo.create_data()
37 calc()
38 monte_carlo.error_analysis()
39
40 # Create grace files.
41 grace.write(y_data_type='j0', file='j0.agr', force=True)
42 grace.write(y_data_type='jwx', file='jwx.agr', force=True)
43 grace.write(y_data_type='jwh', file='jwh.agr', force=True)
44
45 # View the grace files.
46 grace.view(file='j0.agr')
47 grace.view(file='jwx.agr')
48 grace.view(file='jwh.agr')
49
50 # Write out the values.
51 value.write(param='j0', file='j0.txt', force=True)
52 value.write(param='jwx', file='jwx.txt', force=True)
53 value.write(param='jwh', file='jwh.txt', force=True)
54
55 # Finish.
56 results.write(file='results', force=True)
57 state.save('save', force=True)

```

### 8.3 J(w) mapping script mode – data pipe and spin system setup

The steps for setting up relax and the data model concept are described in full detail in Chapter 4. The first step, as for all analyses in relax, is to create a data pipe for storing all the data:

```

4 # Create the data pipe.
5 pipe.create(pipe_name='my_protein', pipe_type='jw')

```

Then, in this example, the  $^{15}\text{N}$  spins are created from one of the NOE relaxation data files (Chapter 6):

```

7 # Set up the 15N spins.

```



```

8 sequence.read(file='noe.600.out', res_num_col=1, res_name_col=2)
9 spin.name(name='N')
10 spin.element(element='N')
11 spin.isotope(isotope='15N', spin_id='@N')

```

Skipping the relaxation data loading, the next part of the analysis is to create protons attached to the nitrogens for the magnetic dipole-dipole relaxation interaction:

```

18 # Generate 1H spins for the magnetic dipole-dipole relaxation interaction.
19 sequence.attach_protons()

```

This is needed to define the magnetic dipole-dipole interaction which governs relaxation.

## 8.4 $J(\omega)$ mapping script mode – relaxation data loading

The loading of relaxation data is straight forward. This is performed prior to the creation of the proton spins so that the data is loaded only into the  $^{15}\text{N}$  spin containers and not both spins for each residue. Only data for a single field strength can be loaded:

```

13 # Load the 15N relaxation data.
14 relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
    res_num_col=1, data_col=3, error_col=4)
15 relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
    res_num_col=1, data_col=3, error_col=4)
16 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
    res_num_col=1, data_col=3, error_col=4)

```

The frequency of the data must also be explicitly specified:

```

28 # Select the frequency.
29 jw_mapping.set_freq(frq=600.0 * 1e6)

```

## 8.5 $J(\omega)$ mapping script mode – relaxation interactions

Prior to calculating the  $J(\omega)$  values, the physical interactions which govern relaxation of the spins must be defined. For the magnetic dipole-dipole relaxation interaction, the user functions are:

```

21 # Define the magnetic dipole-dipole relaxation interaction.
22 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
23 interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)

```

For the chemical shift relaxation interaction, the user function call is:

```

25 # Define the chemical shift relaxation interaction.
26 value.set(val=-172 * 1e-6, param='csa')

```

## 8.6 $J(\omega)$ mapping script mode – calculation and error propagation

Optimisation for this analysis is not needed as this is a direct calculation. Therefore the  $J(\omega)$  values are simply calculated with the call:

```
31 # Reduced spectral density mapping.  
32 calc()
```

The propagation of errors is more complicated. The Monte Carlo simulation framework of `relax` can be used to propagate the relaxation data errors to the spectral density errors. As this is a direct calculation, this collapses into the standard bootstrapping method. The normal Monte Carlo user functions can be called:

```
34 # Monte Carlo simulations (well, bootstrapping as this is a calculation and not a fit!).  
35 monte_carlo.setup(number=500)  
36 monte_carlo.create_data()  
37 calc()  
38 monte_carlo.error_analysis()
```

In this case, the `monte_carlo.initial_values` user function call is not required.

## 8.7 $J(\omega)$ mapping script mode – visualisation and data output

The rest of the script is used to output the results to 2D Grace files for visualisation (the `grace.view` user function calls will launch Grace with the created files), and the output of the values into plain text files.

## Chapter 9

# Consistency testing

### 9.1 Introduction to the consistency testing of relaxation data

In spin relaxation, datasets are often recorded at different magnetic fields. This is especially important when  $R_2$  values are to be used since  $\mu$ s-ms motions contribute to  $R_2$ . This contribution being scaled quadratically with the strength of the magnetic field, recording at multiple magnetic fields helps extract it. Also, acquiring data at multiple magnetic fields allows over-determination of the mathematical problems, e.g. in the model-free approach.

Recording at multiple magnetic fields is a good practice. However, it can cause artifacts if those different datasets are inconsistent. Inconsistencies can originate from, inter alia, the sample or the acquisition. Sample variations can be linked to changes in temperature, concentration, pH, etc. Water suppression is the main cause of acquisition variations as it affects relaxation parameters (especially NOE) of exposed and exchangeable moieties (e.g. the NH moiety).

It is thus a good idea to assess consistency of datasets acquired at different magnetic fields. For this purpose, three tests are implemented in relax. They are all based on the same principle – calculate a field independent value and compare it from one field to another.

The three tests are:

$J(0)$  The spectral density at the zero frequency calculated using the reduced spectral density approach.

$F_\eta$  A consistency function proposed by [Fushman et al. \(1998\)](#).

$F_{R_2}$  A consistency function proposed by [Fushman et al. \(1998\)](#).

These three tests are very similar (all probing consistency of  $R_2$  data and all suffering from the same limitations) and any of them can be used for consistency testing. In the example below, the  $J(0)$  values are used for consistency testing.

Different methods exist to compare test values calculated from one field to another. These include correlation plots and histograms, and calculation of correlation, skewness and

kurtosis coefficients. The details of how to interpret such analyses are available at the end of this chapter in Section 9.7.

For more details on the tests and their implementation within relax, see:

- Morin, S. and Gagné, S. (2009a). Simple tests for the validation of multiple field spin relaxation data. *J. Biomol. NMR*, **45**, 361–372. ([10.1007/s10858-009-9381-4](https://doi.org/10.1007/s10858-009-9381-4))

Or for the origin of the tests themselves:

- Fushman, D., Tjandra, N., and Cowburn, D. (1999). An approach to direct determination of protein dynamics from  $^{15}\text{N}$  NMR relaxation at multiple fields, independent of variable  $^{15}\text{N}$  chemical shift anisotropy and chemical exchange contributions. *J. Am. Chem. Soc.*, **121**(37), 8577–8582. ([10.1021/ja9904991](https://doi.org/10.1021/ja9904991))

In addition, see the following review which includes a discussion on how to evaluate the reliability of recorded relaxation data:

- Morin, S. (2011). A practical guide to protein dynamics from  $^{15}\text{N}$  spin relaxation in solution. *Prog. NMR Spectrosc.*, **59**(3), 245–262. ([10.1016/j.pnmrs.2010.12.003](https://doi.org/10.1016/j.pnmrs.2010.12.003))

## 9.2 Consistency testing in the prompt/script UI mode

The consistency testing analysis is only available via the prompt/script UI modes – no GUI auto-analysis has yet been built by a relax power-user.

### 9.2.1 Consistency testing script mode – the sample script

The following script can be found in the `sample_scripts` directory.

```

1  """ Script for consistency testing.
2
3  Severe artifacts can be introduced if model-free analysis is performed from inconsistent
   multiple magnetic field datasets. The use of simple tests as validation tools for the
   consistency assessment can help avoid such problems in order to extract more reliable
   information from spin relaxation experiments. In particular, these tests are useful
   for detecting inconsistencies arising from R2 data. Since such inconsistencies can
   yield artificial Rex parameters within model-free analysis, these tests should be use
   routinely prior to any analysis such as model-free calculations.
4
5  This script will allow one to calculate values for the three consistency tests J(0), F_eta
   and F_R2. Once this is done, qualitative analysis can be performed by comparing
   values obtained at different magnetic fields. Correlation plots and histograms are
   useful tools for such comparison, such as presented in Morin & Gagne (2009a) J.
   Biomol. NMR, 45: 361-372.
6
7
8  References
```

```

9  =====
10
11  The description of the consistency testing approach:
12
13      Morin & Gagne (2009a) Simple tests for the validation of multiple field spin
14      relaxation data. J. Biomol. NMR, 45: 361-372. U{http://dx.doi.org/10.1007/s10858
15      -009-9381-4}
16
17  The origins of the equations used in the approach:
18
19      J(0):
20      Farrow et al. (1995) Spectral density function mapping using 15N relaxation data
21      exclusively. J. Biomol. NMR, 6: 153-162. U{http://dx.doi.org/10.1007/BF00211779}
22
23      F_eta:
24      Fushman et al. (1998) Direct measurement of 15N chemical shift anisotropy in
25      solution. J. Am. Chem. Soc., 120: 10947-10952. U{http://dx.doi.org/10.1021/ja981686m}
26
27      F_R2:
28      Fushman et al. (1998) Direct measurement of 15N chemical shift anisotropy in
29      solution. J. Am. Chem. Soc., 120: 10947-10952. U{http://dx.doi.org/10.1021/ja981686m}
30
31  A study where consistency tests were used:
32
33      Morin & Gagne (2009) NMR dynamics of PSE-4 beta-lactamase: An interplay of ps-ns order
34      and us-ms motions in the active site. Biophys. J., 96: 4681-4691. U{http://dx.doi.org
35      /10.1016/j.bpj.2009.02.068}
36
37  """
38
39  # Create the data pipe.
40  name = 'consistency'
41  pipe.create(name, 'ct')
42
43  # Set up the 15N spins.
44  sequence.read('noe.600.out', res_num_col=1)
45  spin.name(name='N')
46  spin.element(element='N')
47  spin.isotope(isotope='15N', spin_id='@N')
48
49  # Load the relaxation data.
50  relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
51                  res_num_col=1, data_col=3, error_col=4)
52  relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
53                  res_num_col=1, data_col=3, error_col=4)
54  relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
55                  res_num_col=1, data_col=3, error_col=4)
56
57  # Generate the 1H spins for the magnetic dipole-dipole interaction.
58  sequence.attach_protons()
59
60  # Define the magnetic dipole-dipole relaxation interaction.
61  interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
62  interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)
63
64  # Define the chemical shift relaxation interaction.
65  value.set(val=-172 * 1e-6, param='csa')
66
67  # Set the angle between the 15N-1H vector and the principal axis of the 15N chemical shift
68  tensor
69  value.set(val=15.7, param='orientation')
70
71

```

```

59 # Set the approximate correlation time.
60 value.set(val=13 * 1e-9, param='tc')
61
62 # Set the frequency.
63 consistency_tests.set_frq(frq=600.0 * 1e6)
64
65 # Consistency tests.
66 calc()
67
68 # Monte Carlo simulations.
69 monte_carlo.setup(number=500)
70 monte_carlo.create_data()
71 calc()
72 monte_carlo.error_analysis()
73
74 # Create grace files.
75 grace.write(y_data_type='j0', file='j0.agr', force=True)
76 grace.write(y_data_type='f_eta', file='f_eta.agr', force=True)
77 grace.write(y_data_type='f_r2', file='f_r2.agr', force=True)
78
79 # View the grace files.
80 grace.view(file='j0.agr')
81 grace.view(file='f_eta.agr')
82 grace.view(file='f_r2.agr')
83
84 # Finish.
85 results.write(file='results', force=True)
86 state.save('save', force=True)

```

This is similar in spirit to the reduced spectral density mapping sample script (Chapter 8 on page 127).

### 9.3 Consistency testing script mode – data pipe and spin system setup

The steps for setting up relax and the data model concept are described in full detail in Chapter 4. The first step, as for all analyses in relax, is to create a data pipe for storing all the data:

```

31 # Create the data pipe.
32 name = 'consistency'
33 pipe.create(name, 'ct')

```

Then, in this example, the  $^{15}\text{N}$  spins are created from one of the NOE relaxation data files (Chapter 6):

```

35 # Set up the  $^{15}\text{N}$  spins.
36 sequence.read('noe.600.out', res_num_col=1)
37 spin.name(name='N')
38 spin.element(element='N')
39 spin.isotope(isotope='15N', spin_id='@N')

```

Skipping the relaxation data loading, the next part of the analysis is to create protons attached to the nitrogens for the magnetic dipole-dipole relaxation interaction:

```

46 # Generate the 1H spins for the magnetic dipole-dipole interaction.
47 sequence.attach_protons()

```

This is needed to define the magnetic dipole-dipole interaction which governs relaxation.

## 9.4 Consistency testing script mode – relaxation data loading

The loading of relaxation data is straight forward. This is performed prior to the creation of the proton spins so that the data is loaded only into the  $^{15}\text{N}$  spin containers and not both spins for each spin system. Note that if the relaxation data files contain spin information, then this order is not important. For this analysis, only data for a single field strength can be loaded:

```

41 # Load the relaxation data.
42 relax_data.read(ri_id='R1_600', ri_type='R1', frq=600.0*1e6, file='r1.600.out',
    res_num_col=1, data_col=3, error_col=4)
43 relax_data.read(ri_id='R2_600', ri_type='R2', frq=600.0*1e6, file='r2.600.out',
    res_num_col=1, data_col=3, error_col=4)
44 relax_data.read(ri_id='NOE_600', ri_type='NOE', frq=600.0*1e6, file='noe.600.out',
    res_num_col=1, data_col=3, error_col=4)

```

The frequency of the data must also be explicitly specified:

```

62 # Set the frequency.
63 consistency_tests.set_freq(frq=600.0 * 1e6)

```

## 9.5 Consistency testing script mode – relaxation interactions

Prior to calculating the  $J(0)$ ,  $F_\eta$ , and  $F_{R_2}$  values, the physical interactions which govern relaxation of the spins must be defined. For the magnetic dipole-dipole relaxation interaction, the user functions are:

```

49 # Define the magnetic dipole-dipole relaxation interaction.
50 interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True)
51 interatom.set_dist(spin_id1='@N', spin_id2='@H', ave_dist=1.02 * 1e-10)

```

For the chemical shift relaxation interaction, the user function call is:

```

53 # Define the chemical shift relaxation interaction.
54 value.set(val=-172 * 1e-6, param='csa')

```

For the angle in degrees between the  $^{15}\text{N}$ - $^1\text{H}$  vector and the principal axis of the  $^{15}\text{N}$  chemical shift tensor, the user function call is:

```

56 # Set the angle between the 15N-1H vector and the principal axis of the 15N chemical shift
    tensor
57 value.set(val=15.7, param='orientation')

```

## 9.6 Consistency testing script mode – calculation and error propagation

Optimisation for this analysis is not needed as this is a direct calculation. Therefore the  $J(0)$ ,  $F_\eta$ , and  $F_{R_2}$  values are simply calculated with the call:

```
65 # Consistency tests.
66 calc()
```

The propagation of errors is more complicated. The Monte Carlo simulation framework of relax can be used to propagate the relaxation data errors to the spectral density errors. As this is a direct calculation, this collapses into the standard bootstrapping method. The normal Monte Carlo user functions can be called:

```
68 # Monte Carlo simulations.
69 monte_carlo.setup(number=500)
70 monte_carlo.create_data()
71 calc()
72 monte_carlo.error_analysis()
```

In this case, the `monte_carlo.initial_values` user function call is not required.

## 9.7 Consistency testing script mode – visualisation and data output

The rest of the script is used to output the results to 2D Grace files for visualisation (the `grace.view` user function calls will launch Grace with the created files), and the output of the values into plain text files.

However, simply visualizing the calculated  $J(0)$ ,  $F_\eta$ , and  $F_{R_2}$  values this way does not allow proper consistency testing. Indeed, for assessing the consistency of relaxation data using these tests, different methods exist to compare values calculated from one field to another. These include correlation plots and histograms, and calculation of correlation, skewness and kurtosis coefficients.

To complete the consistency testing analysis, the following steps are needed:

- Extract the  $J(0)$  values at multiple magnetic fields.
- Join together the data from a pair of magnetic fields either by pasting them as two columns of one file (approach A), or by dividing values from a first magnetic field by values from a second magnetic field (approach B).
- Make either a correlation plot (approach A), or an histogram of the ratios (approach B).
- See if the correlation plot is centered around a perfect correlation or skewed away (approach A), or if the values are centered around 1 in the histogram (approach B). If yes, data from multiple magnetic fields is consistent from one magnetic field to another. If no, data is inconsistent. In the case where inconsistency arises, if data



from more than two magnetic fields is available, more than one pair of data can be checked and the inconsistent magnetic field data can be identified.

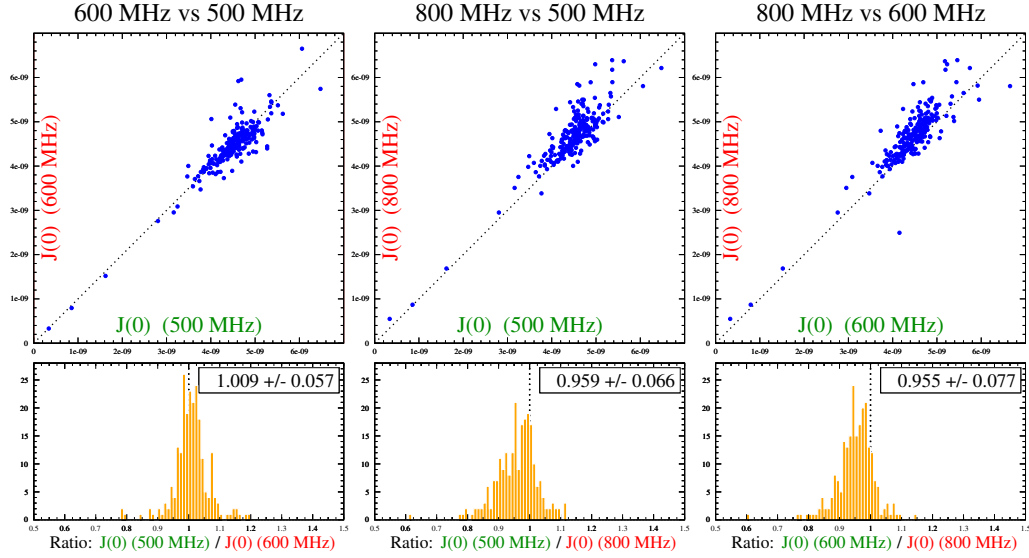


Figure 9.1: Example of consistency testing visual analysis. Relaxation data from three different magnetic fields are compared. For each pair of magnetic field, a correlation plot of the calculated  $J(0)$  values (approach A, top) as well as an histogram of the ration of calculated  $J(0)$  values (approach B, bottom) are shown. These graphs must be manually created from the output of the sample script shown in section 9.2.1. The PSE-4 data, as published in [Morin and Gagné \(2009b\)](#), has been reused for the purpose of this example.

An example of such an analysis is shown in Figure 9.7. This example displays both consistent and inconsistent data. As the figure shows, the data recorded at 500 MHz and 600 MHz are consistent with each other whereas the data recorded at 800 MHz is consistent with the neither the 500 MHz nor 600 MHz data. Since more than two magnetic fields were used, this allowed the identification of the 800 MHz data as being inconsistent allowing the authors to take special care with this data set.

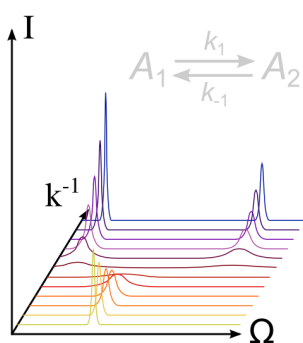
The 800 MHz data inconsistency is seen in the correlation plots (top) by a deviation from the dotted line (which represents the theoretical situation when equal  $J(0)$  values are extracted from both magnetic fields. It is also observable in the histograms (bottom) where the ratio of the data from two magnetic fields is not centered at 1.0. In fact, there seems to be a systematic shift of the calculated  $J(0)$  values at 800 MHz when compared to the two other relaxation magnetic fields. This is caused by a similar shift in the experimental  $R_2$  (transversal relaxation rate) data.

For the 500 MHz and 600 MHz data pair, the data are centered around the dotted line in the correlation plot (approach A, top left) as well as centered around a value of 1.0 in the histogram comparing the ratios of values from both magnetic fields (approach B, bottom left). Of course, there are some outlier values even in the case of consistent data. There are caused by specific dynamic characteristics of these spins and are different from systematic inconsistencies such as depicted in the example above with the data recorded at 800 MHz.



## Chapter 10

# The analysis of relaxation dispersion



### 10.1 Introduction to relaxation dispersion

Relaxation dispersion is the experimental modulation of chemical exchange relaxation. For the  $R_{1\rho}$ -type experiment in which the nucleus of interest is spin-locked, either the spin-lock field strength or the offset between the spin-lock pulse and the chemical shift of the spins is used to modulate the exchange. For the CPMG-type experiment, varying the time between the pulses modules the exchange. Both experiment types are handled by relax.

#### 10.1.1 The modelling of dispersion data

For a system under the influence of chemical exchange, the evolution of the transverse magnetisation is given by the [Bloch \(1946\)](#) equations as modified by [McConnell \(1958\)](#) for chemical exchange – the Bloch-McConnell equations. For a two state exchange jumping

between states A and B, the equation is:

$$\frac{d}{dt} \begin{bmatrix} M_A^+(t) \\ M_B^+(t) \end{bmatrix} = \begin{bmatrix} -i\Omega_A - R_{2A}^0 - p_B k_{\text{ex}} & p_A k_{\text{ex}} \\ p_B k_{\text{ex}} & -i\Omega_B - R_{2B}^0 - p_A k_{\text{ex}} \end{bmatrix} \begin{bmatrix} M_A^+(t) \\ M_B^+(t) \end{bmatrix}. \quad (10.1)$$

The analytic or closed-form frequency-domain solution for this equation however remains intractable. Solutions can nevertheless be found by either making assumptions or restrictions about the exchange process and then analytically solving 10.1 or by finding numeric solutions. The modelling of relaxation dispersion data can hence be categorised into these two distinct methodologies:

**Analytical models:** Optimisation of models based on analytical, closed-form expressions derived from the Bloch-McConnell equations subject to certain conditions (see Section 10.3 on page 148 and Section 10.7 on page 161).

**Numerical models:** Optimisation of models based on numerically solving the Bloch-McConnell equations (see Section 10.4 on page 152 and Section 10.8 on page 164).

### 10.1.2 Implemented models

A number of analytic and numeric models are supported within relax. These cover single quantum (SQ) CPMG-type, single quantum (SQ)  $R_{1\rho}$ -type, and combined proton-heteronuclear single quantum (SQ), zero quantum (ZQ), double quantum (DQ) and multi quantum (MQ) CPMG-type experiments. If the model you are interested in is not available, please see Section 10.11 on page 176 for how you can add new models to relax.

Models which are independent of the experiment type include:

**‘R2eff’:** This is the model used to determine the  $R_{2\text{eff}}$  or  $R_{1\rho}$  values and errors required as the base data for all other models. See Section 10.2.1 on page 147.

**‘No Rex’:** This is the model for no chemical exchange being present. See Section 10.2.2 on page 148.

For the SQ CPMG-type experiments, the analytic models currently supported are:

**‘LM63’:** The original Luz and Meiboom (1963) 2-site fast exchange equation with parameters  $\{R_2^0, \dots, \Phi_{\text{ex}}, k_{\text{ex}}\}$ . See Section 10.3.1 on page 149.

**‘LM63 3-site’:** The original Luz and Meiboom (1963) 3-site fast exchange equation with parameters  $\{R_2^0, \dots, \Phi_{\text{ex},B}, k_B, \Phi_{\text{ex},C}, k_C\}$ . The equations of O’Connell et al. (2009) can be used to approximately convert the parameters  $\{\Phi_{\text{ex},B}, k_B, \Phi_{\text{ex},C}, k_C\}$  to more biologically relevant parameters. See Section 10.3.2 on page 149.

**‘CR72’:** The reduced Carver and Richards (1972) 2-site equation for most time scales whereby the simplification  $R_{2A}^0 = R_{2B}^0$  is assumed. It has the parameters  $\{R_2^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.3.4 on page 151.

- ‘**CR72 full**’: The full [Carver and Richards \(1972\)](#) 2-site equation for most time scales with parameters  $\{R_{2A}^0, R_{2B}^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.3.3 on page 150.
- ‘**IT99**’: The [Ishima and Torchia \(1999\)](#) 2-site model for all time scales with  $p_A \gg p_B$  and with parameters  $\{R_2^0, \dots, \Phi_{\text{ex}}, p_A, \Delta\omega^2, k_{\text{ex}}\}$ . See Section 10.3.5 on page 151.
- ‘**TSMFK01**’: The [Tollinger et al. \(2001\)](#) 2-site very-slow exchange model for time scales within range of microsecond to second time scale. Applicable in the limit of slow exchange, when  $|R_{2A}^0 - R_{2B}^0| \ll k_{AB}, k_{BA} \ll 1/\tau_{\text{CPMG}}$ .  $2 * \tau_{\text{CPMG}}$  is the time between successive 180 degree pulses. Parameters are  $\{R_{2A}^0, \dots, \Delta\omega, k_{AB}\}$ . See Section 10.3.6 on page 152.

For the SQ CPMG-type experiments, the numeric models currently supported are:

- ‘**NS CPMG 2-site expanded**’: A model for 2-site exchange expanded using Maple by Nikolai Skrynnikov ([Tollinger et al., 2001](#)). It has the parameters  $\{R_2^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.4.1 on page 152.
- ‘**NS CPMG 2-site 3D**’: The reduced model for 2-site exchange using 3D magnetisation vectors whereby the simplification  $R_{2A}^0 = R_{2B}^0$  is assumed. It has the parameters  $\{R_2^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.4.3 on page 155.
- ‘**NS CPMG 2-site 3D full**’: The full model for 2-site exchange using 3D magnetisation vectors with parameters  $\{R_{2A}^0, R_{2B}^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.4.2 on page 155.
- ‘**NS CPMG 2-site star**’: The reduced model for 2-site exchange using complex conjugate matrices whereby the simplification  $R_{2A}^0 = R_{2B}^0$  is assumed. It has the parameters  $\{R_2^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.4.5 on page 155.
- ‘**NS CPMG 2-site star full**’: The full model for 2-site exchange using complex conjugate matrices with parameters  $\{R_{2A}^0, R_{2B}^0, \dots, p_A, \Delta\omega, k_{\text{ex}}\}$ . See Section 10.4.4 on page 155.

For the combined proton-heteronuclear SQ, ZQ, DQ and MQ CPMG-type experiments (MMQ – or multi-multiple quantum), the analytic models currently supported are:

- ‘**MMQ CR72**’: The [Carver and Richards \(1972\)](#) 2-site model for most time scales expanded for MMQ CPMG data by [Korzhnev et al. \(2004a\)](#). It has the parameters  $\{R_2^0, \dots, p_A, \Delta\omega, \Delta\omega^H, k_{\text{ex}}\}$ . See Section 10.5.1 on page 156.

For the combined proton-heteronuclear SQ, ZQ, DQ and MQ CPMG-type experiments (MMQ – or multi-multiple quantum), the numeric models currently supported are:

- ‘**NS MMQ 2-site**’: The model for 2-site exchange whereby the simplification  $R_{2A}^0 = R_{2B}^0$  is assumed. It has the parameters  $\{R_2^0, \dots, p_A, \Delta\omega, \Delta\omega^H, k_{\text{ex}}\}$ . See Section 10.6.1 on page 157.
- ‘**NS MMQ 3-site linear**’: The model for 3-site exchange linearised with  $k_{AC} = k_{CA} = 0$  whereby the simplification  $R_{2A}^0 = R_{2B}^0 = R_{2C}^0$  is assumed. It has the parameters  $\{R_2^0, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, \Delta\omega_{AB}^H, \Delta\omega_{BC}^H, k_{\text{ex}}^{AB}, k_{\text{ex}}^{BC}\}$ . See Section 10.6.2 on page 159.

**‘NS MMQ 3-site’:** The model for 3-site exchange whereby the simplification  $R_{2A}^0 = R_{2B}^0 = R_{2C}^0$  is assumed. It has the parameters  $\{R_2^0, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, \Delta\omega_{AB}^H, \Delta\omega_{BC}^H, k_{ex}^{AB}, k_{ex}^{BC}, k_{ex}^{AC}\}$ . See Section 10.6.3 on page 160.

For the  $R_{1\rho}$ -type experiments, the analytic models currently supported are:

**‘M61’:** The Meiboom (1961) 2-site fast exchange equation for on-resonance data with parameters  $\{R'_{1\rho}, \dots, \Phi_{ex}, k_{ex}\}$ . See Section 10.7.1 on page 161.

**‘DPL94’:** The Davis et al. (1994) extension of the ‘M61’ model for off-resonance data with parameters  $\{R'_{1\rho}, \dots, \Phi_{ex}, k_{ex}\}$ . See Section 10.7.3 on page 162.

**‘M61 skew’:** The Meiboom (1961) 2-site equation for all time scales with  $p_A \gg p_B$  and with parameters  $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$ . This model is disabled by default in the dispersion auto-analysis. See Section 10.7.2 on page 161.

**‘TP02’:** The Trott and Palmer (2002) 2-site equation for all time scales with  $p_A \gg p_B$  and with parameters  $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$ . See Section 10.7.4 on page 162.

**‘TAP03’:** The Trott et al. (2003) off-resonance 2-site analytic equation for all time scales with the weak condition  $p_A \gg p_B$  and with parameters  $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$ .

**‘MP05’:** The Miloushev and Palmer (2005) off-resonance 2-site equation for all time scales with parameters  $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$ . See Section 10.7.6 on page 163.

For the  $R_{1\rho}$ -type experiments, the numeric models currently supported are:

**‘NS R1rho 2-site’:** The model for 2-site exchange using 3D magnetisation vectors. It has the parameters  $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$ . See Section 10.8.1 on page 164.

**‘NS  $R_{1\rho}$  3-site linear’:** The model for 3-site exchange linearised with  $k_{AC} = k_{CA} = 0$  whereby the simplification  $R'_{1\rho A} = R'_{1\rho B} = R'_{1\rho C}$  is assumed. It has the parameters  $\{R'_{1\rho}, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, k_{ex}^{AB}, k_{ex}^{BC}\}$ . See Section 10.8.3 on page 166.

**‘NS  $R_{1\rho}$  3-site’:** The model for 3-site exchange whereby the simplification  $R'_{1\rho A} = R'_{1\rho B} = R'_{1\rho C}$  is assumed. It has the parameters  $\{R'_{1\rho}, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, k_{ex}^{AB}, k_{ex}^{BC}, k_{ex}^{AC}\}$ . See Section 10.8.2 on page 164.

### 10.1.3 Dispersion model summary

Except for ‘R2eff’ and ‘No Rex’, all models can be fit to clusterings of spins, or spin blocks. The models are described in more detail below and summarised in Table 10.1. The parameters of the models and of relaxation dispersion in general are given in Table 10.2.

Table 10.1: The dispersion models supported by relax.

| Model name               | Solution | Sites | Parameters   | Restrictions   | Reference                  |
|--------------------------|----------|-------|--|--|----------------------------|
| <hr/>                    |          |       |  |  |                            |
| Experiment independent   |          |       |  |  |                            |
| R2eff                    | -        | -     | $\{R_{2\text{eff}}, \dots\}$   | Fixed relaxation time period   | -                          |
| R2eff                    | -        | -     | $\{R_{2\text{eff}}, I_0, \dots\}$  | Variable relaxation time period  | -                          |
| No Rex                   | Closed   | 0     | $\{R_2^0, \dots\}$   | -  | -                          |
| <hr/>                    |          |       |  |  |                            |
| CPMG-type                |          |       |  |  |                            |
| LM63                     | Analytic | 2     | $\{R_2^0, \dots, \Phi_{\text{ex}}, k_{\text{ex}}\}$                                      | Fast exchange  | Luz and Meiboom (1963)     |
| LM63 3-site              | Analytic | 3     | $\{R_2^0, \dots, \Phi_{\text{ex,B}}, k_{\text{B}}, \Phi_{\text{ex,C}}, k_{\text{C}}\}$   | Fast exchange, $p_{\text{A}} > p_{\text{B}}$ and $p_{\text{A}} > p_{\text{C}}$ | Luz and Meiboom (1963)     |
| CR72                     | Analytic | 2     | $\{R_2^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$                            | $p_{\text{A}} > p_{\text{B}}$ , not very slow exchange                         | Carver and Richards (1972) |
| CR72 full                | Analytic | 2     | $\{R_{2\text{A}}^0, R_{2\text{B}}^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$ | $p_{\text{A}} > p_{\text{B}}$ , not very slow exchange                         | Carver and Richards (1972) |
| IT99                     | Analytic | 2     | $\{R_2^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$                            | $p_{\text{A}} \gg p_{\text{B}}$  | Ishima and Torchia (1999)  |
| TSMFK01                  | Analytic | 2     | $\{R_{2\text{A}}^0, \dots, \Delta\omega, k_{\text{AB}}\}$                                | $p_{\text{A}} \gg p_{\text{B}}$  | Tollinger et al. (2001)    |
| NS CPMG 2-site expanded  | Numeric  | 2     | $\{R_2^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$                            | $p_{\text{A}} > p_{\text{B}}$  | Tollinger et al. (2001)    |
| NS CPMG 2-site 3D        | Numeric  | 2     | $\{R_2^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$                            | $p_{\text{A}} > p_{\text{B}}$  | -                          |
| NS CPMG 2-site 3D full   | Numeric  | 2     | $\{R_{2\text{A}}^0, R_{2\text{B}}^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$ | $p_{\text{A}} > p_{\text{B}}$  | -                          |
| NS CPMG 2-site star      | Numeric  | 2     | $\{R_2^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$                            | $p_{\text{A}} > p_{\text{B}}$  | -                          |
| NS CPMG 2-site star full | Numeric  | 2     | $\{R_{2\text{A}}^0, R_{2\text{B}}^0, \dots, p_{\text{A}}, \Delta\omega, k_{\text{ex}}\}$ | $p_{\text{A}} > p_{\text{B}}$  | -                          |

Table 10.1: The dispersion models supported by relax.

| Model name                 | Solution | Sites | Parameters  | Restrictions                                | Reference                   |
|----------------------------|----------|-------|---|---|-----------------------------|
| <b>MMQ CPMG-type</b>       |          |       |   |   |                             |
| MMQ CR72                   | Analytic | 2     | $\{R_2^0, \dots, p_A, \Delta\omega, \Delta\omega^H, k_{ex}\}$   | $p_A > p_B$                                 | Korzhnev et al. (2004a)     |
| NS MMQ 2-site              | Numeric  | 2     | $\{R_2^0, \dots, p_A, \Delta\omega, \Delta\omega^H, k_{ex}\}$   | $p_A > p_B$                                 | Korzhnev et al. (2005a)     |
| NS MMQ 3-site linear       | Numeric  | 3     | $\{R_2^0, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, \Delta\omega_{AB}^H, \Delta\omega_{BC}^H, k_{ex}^{AB}, k_{ex}^{BC}\}$              | $p_A > p_B$ and $p_B > p_C$                 | Korzhnev et al. (2005a)     |
| NS MMQ 3-site              | Numeric  | 3     | $\{R_2^0, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, \Delta\omega_{AB}^H, \Delta\omega_{BC}^H, k_{ex}^{AB}, k_{ex}^{BC}, k_{ex}^{AC}\}$ | $p_A > p_B$ and $p_B > p_C$                 | Korzhnev et al. (2005a)     |
| <b>R<sub>1ρ</sub>-type</b> |          |       |   |   |                             |
| M61                        | Analytic | 2     | $\{R'_{1\rho}, \dots, \Phi_{ex}, k_{ex}\}$  | Fast exchange, on-resonance,<br>$R_1 = R_2$ | Meiboom (1961)              |
| DPL94                      | Analytic | 2     | $\{R'_{1\rho}, \dots, \Phi_{ex}, k_{ex}\}$  | Fast exchange                               | Davis et al. (1994)         |
| M61 skew                   | Analytic | 2     | $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$  | $p_A \gg p_B$ , on-resonance                | Meiboom (1961)              |
| TP02                       | Analytic | 2     | $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$  | $p_A \gg p_B$ , not fast exchange           | Trott and Palmer (2002)     |
| TAP03                      | Analytic | 2     | $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$  | Weak condition of $p_A \gg p_B$             | Trott et al. (2003)         |
| TP04 <sup>1</sup>          | Analytic | N     | $\{R'_{1\rho}, \dots, p_1, \dots, p_N, \bar{\omega}, k_{12}, \dots, k_{1N}\}$   | One site dominant                           | Trott and Palmer (2004)     |
| MP05                       | Analytic | 2     | $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$  | $p_A > p_B$                                 | Miloushev and Palmer (2005) |
| NS R1rho 2-site            | Numeric  | 2     | $\{R'_{1\rho}, \dots, p_A, \Delta\omega, k_{ex}\}$  | $p_A > p_B$                                 | -                           |
| NS R1rho 3-site linear     | Numeric  | 3     | $\{R'_{1\rho}, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, k_{ex}^{AB}, k_{ex}^{BC}\}$   | $p_A > p_B$ and $p_A > p_C$                 | -                           |
| NS R1rho 3-site            | Numeric  | 3     | $\{R'_{1\rho}, \dots, p_A, p_B, \Delta\omega_{AB}, \Delta\omega_{BC}, k_{ex}^{AB}, k_{ex}^{BC}, k_{ex}^{AC}\}$                                      | $p_A > p_B$ and $p_A > p_C$                 | -                           |

<sup>1</sup>Not implemented yet



Table 10.2: The parameters of relaxation dispersion.

| Parameter            | Equation                            | Description   | Units               |
|----------------------|-------------------------------------|---|---------------------|
| $\nu_{\text{CPMG}}$  | $1/(2\tau_{\text{CPMG}})$           | CPMG frequency  | Hz                  |
| $\tau_{\text{CPMG}}$ | $1/(2\nu_{\text{CPMG}})$            | Delay between CPMG $\pi$ pulses   | s                   |
| $T_{\text{relax}}$   | -                                   | The relaxation delay period   | s                   |
| $I_0$                | -                                   | Reference peak intensity when $T_{\text{relax}}$ is zero                              | -                   |
| $I_1$                | -                                   | Peak intensity for a given $\nu_{\text{CPMG}}$ or spin-lock field strength $\omega_1$ | -                   |
| $R_2^0$              | -                                   | $R_2$ relaxation rate in the absence of exchange                                      | rad.s <sup>-1</sup> |
| $R_{2A}^0$           | -                                   | $R_2$ relaxation rate for state A in the absence of exchange                          | rad.s <sup>-1</sup> |
| $R_{2B}^0$           | -                                   | $R_2$ relaxation rate for state B in the absence of exchange                          | rad.s <sup>-1</sup> |
| $R_{1\rho}'$         | -                                   | $R_{1\rho}$ relaxation rate in the absence of exchange                                | rad.s <sup>-1</sup> |
| $\bar{\omega}$       | $\bar{\omega} - \omega_{\text{rf}}$ | The average resonance offset in the rotating frame                                    | rad.s <sup>-1</sup> |
| $\Omega_A$           | $\omega_A - \omega_{\text{rf}}$     | The resonance offset in the rotating frame for state A                                | rad.s <sup>-1</sup> |
| $\Omega_B$           | $\omega_B - \omega_{\text{rf}}$     | The resonance offset in the rotating frame for state B                                | rad.s <sup>-1</sup> |
| $\Omega_C$           | $\omega_C - \omega_{\text{rf}}$     | The resonance offset in the rotating frame for state C                                | rad.s <sup>-1</sup> |
| $\omega_A$           | -                                   | The Larmor frequency of the spin in state A   | rad.s <sup>-1</sup> |
| $\omega_B$           | -                                   | The Larmor frequency of the spin in state B   | rad.s <sup>-1</sup> |
| $\omega_C$           | -                                   | The Larmor frequency of the spin in state C   | rad.s <sup>-1</sup> |
| $\omega_A^H$         | -                                   | The proton Larmor frequency of the spin in state A (for MMQ data)                     | rad.s <sup>-1</sup> |
| $\omega_B^H$         | -                                   | The proton Larmor frequency of the spin in state B (for MMQ data)                     | rad.s <sup>-1</sup> |
| $\omega_C^H$         | -                                   | The proton Larmor frequency of the spin in state C (for MMQ data)                     | rad.s <sup>-1</sup> |
| $\bar{\omega}$       | $p_A\omega_A + p_B\omega_B$         | The population averaged Larmor frequency of the spin                                  | rad.s <sup>-1</sup> |
| $\omega_1$           | -                                   | Spin-lock field strength, i.e. the amplitude of the rf field                          | rad.s <sup>-1</sup> |
| $\omega_e$           | $\sqrt{\Omega^2 + \omega_1^2}$      | Effective field in the rotating frame   | rad.s <sup>-1</sup> |
| $\omega_{\text{rf}}$ | -                                   | Spin-lock offset, i.e. the frequency of the rf field                                  | rad.s <sup>-1</sup> |
| $\theta$             | $\arctan(\frac{\omega_1}{\Omega})$  | Rotating frame tilt angle   | rad                 |
| $k_{AB}$             | $p_B k_{\text{ex}}$                 | The forward exchange rate from state A to state B (2-site)                            | rad.s <sup>-1</sup> |
| $k_{BA}$             | $p_A k_{\text{ex}}$                 | The reverse exchange rate from state B to state A (2-site)                            | rad.s <sup>-1</sup> |
| $k_{AB}$             | $p_B k_{\text{ex}}^{AB}$            | The forward exchange rate from state A to state B (3-site)                            | rad.s <sup>-1</sup> |
| $k_{BA}$             | $p_A k_{\text{ex}}^{AB}$            | The reverse exchange rate from state B to state A (3-site)                            | rad.s <sup>-1</sup> |
| $k_{BC}$             | $p_C k_{\text{ex}}^{BC}$            | The forward exchange rate from state B to state C (3-site)                            | rad.s <sup>-1</sup> |
| $k_{CB}$             | $p_B k_{\text{ex}}^{BC}$            | The reverse exchange rate from state C to state B (3-site)                            | rad.s <sup>-1</sup> |
| $k_{AC}$             | $p_C k_{\text{ex}}^{AC}$            | The forward exchange rate from state A to state C (3-site)                            | rad.s <sup>-1</sup> |

Table 10.2: The parameters of relaxation dispersion.

| Parameter             | Equation                                    | Description   | Units  |
|-----------------------|---|---|--|
| $k_{CA}$              | $p_A k_{ex}^{AC}$                           | The reverse exchange rate from state C to state A (3-site)        | $\text{rad.s}^{-1}$  |
| $k_{ex}$              | $1/\tau_{ex}$                               | Chemical exchange rate constant                                   | $\text{rad.s}^{-1}$  |
| $k_{ex}^{AB}$         | $k_{AB} + k_{BA}$                           | Chemical exchange rate constant between sites A and B             | $\text{rad.s}^{-1}$  |
| $k_{ex}^{BC}$         | $k_{BC} + k_{CB}$                           | Chemical exchange rate constant between sites B and C             | $\text{rad.s}^{-1}$  |
| $k_{ex}^{AC}$         | $k_{AC} + k_{CA}$                           | Chemical exchange rate constant between sites A and C             | $\text{rad.s}^{-1}$  |
| $k_B$                 | $\approx k_{ex}^{AB}$                       | Approximate chemical exchange rate constant between sites A and B | $\text{rad.s}^{-1}$  |
| $k_C$                 | $\approx k_{ex}^{AC}$                       | Approximate chemical exchange rate constant between sites A and C | $\text{rad.s}^{-1}$  |
| $\tau_{ex}$           | $1/k_{ex}$                                  | Time of exchange  | $\text{s.rad}^{-1}$  |
| $p_A$                 | -   | Population of state A   | -  |
| $p_B$                 | $1 - p_A$                                   | Population of state B (2-site)                                    | -  |
| $p_B$                 | $1 - p_A - p_C$                             | Population of state B (3-site)                                    | -  |
| $p_C$                 | $1 - p_A - p_B$                             | Population of state C (3-site)                                    | -  |
| $\Delta\omega$        | $\omega_B - \omega_A$                       | Chemical shift difference between sites A and B (2-site)          | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega_{AB}$   | $\omega_B - \omega_A$                       | Chemical shift difference between sites A and B (3-site)          | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega_{BC}$   | $\omega_C - \omega_B$                       | Chemical shift difference between sites B and C (3-site)          | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega_{AC}$   | $\Delta\omega_{AB} + \Delta\omega_{BC}$     | Chemical shift difference between sites A and C (3-site)          | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega^H$      | $\omega_B^H - \omega_A^H$                   | Proton chemical shift difference between sites A and B (2-site)   | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega_{AB}^H$ | $\omega_B^H - \omega_A^H$                   | Proton chemical shift difference between sites A and B (3-site)   | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega_{BC}^H$ | $\omega_C^H - \omega_B^H$                   | Proton chemical shift difference between sites B and C (3-site)   | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Delta\omega_{AC}^H$ | $\Delta\omega_{AB}^H + \Delta\omega_{BC}^H$ | Proton chemical shift difference between sites A and C (3-site)   | $\text{rad.s}^{-1}$ (stored as ppm)                        |
| $\Phi_{ex}$           | $p_A p_B \Delta\omega^2$                    | Fast exchange factor  | $\text{rad}^2.\text{s}^{-2}$ (stored as ppm <sup>2</sup> ) |
| $\Phi_{ex,B}$         | See 10.12a on page 150                      | Fast exchange factor between sites A and B                        | $\text{rad}^2.\text{s}^{-2}$ (stored as ppm <sup>2</sup> ) |
| $\Phi_{ex,C}$         | See 10.12b on page 150                      | Fast exchange factor between sites A and C                        | $\text{rad}^2.\text{s}^{-2}$ (stored as ppm <sup>2</sup> ) |

## 10.2 The base dispersion models

### 10.2.1 The R2eff model

This is the simplest of all models in that the dispersion component of the base data – the peak intensity values – is not modelled. It is used to determine either the  $R_{2\text{eff}}$  or  $R_{1\rho}$  values and errors as required for the base data for all other models. It can be selected by setting the model to ‘R2eff’. Depending on the experiment type, this model will be handled differently. The  $R_{2\text{eff}}/R_{1\rho}$  values determined can be later copied to the data pipes of the other dispersion models using the appropriate user functions.

#### Fixed relaxation period experiments

For the fixed relaxation time period CPMG-type experiments, the  $R_{2\text{eff}}/R_{1\rho}$  values are determined by direct calculation using the formula

$$R_{2\text{eff}}(\nu_{\text{CPMG}}) = -\frac{1}{T_{\text{relax}}} \cdot \ln \left( \frac{I_1(\nu_{\text{CPMG}})}{I_0} \right). \quad (10.2)$$

The values and errors are determined with a single call of the `calc` user function. The  $R_{1\rho}$  version of the equation is essentially the same:

$$R_{1\rho}(\omega_1) = -\frac{1}{T_{\text{relax}}} \cdot \ln \left( \frac{I_1(\omega_1)}{I_0} \right). \quad (10.3)$$

Errors are calculated using the formula

$$\sigma_{R_2} = \frac{1}{T_{\text{relax}}} \sqrt{\left( \frac{\sigma_{I_1}}{I_1(\omega_1)} \right)^2 + \left( \frac{\sigma_{I_0}}{I_0} \right)^2}. \quad (10.4)$$

In a number of publications, the error formula from [Ishima and Torchia \(2005\)](#) has been used. This is the collapse of Equation 10.4 by setting  $\sigma_{I_0}$  to zero:

$$\sigma_{R_2} = \frac{\sigma_{I_1}}{T_{\text{relax}} I_1(\omega_1)}. \quad (10.5)$$

This is not implemented in `relax` as it can be shown by simple simulation that the formula is incorrect (see Figure 10.1). This formula significantly underestimates the real errors. The use of the same  $I_0$  value for all dispersion points does not cause a decrease in the  $R_{2\text{eff}}$  error but rather a correlation in the errors.

#### Variable relaxation period experiments

For the variable relaxation time period type experiments, the  $R_{2\text{eff}}/R_{1\rho}$  values are determined by fitting to the simple two parameter exponential as in a  $R_1$  or  $R_2$  analysis. Both  $R_{2\text{eff}}/R_{1\rho}$  and the initial peak intensity  $I_0$  are optimised using the `minimise` user function for each exponential curve separately. Monte Carlo simulations are used to obtain the parameter errors.

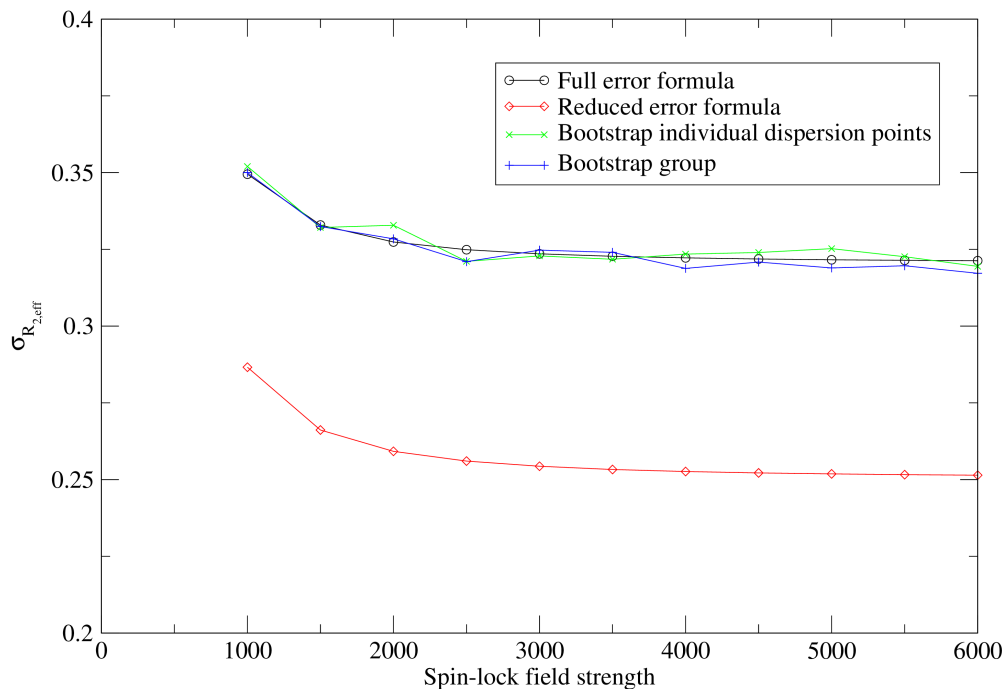


Figure 10.1: A demonstration of the inaccuracy of the error formula of Equation 10.5 from Ishima and Torchia (2005). This plot was generated using the script `test_suite/shared_data/dispersion/error_testing/simulation.py`. The bootstrapping simulation involves randomising noise-free  $I_0$  and  $I_1$  values for each dispersion data point assuming Gaussian errors. The full error formula is from Equation 10.4, the reduced error formula is from Equation 10.5, the bootstrapping using individual dispersion points estimates the errors assuming different  $I_0$  randomisations for each dispersion point and each simulation, and the bootstrapping group graph uses the same randomised  $I_0$  value for all dispersion points for each simulation.

### 10.2.2 The model for no chemical exchange relaxation

This model is provided for model selection purposes. In combination with frequentist methods, such as AIC, or Bayesian methods it can show if the presence of chemical exchange is statistically significant. Optimisation is still required as one  $R_2^0$  value per magnetic field strength will be fit to the measured data for each spin system. It is selected by setting the model to ‘No Rex’.

## 10.3 The analytic CPMG models

These are the analytic models designed for a single data type – the single quantum CPMG-type experiment.

### 10.3.1 The LM63 2-site fast exchange CPMG model

This is the original model for 2-site fast exchange for CPMG-type experiments. It is selected by setting the model to ‘LM63’, here named after [Luz and Meiboom \(1963\)](#). The original  $n$ -site Equation (7) from their paper can be written as

$$R_{\text{ex}} = \left[ 1 - 2\tau_{\text{ex}}g \cdot \tanh(2\tau_{\text{ex}}g)^{-1} \right] \cdot \tau_{\text{ex}} \cdot \sum_{i=2}^n p_i \Delta\omega_i, \quad (10.6)$$

where  $g$  is the pulse repetition rate defined as

$$g = 2\nu_{\text{CPMG}}. \quad (10.7)$$

It can be rearranged as

$$R_{\text{ex}} = \sum_{i=2}^n \frac{\Phi_{\text{ex},i}}{k_i} \cdot \left( 1 - \frac{4\nu_{\text{CPMG}}}{k_i} \cdot \tanh\left(\frac{k_i}{4\nu_{\text{CPMG}}}\right) \right). \quad (10.8)$$

The equation for the 2-site exchange process can be expressed as

$$R_{2\text{eff}} = R_2^0 + \frac{\Phi_{\text{ex}}}{k_{\text{ex}}} \cdot \left( 1 - \frac{4\nu_{\text{CPMG}}}{k_{\text{ex}}} \cdot \tanh\left(\frac{k_{\text{ex}}}{4\nu_{\text{CPMG}}}\right) \right). \quad (10.9)$$

The reference for this equation is:

- Luz, Z. and Meiboom, S. (1963). Nuclear magnetic resonance study of protolysis of trimethylammonium ion in aqueous solution - order of reaction with respect to solvent. *J. Chem. Phys.*, **39**(2), 366–370. ([10.1063/1.1734254](#))

### 10.3.2 The LM63 3-site fast exchange CPMG model

This is the original [Luz and Meiboom \(1963\)](#) model for 3-site fast exchange for CPMG-type experiments. It is selected by setting the model to ‘LM63 3-site’. Taking the original Equation 10.8, the equation for 3-site exchange is simply:

$$R_{\text{ex}} = \sum_{i=2}^3 \frac{\Phi_{\text{ex},i}}{k_i} \cdot \left( 1 - \frac{4\nu_{\text{CPMG}}}{k_i} \cdot \tanh\left(\frac{k_i}{4\nu_{\text{CPMG}}}\right) \right), \quad (10.10)$$

The reference for this equation is:

- Luz, Z. and Meiboom, S. (1963). Nuclear magnetic resonance study of protolysis of trimethylammonium ion in aqueous solution - order of reaction with respect to solvent. *J. Chem. Phys.*, **39**(2), 366–370. ([10.1063/1.1734254](#))

This model is only provided as a demonstration and should not be used for a normal analysis. Without data at multiple temperatures, a feature not currently supported within relax, that there are infinite lines of solutions and that the  $\Phi_{\text{ex,B}}$ ,  $\Phi_{\text{ex,C}}$ ,  $k_B$  and  $k_C$  parameters are all convoluted together.

This equation was made more practically relevant in the paper of [O'Connell et al. \(2009\)](#). This relies on the assumption that site 1 (or A) has a much larger equilibrium population than the other sites ( $p_A \gg p_B$  and  $p_A \gg p_C$ ). As stated, “if the different values of  $j_i$  are well-separated (by a factor of 3-10), then Eq. 3 reduces approximately to the sum of  $n - 1$  independent two-state processes for exchange between site 1 and the  $n - 1$  other sites”. In this situation, the following relationships hold

$$k_B \approx k_{\text{ex}}^{\text{AB}} = k_{\text{AB}} + k_{\text{BA}}, \quad (10.11\text{a})$$

$$k_C \approx k_{\text{ex}}^{\text{AC}} = k_{\text{AC}} + k_{\text{CA}}, \quad (10.11\text{b})$$

and

$$\Phi_{\text{ex,B}} = \overline{\Phi_{\text{ex}}} \frac{(k_{\text{ex}}^{\text{AB}})^2 (\overline{k_{\text{ex}}} - k_{\text{ex}}^{\text{AC}})}{k_{\text{ex}}^2 (k_{\text{ex}} - k_{\text{ex}}^{\text{AC}})}, \quad (10.12\text{a})$$

$$\Phi_{\text{ex,C}} = \overline{\Phi_{\text{ex}}} \frac{(k_{\text{ex}}^{\text{AC}})^2 (\overline{k_{\text{ex}}} - k_{\text{ex}}^{\text{AB}})}{k_{\text{ex}}^2 (k_{\text{ex}} - k_{\text{ex}}^{\text{AB}})}, \quad (10.12\text{b})$$

with

$$\overline{\Phi_{\text{ex,B}}} \approx (p_A + p_C) p_B \Delta \omega_{\text{AB}}^2, \quad (10.13\text{a})$$

$$\overline{\Phi_{\text{ex,C}}} \approx (p_A + p_B) p_C \Delta \omega_{\text{AC}}^2. \quad (10.13\text{b})$$

The parameter deconvolutions for this model can be performed after a relax analysis, if desired.

### 10.3.3 The full CR72 2-site CPMG model

This is the model for 2-site exchange on most times scales (with the constraint that  $p_A > p_B$ ), named after [Carver and Richards \(1972\)](#). It is selected by setting the model to ‘CR72 full’. The equation is

$$R_{2\text{eff}} = \frac{1}{2} \left( R_{2A}^0 + R_{2B}^0 + k_{\text{ex}} - 2\nu_{\text{CPMG}} \cosh^{-1} \left( D_+ \cosh(\eta_+) - D_- \cos(\eta_-) \right) \right), \quad (10.14)$$

where

$$D_{\pm} = \frac{1}{2} \left( \pm 1 + \frac{\Psi + 2\Delta\omega^2}{\sqrt{\Psi^2 + \zeta^2}} \right), \quad (10.15)$$

$$\eta_{\pm} = 2^{\frac{2}{3}} \frac{1}{\nu_{\text{CPMG}}} \left( \pm \Psi + \sqrt{\Psi^2 + \zeta^2} \right)^{\frac{1}{2}}, \quad (10.16)$$

$$\Psi = (R_{2A}^0 - R_{2B}^0 - p_A k_{\text{ex}} + p_B k_{\text{ex}})^2 - \Delta\omega^2 + 4p_A p_B k_{\text{ex}}^2, \quad (10.17)$$

$$\zeta = 2\Delta\omega (R_{2A}^0 - R_{2B}^0 - p_A k_{\text{ex}} + p_B k_{\text{ex}}). \quad (10.18)$$

This model is not accurate when the motional process is very slow. In that case, the ‘TSMFK01’ model in Section 10.3.6 on page 152 should be used instead.

The reference for this equation is:

- Carver, J. and Richards, R. (1972). General 2-site solution for chemical exchange produced dependence of T2 upon Carr-Purcell pulse separation. *J. Magn. Reson.*, 6(1), 89–105. ([10.1016/0022-2364\(72\)90090-X](https://doi.org/10.1016/0022-2364(72)90090-X))

### 10.3.4 The reduced CR72 2-site CPMG model

This is the model for 2-site exchange on most times scales (with the constraint that  $p_A > p_B$ ), named after [Carver and Richards \(1972\)](#). It is selected by setting the model to ‘CR72’. It is the same as the full CR72 model described above, but with the simplification that  $R_{2A}^0 = R_{2B}^0$ . This simplifies the equations to

$$R_{2\text{eff}} = R_2^0 + \frac{k_{\text{ex}}}{2} - \nu_{\text{CPMG}} \cosh^{-1} (D_+ \cosh(\eta_+) - D_- \cosh(\eta_-)), \quad (10.19)$$

where  $D_{\pm}$  and  $\eta_{\pm}$  are unchanged and

$$\Psi = k_{\text{ex}}^2 - \Delta\omega^2, \quad (10.20)$$

$$\zeta = -2\Delta\omega(p_A k_{\text{ex}} - p_B k_{\text{ex}}). \quad (10.21)$$

As mentioned in the ‘CR72 full’ model section, this model is not accurate when the motional process is very slow. In that case please use the ‘TSMFK01’ model in Section 10.3.6 on page 152 instead.

### 10.3.5 The IT99 2-site CPMG model

This is the model for 2-site exchange on all times scales (with the constraint that  $p_A \gg p_B$ ), named after [Ishima and Torchia \(1999\)](#). It is selected by setting the model to ‘IT99’. The equation is:

$$R_{\text{ex}} \simeq \frac{\Phi_{\text{ex}} \tau_{\text{ex}}}{1 + \omega_a^2 \tau_{\text{ex}}^2}, \quad (10.22)$$

$$\omega_a^2 = \sqrt{\omega_{1\text{eff}}^4 + p_A^2 \Delta\omega^4}, \quad (10.23)$$

$$R_{2\text{eff}} = R_2^0 + R_{\text{ex}}. \quad (10.24)$$

The effective rotating frame field for a CPMG-type experiment is given by

$$\omega_{1\text{eff}} = 4\sqrt{3}\nu_{\text{CPMG}}, \quad (10.25)$$

and hence

$$\omega_{1\text{eff}}^4 = 2304\nu_{\text{CPMG}}^4. \quad (10.26)$$

The reference for this equation is:

- Ishima, R. and Torchia, D. (1999). Estimating the time scale of chemical exchange of proteins from measurements of transverse relaxation rates in solution. *J. Biomol. NMR*, **14**(4), 369–372. ([10.1023/A:1008324025406](https://doi.org/10.1023/A:1008324025406))

### 10.3.6 The TSMFK01 2-site CPMG model

This is the model for 2-site very-slow exchange model for time scales within range of microsecond to second time scale, where  $p_A \gg p_B$ , and named after [Tollinger et al. \(2001\)](#). It is selected by setting the model to ‘TSMFK01’. A particularly interesting feature of the dispersion curves is the damped oscillations, which occur at low CPMG field strengths, and is solely a function of the chemical shift difference between the two sites (i.e., independent of the rate of exchange).

The equation is:

$$R_{2\text{eff}} = R_{2A}^0 + k_{AB} - k_{AB} \frac{\sin(\Delta\omega \cdot \tau_{\text{CPMG}})}{\Delta\omega \cdot \tau_{\text{CPMG}}} \quad (10.27)$$

The reference for this equation is:

- Tollinger, M., Skrynnikov, N. R., Mulder, F. A. A., Forman-Kay, J. D., and Kay, L. E. (2001). Slow dynamics in folded and unfolded states of an sh3 domain. *J. Am. Chem. Soc.*, **123**(46), 11341–11352. ([10.1021/ja011300z](https://doi.org/10.1021/ja011300z))

## 10.4 The numeric CPMG models

These are the numeric models designed for a single data type – the single quantum CPMG-type experiment.

### 10.4.1 The NS 2-site expanded CPMG model

This is the numerical model for 2-site exchange expanded using Maple by Nikolai Skrynnikov. It is selected by setting the model to ‘NS CPMG 2-site expanded’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces.

This model will give the same results as the other numerical solutions whereby  $R_{2A}^0 = R_{2B}^0$ . The following is the set of equations of the expansion used in relax. It has been modified from the original for speed. See the `lib.dispersion.ns_cpmg_2site_expanded` module for more details including the original code. Further simplifications can be found in the



code.

$$t_3 = \iota, \quad (10.28.1)$$

$$t_4 = t_3 \Delta\omega, \quad (10.28.2)$$

$$t_5 = k_{BA}^2, \quad (10.28.3)$$

$$t_8 = 2t_4 k_{BA}, \quad (10.28.4)$$

$$t_{10} = 2k_{BA} k_{AB}, \quad (10.28.5)$$

$$t_{11} = \Delta\omega^2, \quad (10.28.6)$$

$$t_{14} = 2t_4 k_{AB}, \quad (10.28.7)$$

$$t_{15} = k_{AB}^2, \quad (10.28.8)$$

$$t_{17} = \sqrt{t_5 - t_8 + t_{10} - t_{11} + t_{14} + t_{15}}, \quad (10.28.9)$$

$$t_{21} = \exp\left(\frac{(-k_{BA} + t_4 - k_{AB} + t_{17})\tau_{\text{CPMG}}}{2}\right), \quad (10.28.10)$$

$$t_{22} = \frac{1}{t_{17}}, \quad (10.28.11)$$

$$t_{28} = \exp\left(\frac{(-k_{BA} + t_4 - k_{AB} - t_{17})\tau_{\text{CPMG}}}{2}\right), \quad (10.28.12)$$

$$t_{31} = t_{22} k_{AB} (t_{21} - t_{28}), \quad (10.28.13)$$

$$t_{33} = \sqrt{t_5 + t_8 + t_{10} - t_{11} - t_{14} + t_{15}}, \quad (10.28.14)$$

$$t_{34} = k_{BA} + t_4 - k_{AB} + t_{33}, \quad (10.28.15)$$

$$t_{37} = \exp((-k_{BA} - t_4 - k_{AB} + t_{33})\tau_{\text{CPMG}}), \quad (10.28.16)$$

$$t_{39} = \frac{1}{t_{33}}, \quad (10.28.17)$$

$$t_{41} = k_{BA} + t_4 - k_{AB} - t_{33}, \quad (10.28.18)$$

$$t_{44} = \exp((-k_{BA} - t_4 - k_{AB} - t_{33})\tau_{\text{CPMG}}), \quad (10.28.19)$$

$$t_{47} = \frac{t_{39}}{2} (t_{34} t_{37} - t_{41} t_{44}), \quad (10.28.20)$$

$$t_{49} = k_{BA} - t_4 - k_{AB} - t_{17}, \quad (10.28.21)$$

$$t_{51} = t_{21} t_{49} t_{22}, \quad (10.28.22)$$

$$t_{52} = k_{BA} - t_4 - k_{AB} + t_{17}, \quad (10.28.23)$$

$$t_{54} = t_{28} t_{52} t_{22}, \quad (10.28.24)$$

$$t_{55} = t_{54} - t_{51}, \quad (10.28.25)$$

$$t_{60} = \frac{1}{2} t_{39} k_{AB} (t_{37} - t_{44}), \quad (10.28.26)$$

$$t_{62} = t_{31} t_{47} + t_{55} t_{60}, \quad (10.28.27)$$

$$t_{63} = \frac{1}{k_{AB}}, \quad (10.28.28)$$

$$t_{68} = \frac{t_{63}}{2} (t_{49} t_{54} - t_{52} t_{51}), \quad (10.28.29)$$

$$t_{69} = \frac{t_{62} t_{68}}{2}, \quad (10.28.30)$$

$$t_{72} = t_{37} t_{41} t_{39}, \quad (10.28.31)$$

$$t_{76} = t_{44}t_{34}t_{39}, \quad (10.28.32)$$

$$t_{78} = \frac{t_{63}}{2} (t_{41}t_{76} - t_{34}t_{72}), \quad (10.28.33)$$

$$t_{80} = \frac{1}{2}(t_{76} - t_{72}), \quad (10.28.34)$$

$$t_{82} = \frac{1}{2}(t_{31}t_{78} + t_{55}t_{80}), \quad (10.28.35)$$

$$t_{83} = \frac{t_{82}t_{55}}{2}, \quad (10.28.36)$$

$$t_{88} = \frac{t_{22}}{2} (t_{52}t_{21} - t_{49}t_{28}), \quad (10.28.37)$$

$$t_{91} = t_{88}t_{47} + t_{68}t_{60}, \quad (10.28.38)$$

$$t_{92} = t_{91}t_{88}, \quad (10.28.39)$$

$$t_{95} = \frac{1}{2}(t_{88}t_{78} + t_{68}t_{80}), \quad (10.28.40)$$

$$t_{96} = t_{95}t_{31}, \quad (10.28.41)$$

$$t_{97} = t_{69} + t_{83}, \quad (10.28.42)$$

$$t_{98} = t_{97}^2, \quad (10.28.43)$$

$$t_{99} = t_{92} + t_{96}, \quad (10.28.44)$$

$$t_{102} = t_{99}^2, \quad (10.28.45)$$

$$t_{108} = t_{62}t_{88} + t_{82}t_{31}, \quad (10.28.46)$$

$$t_{112} = \sqrt{t_{98} - 2t_{99}t_{97} + t_{102} + 2(t_{91}t_{68} + t_{95}t_{55})t_{108}}, \quad (10.28.47)$$

$$t_{113} = t_{97} - t_{99} - t_{112}, \quad (10.28.48)$$

$$t_{115} = n_{\text{CPMG}}, \quad (10.28.49)$$

$$t_{116} = \left( \frac{t_{97} + t_{99} + t_{112}}{2} \right)^{t_{115}}, \quad (10.28.50)$$

$$t_{118} = \frac{1}{t_{112}}, \quad (10.28.51)$$

$$t_{120} = t_{97} - t_{99} + t_{112}, \quad (10.28.52)$$

$$t_{122} = \left( \frac{t_{97} + t_{99} - t_{112}}{2} \right)^{t_{115}}, \quad (10.28.53)$$

$$t_{127} = \frac{1}{2t_{108}}, \quad (10.28.54)$$

$$t_{139} = \frac{1}{2(k_{\text{AB}} + k_{\text{BA}})} \left[ (t_{120}t_{122} - t_{113}t_{116})t_{118}k_{\text{BA}} \right. \\ \left. + (t_{120}t_{122} - t_{116}t_{120})t_{113}t_{118}t_{127}k_{\text{AB}} \right]. \quad (10.28.55)$$

The relative peak intensities, magnetisation, and effective  $R_2$  relaxation rate are calculated as

$$I_0 = p_{\text{A}}, \quad (10.29\text{a})$$

$$I_1 = \Re(t_{139}) \exp(-T_{\text{relax}}R_2^0), \quad (10.29\text{b})$$

$$M_x = I_1/I_0, \quad (10.29\text{c})$$

$$R_{2\text{eff}} = -\frac{1}{T_{\text{relax}}} \cdot \ln(M_x). \quad (10.29\text{d})$$

In these equations  $\tau_{\text{CPMG}}$  and  $n_{\text{CPMG}}$  are numpy arrays and hence  $t_{139}$  is also a numpy array. This avoids a Python loop over the dispersion points until the very end of the calculation, required to populate the  $R_{2\text{eff}}$  data structure, resulting in very fast calculations.

The reference for this model is:

- Tollinger, M., Skrynnikov, N. R., Mulder, F. A. A., Forman-Kay, J. D., and Kay, L. E. (2001). Slow dynamics in folded and unfolded states of an sh3 domain. *J. Am. Chem. Soc.*, **123**(46), 11341–11352. ([10.1021/ja011300z](https://doi.org/10.1021/ja011300z))

#### 10.4.2 The full NS 2-site 3D CPMG model

This is the numerical model for 2-site exchange using 3D magnetisation vectors. It is selected by setting the model to ‘NS CPMG 2-site 3D full’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces.

#### 10.4.3 The reduced NS 2-site 3D CPMG model

This is the numerical model for 2-site exchange using 3D magnetisation vectors, whereby the simplification  $R_{2A}^0 = R_{2B}^0$  is assumed. It is selected by setting the model to ‘NS CPMG 2-site 3D’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces.

#### 10.4.4 The full NS 2-site star CPMG model

This is the numerical model for 2-site exchange using complex conjugate matrices. It is selected by setting the model to ‘NS CPMG 2-site star full’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces.

#### 10.4.5 The reduced NS 2-site star CPMG model

This is the numerical model for 2-site exchange using complex conjugate matrices, whereby the simplification  $R_{2A}^0 = R_{2B}^0$  is assumed. It is selected by setting the model to ‘NS CPMG 2-site star’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces.

### 10.5 The analytic MMQ CPMG models

These are the analytic models designed for handling combined proton-heteronuclear SQ, ZQ, DQ, and MQ CPMG-type experiments. This data combination is labelled as multiple multiple quantum data or MMQ.

### 10.5.1 The MMQ CR72 model

This is the analytic CR72 model for 2-site exchange on most times scales (Section 10.3.4 on page 151) extended for multiple types of multiple quantum data (MMQ) by Korzhnev et al. (2004a). It is selected by setting the model to ‘MMQ CR72’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces. The equation for the exchange process is

$$R_{2\text{eff}} = \Re(\lambda_1) - \frac{1}{T_{\text{relax}}} \ln(Q), \quad (10.30)$$

where

$$\lambda_1 = R_{2,\text{MQ}}^0 + \frac{k_{\text{ex}}}{2} - \nu_{\text{CPMG}} \cosh^{-1}(D_+ \cosh(\eta_+) - D_- \cos(\eta_-)), \quad (10.31)$$

$$D_{\pm} = \frac{1}{2} \left( \pm 1 + \frac{\Psi + 2\Delta\omega^2}{\sqrt{\Psi^2 + \zeta^2}} \right), \quad (10.32)$$

$$\eta_{\pm} = 2^{\frac{2}{3}} \frac{1}{\nu_{\text{CPMG}}} \left( \pm \Psi + \sqrt{\Psi^2 + \zeta^2} \right)^{\frac{1}{2}}, \quad (10.33)$$

$$\Psi = (i\Delta\omega^H + p_A k_{\text{ex}} - p_B k_{\text{ex}})^2 - \Delta\omega^2 + 4p_A p_B k_{\text{ex}}^2, \quad (10.34)$$

$$\zeta = -2\Delta\omega (i\Delta\omega^H + p_A k_{\text{ex}} - p_B k_{\text{ex}}), \quad (10.35)$$

and where

$$Q = \Re \left( 1 - m_{D+}^2 + m_{D+} m_{Z+} - m_{Z+}^2 + \frac{m_{D+} + m_{Z+}}{2} \sqrt{\frac{p_B}{p_A}} \right), \quad (10.36)$$

and

$$m_{D\pm} = \pm \frac{i k_{\text{ex}} \sqrt{p_A p_B}}{d_{\pm} z_{\pm}} \left( z_{\pm} + 2\Delta\omega \frac{\sin(z_{\pm} \delta)}{\sin((d_{\pm} + z_{\pm}) \delta)} \right), \quad (10.37)$$

$$m_{Z\mp} = \pm \frac{i k_{\text{ex}} \sqrt{p_A p_B}}{d_{\pm} z_{\pm}} \left( d_{\pm} - 2\Delta\omega \frac{\sin(d_{\pm} \delta)}{\sin((d_{\pm} + z_{\pm}) \delta)} \right), \quad (10.38)$$

and

$$d_{\pm} = (\Delta\omega^H + \Delta\omega) \pm i k_{\text{ex}}, \quad (10.39)$$

$$z_{\pm} = (\Delta\omega^H - \Delta\omega) \pm i k_{\text{ex}}. \quad (10.40)$$

The symbol  $\delta$  is half of  $\tau_{\text{CPMG}}$  or

$$\delta = \frac{1}{4\nu_{\text{CPMG}}}. \quad (10.41)$$

The references for this model are:

- Korzhnev, D. M., Kloiber, K., Kanelis, V., Tugarinov, V., and Kay, L. E. (2004a). Probing slow dynamics in high molecular weight proteins by methyl-TROSY NMR spectroscopy: application to a 723-residue enzyme. *J. Am. Chem. Soc.*, **126**(12), 3964–3973. ([10.1021/ja039587i](https://doi.org/10.1021/ja039587i))

- Korzhnev, D. M., Kloiber, K., and Kay, L. E. (2004b). Multiple-quantum relaxation dispersion NMR spectroscopy probing millisecond time-scale dynamics in proteins: theory and application. *J. Am. Chem. Soc.*, **126**(23), 7320–7329. ([10.1021/ja049968b](https://doi.org/10.1021/ja049968b))
- Korzhnev, D. M., Neudecker, P., Mittermaier, A., Orekhov, V. Y., and Kay, L. E. (2005a). Multiple-site exchange in proteins studied with a suite of six NMR relaxation dispersion experiments: an application to the folding of a Fyn SH3 domain mutant. *J. Am. Chem. Soc.*, **127**(44), 15602–15611. ([10.1021/ja054550e](https://doi.org/10.1021/ja054550e))

## 10.6 The numeric MMQ CPMG models

These are the numeric models designed for handling combined proton-heteronuclear SQ, ZQ, DQ, and MQ CPMG-type experiments. This data combination is labelled as multiple multiple quantum data or MMQ.

### 10.6.1 The NS MMQ 2-site model

This is the numerical model for 2-site exchange for proton-heteronuclear SQ, ZQ, DQ and MQ CPMG data, as derived in ([Korzhnev et al., 2004a,b, 2005a](#)). It is selected by setting the model to ‘NS MMQ 2-site’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces. Different sets of equations are used for the different data types.

#### The SQ, ZD and DQ equations

The basic evolution matrices for single, zero and double quantum CPMG-type data for this model are

$$R_{2\text{eff}} = -\frac{1}{T_{\text{relax}}} \log \frac{\mathbf{M}_A(T_{\text{relax}})}{\mathbf{M}_A(0)}, \quad (10.42)$$

where  $\mathbf{M}_A(0)$  is proportional to the vector  $[p_A, p_B]^T$  and

$$\mathbf{M}_A(T_{\text{relax}}) = (\mathbf{A}_{\pm} \mathbf{A}_{\mp} \mathbf{A}_{\mp} \mathbf{A}_{\pm})^n \mathbf{M}_A(0) \quad (10.43)$$

The evolution matrix  $\mathbf{A}$  is defined as

$$\mathbf{A}_{\pm} = e^{\mathbf{a}_{\pm} \cdot \tau_{\text{CPMG}}}, \quad (10.44)$$

where

$$\mathbf{a}_{\pm} = \begin{pmatrix} -k_{AB} - R_{2A}^0 & k_{BA} \\ k_{AB} & -k_{BA} \pm i\Delta\omega - R_{2B}^0 \end{pmatrix}. \quad (10.45)$$

For different data types  $\Delta\omega$  is defined as:  $\Delta\omega$  ( $^{15}\text{N}$  SQ-type data);  $\Delta\omega^{\text{H}}$  ( $^1\text{H}$  SQ-type data);  $\Delta\omega^{\text{H}} - \Delta\omega$  (ZQ-type data); and  $\Delta\omega^{\text{H}} + \Delta\omega$  (DQ-type data).

### The MQ equations

The equation for the exchange process for multiple quantum CPMG-type data is

$$R_{2\text{eff}} = -\frac{1}{T} \log \left\{ \text{Re} \left[ \frac{0.5}{p_A} \begin{pmatrix} 1 & 0 \end{pmatrix} \cdot (\mathbf{A}\mathbf{B} + \mathbf{C}\mathbf{D}) \cdot \begin{pmatrix} p_A \\ p_B \end{pmatrix} \right] \right\}, \quad (10.46)$$

where  $T$  is the constant time interval, and the matrices  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$ , and  $\mathbf{D}$  are differentially defined. When  $n$  is even, they are defined as

$$\mathbf{A} = (\mathbf{M}_1 \mathbf{M}_2 \mathbf{M}_2 \mathbf{M}_1)^{\frac{n}{2}}, \quad (10.47a)$$

$$\mathbf{B} = (\mathbf{M}_2^* \mathbf{M}_1^* \mathbf{M}_1^* \mathbf{M}_2^*)^{\frac{n}{2}}, \quad (10.47b)$$

$$\mathbf{C} = (\mathbf{M}_2 \mathbf{M}_1 \mathbf{M}_1 \mathbf{M}_2)^{\frac{n}{2}}, \quad (10.47c)$$

$$\mathbf{D} = (\mathbf{M}_1^* \mathbf{M}_2^* \mathbf{M}_2^* \mathbf{M}_1^*)^{\frac{n}{2}}. \quad (10.47d)$$

When  $n$  is odd, they are defined as

$$\mathbf{A} = (\mathbf{M}_1 \mathbf{M}_2 \mathbf{M}_2 \mathbf{M}_1)^{\frac{n-1}{2}} \mathbf{M}_1 \mathbf{M}_2, \quad (10.48a)$$

$$\mathbf{B} = (\mathbf{M}_1^* \mathbf{M}_2^* \mathbf{M}_2^* \mathbf{M}_1^*)^{\frac{n-1}{2}} \mathbf{M}_1^* \mathbf{M}_2^*, \quad (10.48b)$$

$$\mathbf{C} = (\mathbf{M}_2 \mathbf{M}_1 \mathbf{M}_1 \mathbf{M}_2)^{\frac{n-1}{2}} \mathbf{M}_2 \mathbf{M}_1, \quad (10.48c)$$

$$\mathbf{D} = (\mathbf{M}_2^* \mathbf{M}_1^* \mathbf{M}_1^* \mathbf{M}_2^*)^{\frac{n-1}{2}} \mathbf{M}_2^* \mathbf{M}_1^*. \quad (10.48d)$$

When  $n$  is zero, to avoid matrix powers of zero they are defined as

$$\mathbf{A} = \mathbf{M}_1 \mathbf{M}_2, \quad (10.49a)$$

$$\mathbf{B} = \mathbf{M}_1^* \mathbf{M}_2^*, \quad (10.49b)$$

$$\mathbf{C} = \mathbf{M}_2 \mathbf{M}_1, \quad (10.49c)$$

$$\mathbf{D} = \mathbf{M}_2^* \mathbf{M}_1^*. \quad (10.49d)$$

The  $\mathbf{M}$  matrices are defined as:

$$\mathbf{M}_j = \exp(\mathbf{m}_j \delta), \quad (10.50)$$

where  $2\delta$  is the spacing between successive  $180^\circ$  pulses and where The references for this model are:

$$\mathbf{m}_1 = \begin{pmatrix} -p_B k_{\text{ex}} - R_{2,\text{DQ}}^A & p_A k_{\text{ex}} \\ p_B k_{\text{ex}} & -p_A k_{\text{ex}} - i(\Delta\omega^H + \Delta\omega) - R_{2,\text{DQ}}^B \end{pmatrix}, \quad (10.51a)$$

$$\mathbf{m}_2 = \begin{pmatrix} -p_B k_{\text{ex}} - R_{2,\text{ZQ}}^A & p_A k_{\text{ex}} \\ p_B k_{\text{ex}} & -p_A k_{\text{ex}} - i(\Delta\omega^H - \Delta\omega) - R_{2,\text{ZQ}}^B \end{pmatrix}. \quad (10.51b)$$

For the model it is assumed that  $R_{2,\text{DQ}}^A = R_{2,\text{ZQ}}^A = R_{2A}^0$  and  $R_{2,\text{DQ}}^B = R_{2,\text{ZQ}}^B = R_{2B}^0$ . The references for this model are:

- Korzhnev, D. M., Kloiber, K., Kanelis, V., Tugarinov, V., and Kay, L. E. (2004a). Probing slow dynamics in high molecular weight proteins by methyl-TROSY NMR spectroscopy: application to a 723-residue enzyme. *J. Am. Chem. Soc.*, **126**(12), 3964–3973. ([10.1021/ja039587i](https://doi.org/10.1021/ja039587i))
- Korzhnev, D. M., Kloiber, K., and Kay, L. E. (2004b). Multiple-quantum relaxation dispersion NMR spectroscopy probing millisecond time-scale dynamics in proteins: theory and application. *J. Am. Chem. Soc.*, **126**(23), 7320–7329. ([10.1021/ja049968b](https://doi.org/10.1021/ja049968b))
- Korzhnev, D. M., Neudecker, P., Mittermaier, A., Orekhov, V. Y., and Kay, L. E. (2005a). Multiple-site exchange in proteins studied with a suite of six NMR relaxation dispersion experiments: an application to the folding of a Fyn SH3 domain mutant. *J. Am. Chem. Soc.*, **127**(44), 15602–15611. ([10.1021/ja054550e](https://doi.org/10.1021/ja054550e))

### 10.6.2 The NS MMQ 3-site linear model

This is the numerical model for 3-site exchange for proton-heteronuclear SQ, ZQ, DQ and MQ CPMG data, as derived in ([Korzhnev et al., 2004a,b, 2005a](#)). As this model is linear, the assumption that  $k_{AC} = k_{CA} = 0$  has been made. To simplify the optimisation space for the model, the assumption  $R_{2A}^0 = R_{2B}^0 = R_{2C}^0 = R_2^0$  has also been made.

#### The SQ, ZD and DQ equations

The basic evolution matrices for single, zero and double quantum CPMG-type data for this model are

$$\mathbf{A}_{\pm} = e^{\mathbf{a}_{\pm} \cdot \tau_{\text{CPMG}}}, \quad (10.52)$$

where

$$\mathbf{a}_{\pm} = \begin{pmatrix} -k_{AB} & & k_{BA} & 0 \\ k_{AB} & -k_{BA} - k_{BC} \pm i\Delta\omega_{AB} & k_{CB} \\ 0 & k_{BC} & -k_{CB} \pm i\Delta\omega_{AC} \end{pmatrix} - \begin{pmatrix} R_{2A}^0 & 0 & 0 \\ 0 & R_{2B}^0 & 0 \\ 0 & 0 & R_{2C}^0 \end{pmatrix}. \quad (10.53)$$

#### The MQ equations

The formulae for multiple quantum CPMG-type data are the same as for the ‘NS MMQ 2-site’ model except for the  $R_{2\text{eff}}$  calculation and the  $\mathbf{m}_j$  matrices. The rate is calculated as

$$R_{2\text{eff}} = -\frac{1}{T} \log \left\{ \text{Re} \left[ \frac{0.5}{p_A} (1 \ 0 \ 0) \cdot (\mathbf{AB} + \mathbf{CD}) \cdot \begin{pmatrix} p_A \\ p_B \\ p_C \end{pmatrix} \right] \right\}. \quad (10.54)$$

The  $\mathbf{m}_j$  matrices are

$$\mathbf{m}_1 = \begin{pmatrix} -k_{AB} & k_{BA} & 0 \\ k_{AB} & -k_{BA} - k_{BC} - i(\Delta\omega_{AB}^H + \Delta\omega_{AB}) & k_{CB} \\ 0 & k_{BC} & -k_{CB} - i(\Delta\omega_{AC}^H + \Delta\omega_{AC}) \end{pmatrix} - \begin{pmatrix} R_{2A}^0 & 0 & 0 \\ 0 & R_{2B}^0 & 0 \\ 0 & 0 & R_{2C}^0 \end{pmatrix}, \quad (10.55a)$$

$$\mathbf{m}_2 = \begin{pmatrix} -k_{AB} & k_{BA} & 0 \\ k_{AB} & -k_{BA} - k_{BC} - i(\Delta\omega_{AB}^H - \Delta\omega_{AB}) & k_{CB} \\ 0 & k_{BC} & -k_{CB} - i(\Delta\omega_{AC}^H - \Delta\omega_{AC}) \end{pmatrix} - \begin{pmatrix} R_{2A}^0 & 0 & 0 \\ 0 & R_{2B}^0 & 0 \\ 0 & 0 & R_{2C}^0 \end{pmatrix}. \quad (10.55b)$$

For the model, the assumption  $R_{2A}^0 = R_{2B}^0 = R_{2C}^0 = R_2^0$  is made.

### 10.6.3 The NS MMQ 3-site model

This is the numerical model for 3-site exchange for proton-heteronuclear SQ, ZQ, DQ and MQ CPMG data, as derived in (Korzhnev et al., 2004a,b, 2005a). However it has been extended to allow the  $A \leftrightarrow C$  transition. To simplify the optimisation space for the model as in the ‘NS MMQ 3-site linear’ model, the assumption  $R_{2A}^0 = R_{2B}^0 = R_{2C}^0 = R_2^0$  has been made.

#### The SQ, ZD and DQ equations

The basic evolution matrices for single, zero and double quantum CPMG-type data for this model are

$$\mathbf{A}_{\pm} = e^{\mathbf{a}_{\pm} \cdot \tau_{\text{CPMG}}}, \quad (10.56)$$

where

$$\mathbf{a}_{\pm} = \begin{pmatrix} -k_{AB} - k_{AC} & k_{BA} & k_{CA} \\ k_{AB} & -k_{BA} - k_{BC} \pm i\Delta\omega_{AB} & k_{CB} \\ k_{AC} & k_{BC} & -k_{CB} - k_{CA} \pm i\Delta\omega_{AC} \end{pmatrix} - \begin{pmatrix} R_{2A}^0 & 0 & 0 \\ 0 & R_{2B}^0 & 0 \\ 0 & 0 & R_{2C}^0 \end{pmatrix}. \quad (10.57)$$



### The MQ equations

The  $\mathbf{m}_j$  matrices for this model are

$$\mathbf{m}_1 = \begin{pmatrix} -k_{AB} - k_{AC} & k_{BA} & k_{CA} \\ k_{AB} & -k_{BA} - k_{BC} - i(\Delta\omega_{AB}^H + \Delta\omega_{AB}) & k_{CB} \\ k_{AC} & k_{BC} & -k_{CB} - k_{CA} - i(\Delta\omega_{AC}^H + \Delta\omega_{AC}) \end{pmatrix} - \begin{pmatrix} R_{2A}^0 & 0 & 0 \\ 0 & R_{2B}^0 & 0 \\ 0 & 0 & R_{2C}^0 \end{pmatrix}, \quad (10.58a)$$

$$\mathbf{m}_2 = \begin{pmatrix} -k_{AB} - k_{AC} & k_{BA} & k_{CA} \\ k_{AB} & -k_{BA} - k_{BC} - i(\Delta\omega_{AB}^H - \Delta\omega_{AB}) & k_{CB} \\ k_{AC} & k_{BC} & -k_{CB} - k_{CA} - i(\Delta\omega_{AC}^H - \Delta\omega_{AC}) \end{pmatrix} - \begin{pmatrix} R_{2A}^0 & 0 & 0 \\ 0 & R_{2B}^0 & 0 \\ 0 & 0 & R_{2C}^0 \end{pmatrix}. \quad (10.58b)$$

## 10.7 The analytic $R_{1\rho}$ models

These are the analytic models designed for  $R_{1\rho}$ -type experiments.

### 10.7.1 The M61 2-site fast exchange $R_{1\rho}$ model

This is the model for 2-site fast exchange for on-resonance  $R_{1\rho}$ -type data. It is selected by setting the model to ‘M61’, here named after [Meiboom \(1961\)](#). The equation for the exchange process is

$$R_{1\rho} = R'_{1\rho} + \frac{\Phi_{\text{ex}} k_{\text{ex}}}{k_{\text{ex}}^2 + \omega_e^2}. \quad (10.59)$$

The reference for this equation is:

- Meiboom, S. (1961). Nuclear magnetic resonance study of proton transfer in water. *J. Chem. Phys.*, **34**(2), 375–388. ([10.1063/1.1700960](#))

### 10.7.2 The M61 skew 2-site fast exchange $R_{1\rho}$ model

This is the second model for 2-site fast exchange for on-resonance  $R_{1\rho}$ -type data from [Meiboom \(1961\)](#). It is selected by setting the model to ‘M61 skew’. The equation for the exchange process is

$$R_{1\rho} = R'_{1\rho} + \frac{p_A^2 p_B \Delta\omega^2 k_{\text{ex}}}{k_{\text{ex}}^2 + p_A^2 \Delta\omega^2 + \omega_1^2}. \quad (10.60)$$

Care must be taken as this model appears to have infinite lines of solutions –  $p_A$  and  $\Delta\omega$  are convoluted. Hence this model is disabled in the dispersion auto-analysis.

### 10.7.3 The DPL94 2-site fast exchange $R_{1\rho}$ model

This is the model for 2-site fast exchange for  $R_{1\rho}$ -type data. It is selected by setting the model to ‘DPL94’, here named after [Davis et al. \(1994\)](#). It extends the [Meiboom \(1961\)](#) model to off-resonance data. The model collapses to the M61 model for on-resonance data. The equation for the exchange process is

$$R_{1\rho} = R_1 \cos^2 \theta + \left( R'_{1\rho} + \frac{\Phi_{\text{ex}} k_{\text{ex}}}{k_{\text{ex}}^2 + \omega_e^2} \right) \sin^2 \theta, \quad (10.61)$$

where  $\theta$  is the rotating frame tilt angle. The reference for this equation is:

- Davis, D., Perlman, M., and London, R. (1994). Direct measurements of the dissociation-rate constant for inhibitor-enzyme complexes via the T1rho and T2 (CPMG) methods. *J. Magn. Reson.*, **104**(3), 266–275. ([10.1006/jmrb.1994.1084](#))

### 10.7.4 The TP02 2-site exchange $R_{1\rho}$ model

This is the model for 2-site exchange for off-resonance  $R_{1\rho}$ -type data from [Trott and Palmer \(2002\)](#). It is selected by setting the model to ‘TP02’. The equation for the exchange process is

$$R_{1\rho} = R_1 \cos^2 \theta + R'_{1\rho} \sin^2 \theta + \frac{\sin^2 \theta p_A p_B \Delta \omega^2 k_{\text{ex}}}{\omega_{\text{Aeff}}^2 \omega_{\text{Beff}}^2 / \omega_{\text{eff}}^2 + k_{\text{ex}}^2}, \quad (10.62)$$

in which

$$\delta_A = \omega_A - \omega_{\text{rf}}, \quad (10.63a)$$

$$\delta_B = \omega_B - \omega_{\text{rf}}, \quad (10.63b)$$

$$\bar{\omega} = p_A \omega_A + p_B \omega_B, \quad (10.63c)$$

$$\bar{\Omega} = \bar{\omega} - \omega_{\text{rf}}, \quad (10.63d)$$

$$\omega_{\text{Aeff}}^2 = \omega_1^2 + \delta_A^2, \quad (10.63e)$$

$$\omega_{\text{Beff}}^2 = \omega_1^2 + \delta_B^2, \quad (10.63f)$$

$$\omega_{\text{eff}}^2 = \omega_1^2 + \bar{\Omega}^2, \quad (10.63g)$$

$$\theta = \arctan \left( \frac{\omega_1}{\bar{\Omega}} \right). \quad (10.63h)$$

The equation is accurate only when populations are highly skewed with  $p_A \gg p_B$ . And it is valid only for exchange processes which are not fast. Note that this model has been superseded by the ‘TAP03’ and ‘MP05’ models. The reference for this equation is:

- Trott, O. and Palmer, 3rd, A. G. (2002). R1rho relaxation outside of the fast-exchange limit. *J. Magn. Reson.*, **154**(1), 157–160. ([10.1006/jmre.2001.2466](#))

### 10.7.5 The TAP03 2-site exchange $R_{1\rho}$ model

This is the model for 2-site exchange for off-resonance  $R_{1\rho}$ -type data from [Trott et al. \(2003\)](#). It is selected by setting the model to ‘TAP03’. The equation for the exchange process is

$$R_{1\rho} = R_1 \cos^2 \theta + R'_{1\rho} \sin^2 \theta + \left( \frac{1}{\gamma} \right) \frac{\sin^2 \hat{\theta} p_A p_B \Delta \omega^2 k_{\text{ex}}}{\hat{\omega}_{\text{Aeff}}^2 \hat{\omega}_{\text{Beff}}^2 / \hat{\omega}_{\text{eff}}^2 + k_{\text{ex}}^2 - 2 \sin^2 \hat{\theta} p_A p_B \Delta \omega^2 + (1 - \gamma) \omega_1^2}, \quad (10.64)$$

in which, in addition to those parameters defined above for the ‘TP02’ model,

$$\sigma = p_B \delta_A + p_A \delta_B, \quad (10.65a)$$

$$\gamma = 1 - p_A p_B \Delta \omega^2 \frac{\sigma^2 - k_{\text{ex}}^2 + \omega_1^2}{(\sigma^2 + k_{\text{ex}}^2 + \omega_1^2)^2}, \quad (10.65b)$$

$$\hat{\omega}_{\text{Aeff}}^2 = \gamma \omega_1^2 + \delta_A^2, \quad (10.65c)$$

$$\hat{\omega}_{\text{Beff}}^2 = \gamma \omega_1^2 + \delta_B^2, \quad (10.65d)$$

$$\hat{\omega}_{\text{eff}}^2 = \gamma \omega_1^2 + \bar{\Omega}^2, \quad (10.65e)$$

$$\hat{\theta} = \arctan \left( \frac{\sqrt{\gamma} \omega_1}{\bar{\Omega}} \right). \quad (10.65f)$$

The equation is accurate when populations are less skewed than the ‘TP02’ model ( $p_A \gg p_B$ ). Note that this model, as with the ‘TP02’ model, has been superseded by the ‘MP05’ model in the next section. The reference for this equation is:

- Trott, O., Abergel, D., and Palmer, A. (2003). An average-magnetization analysis of R-1 rho relaxation outside of the fast exchange. *Mol. Phys.*, **101**(6), 753–763. ([10.1080/0026897021000054826](#))

### 10.7.6 The MP05 2-site exchange $R_{1\rho}$ model

This is the model for 2-site exchange for off-resonance  $R_{1\rho}$ -type data for all time scales from [Miloushev and Palmer \(2005\)](#). It is selected by setting the model to ‘MP05’. The equation for the exchange process is

$$R_{1\rho} = R_1 \cos^2 \theta + R'_{1\rho} \sin^2 \theta + \frac{\sin^2 \theta p_A p_B \Delta \omega^2 k_{\text{ex}}}{\omega_{\text{Aeff}}^2 \omega_{\text{Beff}}^2 / \omega_{\text{eff}}^2 + k_{\text{ex}}^2 - \sin^2 \theta p_A p_B \Delta \omega^2 \left( 1 + \frac{2k_{\text{ex}}^2 (p_A \omega_{\text{Aeff}}^2 + p_B \omega_{\text{Beff}}^2)}{\omega_{\text{Aeff}}^2 \omega_{\text{Beff}}^2 + \omega_{\text{eff}}^2 k_{\text{ex}}^2} \right)}, \quad (10.66)$$

in which the parameters are defined as in the ‘TP02’ model above. This model supersedes both the ‘TP02’ and ‘TAP03’ models. The reference for this equation is:

- Miloushev, V. Z. and Palmer, 3rd, A. G. (2005). R(1rho) relaxation for two-site chemical exchange: general approximations and some exact solutions. *J. Magn. Reson.*, **177**(2), 221–227. ([10.1016/j.jmr.2005.07.023](#))

## 10.8 The numeric $R_{1\rho}$ models

These are the numeric models designed for  $R_{1\rho}$ -type experiments.

### 10.8.1 The NS 2-site $R_{1\rho}$ model

This is the numerical model for 2-site exchange using 3D magnetisation vectors. It is selected by setting the model to ‘NS R1rho 2-site’. The simple constraint  $p_A > p_B$  is used to halve the optimisation space, as both sides of the limit are mirror image spaces.

For this model, the equations from [Korzhnev et al. \(2005b\)](#) have been used. The  $R_{1\rho}$  value for state A magnetisation is defined as

$$R_{1\rho} = -\frac{1}{T_{\text{relax}}} \cdot \ln (M_0^T \cdot e^{R \cdot T_{\text{relax}}} \cdot M_0), \quad (10.67)$$

where

$$M_0 = \begin{pmatrix} \sin \theta \\ 0 \\ \cos \theta \\ 0 \\ 0 \\ 0 \end{pmatrix}, \quad (10.68)$$

$$\theta = \arctan \left( \frac{\omega_1}{\Omega_A} \right). \quad (10.69)$$

The relaxation evolution matrix is defined as

$$R = \begin{pmatrix} -R'_{1\rho} - k_{AB} & -\delta_A & 0 & k_{BA} & 0 & 0 \\ \delta_A & -R'_{1\rho} - k_{AB} & -\omega_1 & 0 & k_{BA} & 0 \\ 0 & \omega_1 & -R_1 - k_{AB} & 0 & 0 & k_{BA} \\ k_{AB} & 0 & 0 & -R'_{1\rho} - k_{BA} & -\delta_B & 0 \\ 0 & k_{AB} & 0 & \delta_B & -R'_{1\rho} - k_{BA} & -\omega_1 \\ 0 & 0 & k_{AB} & 0 & \omega_1 & -R_1 - k_{BA} \end{pmatrix}, \quad (10.70)$$

where  $\delta_{A,B}$  is defined in Equations [10.63a](#) and [10.63b](#).

### 10.8.2 The NS 3-site $R_{1\rho}$ model

This is the numerical model for 3-site exchange using 3D magnetisation vectors. It is selected by setting the model to ‘NS R1rho 3-site’. The constraints  $p_A > p_B$  and  $p_A > p_C$  is used to decrease the size of the optimisation space, as both sides of the limit are mirror image spaces.

For this model, as for the 2-site model above, the equations from [Korzhnev et al. \(2005b\)](#) have been used. These have been however rearranged to match the notation in [Palmer and Massi \(2006\)](#). The  $R_{1\rho}$  value for state A magnetisation is defined as

$$R_{1\rho} = -\frac{1}{T_{\text{relax}}} \cdot \ln(M_0^T \cdot e^{R \cdot T_{\text{relax}}} \cdot M_0), \quad (10.71)$$

where

$$M_0 = \begin{pmatrix} \sin \theta \\ 0 \\ \cos \theta \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \quad (10.72)$$

$$\theta = \arctan\left(\frac{\omega_1}{\Omega_A}\right). \quad (10.73)$$

This assumes that the starting magnetisation has an X and Z component only for the A state. The relaxation evolution matrix is defined as

$$\begin{aligned} R = & \begin{pmatrix} -R'_{1\rho A} - k_{AB} - k_{AC} & -\delta_A & 0 & \cdots \\ \delta_A & -R'_{1\rho A} - k_{AB} - k_{AC} & -\omega_1 & \cdots \\ 0 & \omega_1 & -R_{1A} - k_{AB} - k_{AC} & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix} \\ & + \begin{pmatrix} \ddots & \vdots & \vdots & \vdots & \ddots \\ \cdots & -R'_{1\rho B} - k_{BA} - k_{BC} & -\delta_B & 0 & \cdots \\ \cdots & \delta_B & -R'_{1\rho B} - k_{BA} - k_{BC} & -\omega_1 & \cdots \\ \cdots & 0 & \omega_1 & -R_{1B} - k_{BA} - k_{BC} & \cdots \\ \ddots & \vdots & \vdots & \vdots & \ddots \end{pmatrix} \\ & + \begin{pmatrix} \ddots & \vdots & \vdots & \vdots & \ddots \\ \cdots & -R'_{1\rho C} - k_{CA} - k_{CB} & -\delta_C & 0 & \cdots \\ \cdots & \delta_C & -R'_{1\rho C} - k_{CA} - k_{CB} & -\omega_1 & \cdots \\ \cdots & 0 & \omega_1 & -R_{1C} - k_{CA} - k_{CB} & \cdots \end{pmatrix} \\ & + \begin{pmatrix} & & k_{BA} & 0 & 0 & \cdots \\ & \ddots & 0 & k_{BA} & 0 & \cdots \\ & & 0 & 0 & k_{BA} & \cdots \\ k_{AB} & 0 & 0 & & & \\ 0 & k_{AB} & 0 & & \ddots & \cdots \\ 0 & 0 & k_{AB} & & & \\ \vdots & \vdots & \vdots & & & \ddots \end{pmatrix} \end{aligned}$$

$$\begin{aligned}
& + \begin{pmatrix} & & & \cdots & k_{CA} & 0 & 0 \\ & \ddots & & \cdots & 0 & k_{CA} & 0 \\ & & & \cdots & 0 & 0 & k_{CA} \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ k_{AC} & 0 & 0 & \cdots & & & \\ 0 & k_{AC} & 0 & \cdots & & \ddots & \\ 0 & 0 & k_{AC} & \cdots & & & \end{pmatrix} \\
& + \begin{pmatrix} \ddots & & \vdots & & \vdots & \vdots & \vdots \\ & & & k_{CB} & 0 & 0 & \\ \cdots & & \ddots & 0 & k_{CB} & 0 & \\ & & & 0 & 0 & k_{CB} & \\ \cdots & k_{BC} & 0 & 0 & & & \\ \cdots & 0 & k_{BC} & 0 & & \ddots & \\ \cdots & 0 & 0 & k_{BC} & & & \end{pmatrix}, \tag{10.74}
\end{aligned}$$

where  $\delta_{A,B,C}$  are defined as in Equations 10.63a and 10.63b. For the model, the assumptions  $R'_{1\rho A} = R'_{1\rho B} = R'_{1\rho C} = R'_{1\rho}$  and  $R_{1A} = R_{1B} = R_{1C} = R_1$  have been made.

### 10.8.3 The NS 3-site linear $R_{1\rho}$ model

This is the numerical model for 3-site linear exchange using 3D magnetisation vectors. The assumption that  $k_{AC} = k_{CA} = 0$  has been made to linearise this model. It is selected by setting the model to ‘NS R1rho 3-site linear’. The constraints  $p_A > p_B$  and  $p_A > p_C$  is used to decrease the size of the optimisation space, as both sides of the limit are mirror image spaces. To simplify the optimisation space for the model as in the ‘NS  $R_{1\rho}$  3-site’ model, the assumptions  $R_{2A}^0 = R_{2B}^0 = R_{2C}^0 = R_2^0$  and  $R_{1A} = R_{1B} = R_{1C} = R_1$  have been made.

The equations are the same as for the ‘NS R1rho 3-site’ model except for the relaxation evolution matrix which simplifies to

$$\begin{aligned}
R = & \begin{pmatrix} -R'_{1\rho A} - k_{AB} & -\delta_A & 0 & \cdots \\ \delta_A & -R'_{1\rho A} - k_{AB} & -\omega_1 & \cdots \\ 0 & \omega_1 & -R_{1A} - k_{AB} & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix} \\
& + \begin{pmatrix} \ddots & \vdots & \vdots & \vdots & \ddots \\ \cdots & -R'_{1\rho B} - k_{BA} - k_{BC} & -\delta_B & 0 & \cdots \\ \cdots & \delta_B & -R'_{1\rho B} - k_{BA} - k_{BC} & -\omega_1 & \cdots \\ \cdots & 0 & \omega_1 & -R_{1B} - k_{BA} - k_{BC} & \cdots \\ \cdots & \vdots & \vdots & \vdots & \ddots \end{pmatrix}
\end{aligned}$$

$$\begin{aligned}
& + \begin{pmatrix} \ddots & \vdots & \vdots & \vdots \\ \cdots & -R'_{1\rho C} - k_{CB} & -\delta_C & 0 \\ \cdots & \delta_C & -R'_{1\rho C} - k_{CB} & -\omega_1 \\ \cdots & 0 & \omega_1 & -R_{1C} - k_{CB} \end{pmatrix} \\
& + \begin{pmatrix} & & k_{BA} & 0 & 0 & \cdots \\ & \ddots & 0 & k_{BA} & 0 & \cdots \\ & & 0 & 0 & k_{BA} & \cdots \\ k_{AB} & 0 & 0 & & & \\ 0 & k_{AB} & 0 & & \ddots & \cdots \\ 0 & 0 & k_{AB} & & & \ddots \\ \vdots & \vdots & \vdots & & \vdots & \ddots \end{pmatrix} \\
& + \begin{pmatrix} \ddots & \vdots & \vdots & \vdots & \vdots \\ \cdots & \ddots & 0 & k_{CB} & 0 \\ \cdots & & 0 & 0 & k_{CB} \\ \cdots & k_{BC} & 0 & 0 & \\ \cdots & 0 & k_{BC} & 0 & \ddots \\ \cdots & 0 & 0 & k_{BC} & \end{pmatrix}, \tag{10.75}
\end{aligned}$$

where  $\delta_{A,B,C}$  are defined as in Equations 10.63a and 10.63b. For the model, the assumptions  $R'_{1\rho A} = R'_{1\rho B} = R'_{1\rho C} = R'_{1\rho}$  and  $R_{1A} = R_{1B} = R_{1C} = R_1$  have been made.

## 10.9 Relaxation dispersion optimisation theory

The implementation of optimisation in relax is discussed in detail in Chapter 12. To understand the concepts in this subsection, it is best to look at that chapter first.

### 10.9.1 The relaxation dispersion auto-analysis

In relax, optimisation can either be performed manually or one of the auto-analyses can be employed. Note that if you are using the relax GUI, you will be using the dispersion auto-analysis. The auto-analysis is a fully self-contained protocol designed to make the analysis as simple as possible. All details can be seen in the `auto_analyses/relax_disp.py` file which, in reality, is simply a large relax script.

The relaxation dispersion auto-analysis implements many of the concepts described in detail in the next sections. It can be summarised as:

**Peak intensity error analysis:** An error analysis is performed to determine the peak intensity errors, if not already calculated (see Section 14.2.200 on page 439).

**‘R2eff’ model optimisation:** Firstly the ‘R2eff’ model is either optimised (using the `minimise` user function) or simply calculated (using the `calc` user function) to find

the  $R_{2\text{eff}}$  or  $R_{1\rho}$  values used as the base data for all other dispersion models (see Section 10.2.1 on page 147).

**Dispersion curve insignificance:** Spins with insignificant dispersion profiles will be deselected with the `relax_disp.insignificance` user function, as described below, excluding the ‘No Rex’ model.

**Model optimisation:** Sequential optimisation of each of the specified dispersion models. This consists of a grid search followed by Nelder-Mead simplex optimisation constrained using the log-barrier constraint algorithm. Each model will be stored in a different data pipe. See Section 14.2.52 on page 324 for the grid search and Section 14.2.64 on page 332 for minimisation.

**Grid search avoidance:** A number of tricks are used to speed up optimisation by skipping or decreasing the size of the initial grid search:

**Pre-run directory:** If a pre-run directory is supplied – a separate directory containing the dispersion auto-analysis results from a previous run – the optimised parameters from these previous results will be used as the starting point for optimisation rather than performing a grid search. This is used in a clustered analysis whereby the pre-run directory contains results from a non-clustered analysis. This is essential for when large spin clusters are specified, as a grid search becomes prohibitively expensive with clusters of three or more spins. At some point a RelaxError will occur because the grid search is impossibly large. For the cluster specific parameters, i.e. the populations of the states and the exchange parameters, an average value will be used as the starting point. For all other parameters, the  $R_2^0$  values for each spin and magnetic field, as well as the parameters related to the chemical shift difference  $\Delta\omega$ , the optimised values of the previous run will be directly copied.

**Model nesting:** If two models are nested, then the parameters of the simpler will be used as the starting point for optimisation of the more complex. The currently supported nested model pairs are ‘LM63’ and ‘LM63 3-site’, ‘CR72’ and ‘CR72 full’, ‘CR72’ and ‘MMQ CR72’, ‘NS CPMG 2-site 3D’ and ‘NS CPMG 2-site 3D full’, and ‘NS CPMG 2-site star’ and ‘NS CPMG 2-site star full’. In these cases, the  $R_{2A}^0$  and  $R_{2B}^0$  parameter values are set to the simpler model  $R_2^0$  value and the grid search is bypassed.

**Model equivalence:** When two models are equivalent, the optimised parameters of one model can be used as the starting point of the other rather than performing a grid search. This is used in the auto-analysis for avoiding the grid search in the numeric models. The optimised ‘CR72’ model is used for the ‘NS CPMG 2-site expanded’, ‘NS CPMG 2-site 3D’, and ‘NS CPMG 2-site star’ models. The optimised ‘MMQ CR72’ model is used for the ‘NS MMQ 2-site’ model. And the ‘MP05’ model is used for the ‘NS R1rho 2-site’ model.

**Interruption:** The optimisation procedure of the auto-analysis can read saved results files if a previous calculation was interrupted.

**Model elimination:** As it is quite common that some of the dispersion models fail to optimise to reasonable values, or will even optimise to non-physically possible values where the global minimum is located, model elimination is performed to remove these models. The relax implementation is described in d’Auvergne and Gooley (2006).



This needs to be performed prior to model selection as a failed model will often provide a statistically better fit than a non-failed model.

**Per-model error analysis:** If desired, Monte Carlo simulations for error propagation can be performed for each model. This does however require far greater computation time.

**Model selection:** If more than one model is analysed, AIC model selection will be performed to judge statistical significance of the models (Akaike, 1973). This is used to determine if statistically significant  $R_{\text{ex}}$  contributions can be extracted from the data, as well as determine if one model is better than the other. Different statistical techniques such as AICc and BIC can be used when using the script UI (Hurvich and Tsai, 1989; Schwarz, 1978). The AIC, AICc and BIC equations for NMR relaxation data were derived in d’Auvergne and Gooley (2003). In most cases, the list models to choose from should be severely limited. The results will be stored in a new ‘final’ data pipe and output files placed in the `final` directory.

**Error analysis:** Monte Carlo simulations for error propagation is performed on the final data pipe (see Section 14.2.89 on page 370 as well as the descriptions for all of the other `monte_carlo` user functions). Model elimination is performed again to remove the Monte Carlo simulations which have failed.

**Output file creation:** For each of the models and the final model selection results, the `relax_disp.plot_disp_curves` (Section 14.2.162 on page 415), `relax_disp.plot_exp_curves` (Section 14.2.163 on page 416), `relax_disp.write_disp_curves` (Section 14.2.171 on page 421), `grace.write` (Section 14.2.51 on page 320) and `value.write` (Section 14.2.241 on page 479) user functions will be called to generate all the output files you would need. These generate both Grace 2D plots of the data as well as plain text files. Additional output files can be created after the analysis by using the user functions manually.

All these steps will be shown in full detail in the relax logs. You should check very carefully for any relax warnings as these can be an indication that something has not been set up correctly.

If you are a power user, you are free to use all of the relax user functions, the relax library, and the relax data store to implement your own protocol. If you wish, the protocol can be converted into a new auto-analysis and distributed as part of relax. The relax test suite will ensure the protocol remains functional for the lifetime of relax.

### 10.9.2 Dispersion curve insignificance

To avoid severe model failure due to the fitting of statistically insignificant dispersion curves, the `relax_disp.insignificance` user function can be used. This is activated by default in the auto-analysis. The user function takes a single insignificance value and if the difference between the smallest and largest  $R_{2\text{eff}}$  or  $R_{1\rho}$  value for an individual spin for all dispersion curves is less than this, then that spin will be deselected. See Section 14.2.159 on page 414 for more details.

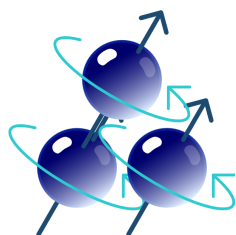
### 10.9.3 The relaxation dispersion space

In a dispersion analysis the target function  $f(\theta)$  is the chi-squared equation

$$\chi^2(\theta) = \sum_{i=1}^n \frac{(R_{2\text{eff}} - R_{2\text{eff}}(\theta))^2}{\sigma_i^2}, \quad (10.76)$$

where  $i$  is the summation index,  $R_{2\text{eff}}$  is the experimental relaxation data which belongs to the data set  $R$  and includes the  $R_{2\text{eff}}$  and  $R_{1\rho}$  values for all experiments at all magnetic field strengths,  $R_{2\text{eff}}(\theta)$  is the back calculated relaxation data belonging to the set  $R(\theta)$ , and  $\sigma_i$  is the experimental  $R_{2\text{eff}}/R_{1\rho}$  error. For standard optimisation, the summation index ranges over the relaxation data of an individual spin. However this can be changed with clustering whereby the relaxation data from a group of spin systems are optimised using a shared set of parameters.

### 10.9.4 The clustered relaxation dispersion analysis



Often in a relaxation dispersion analysis you will wish to fit a number of spin systems together using global parameters such as  $k_{\text{ex}}$ ,  $p_A$ , etc. This can be achieved through the concept of clustering. A cluster is defined by an ID string and can contain any number of spins. Multiple clusters in one analysis can be defined. Any spins not included in a cluster will be treated as a free spin whereby all parameters of the dispersion model are local to that spin. Spin clusters can be defined using the `relax_disp.cluster` user function (see Section 14.2.154 on page 411) or via the spin cluster GUI element.

### 10.9.5 Dispersion parameter grid search

One of the most statistically unbiased methods for determining an initial parameter estimate prior to optimisation is to perform a grid search. This is performed via the `grid_search` user function (see Section 14.2.52 on page 324).

For some dispersion models the grid search can be too computationally expensive. In this case, some tricks can be used to bypass the parts of the grid search or the whole grid search:

**Model nesting:** Using the optimised parameters of a simpler nested model as the starting point for optimisation.

**Model equivalence:** Using the optimised solution of an equivalent analytic model as the starting point for a numeric model.

These tricks are implemented in the relaxation dispersion auto-analysis protocol as described above. If you do not use the auto-analysis or the GUI, then you are free to implement your own solutions.

The grid search lower and upper bounds default to:

$$1 \leq R_2^0 \leq 40, \quad (10.77a)$$

$$1 \leq R_{2A}^0 \leq 40, \quad (10.77b)$$

$$1 \leq R_{2B}^0 \leq 40, \quad (10.77c)$$

$$0 \leq \Phi_{\text{ex}} \leq 10, \quad (10.77d)$$

$$0 \leq \Phi_{\text{ex},B} \leq 10, \quad (10.77e)$$

$$0 \leq \Phi_{\text{ex},C} \leq 10, \quad (10.77f)$$

$$0 \leq p_A \Delta\omega^2 \leq 10, \quad (10.77g)$$

$$0 \leq \Delta\omega \leq 10, \quad (10.77h)$$

$$0 \leq \Delta\omega_{AB} \leq 10, \quad (10.77i)$$

$$0 \leq \Delta\omega_{BC} \leq 10, \quad (10.77j)$$

$$0 \leq \Delta\omega^H \leq 3, \quad (10.77k)$$

$$0 \leq \Delta\omega_{AB}^H \leq 3, \quad (10.77l)$$

$$0 \leq \Delta\omega_{BC}^H \leq 3, \quad (10.77m)$$

$$0.5 \leq p_A \leq 1, \quad (10.77n)$$

$$0.0 \leq p_B \leq 0.5, \quad (10.77o)$$

$$0 \leq k_{\text{ex}} \leq 1e^6, \quad (10.77p)$$

$$0 \leq k_{\text{ex}}^{AB} \leq 1e^6, \quad (10.77q)$$

$$0 \leq k_{\text{ex}}^{BC} \leq 1e^6, \quad (10.77r)$$

$$0 \leq k_A \leq 1e^6, \quad (10.77s)$$

$$0 \leq k_B \leq 1e^6, \quad (10.77t)$$

$$0 \leq k_{AB} \leq 1e^6, \quad (10.77u)$$

$$0 \leq \tau_{\text{ex}} \leq 1e^{-6}. \quad (10.77v)$$

For the MMQ models, the grid bounds are slightly different with

$$-10 \leq \Delta\omega \leq 10, \quad (10.78a)$$

$$-10 \leq \Delta\omega_{AB} \leq 10, \quad (10.78b)$$

$$-10 \leq \Delta\omega_{BC} \leq 10, \quad (10.78c)$$

$$-3 \leq \Delta\omega^H \leq 3, \quad (10.78d)$$

$$-3 \leq \Delta\omega_{AB}^H \leq 3, \quad (10.78e)$$

$$-3 \leq \Delta\omega_{BC}^H \leq 3. \quad (10.78f)$$

These values can be changed when not using the auto-analysis. Linear constraints can decrease the number of grid points searched through.



for the population parameters as

$$\begin{pmatrix} -1 & 0 \\ 1 & 0 \\ 1 & 0 \\ -1 & -1 \\ 1 & 2 \end{pmatrix} \cdot \begin{pmatrix} p_A \\ p_B \end{pmatrix} \geq \begin{pmatrix} -1 \\ 0.5 \\ 0.85 \\ -1 \\ 1 \end{pmatrix}, \quad (10.81)$$

and for the exchange rate and time parameters as

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} k_{\text{ex}} \\ k_{\text{ex}}^{\text{AB}} \\ k_{\text{ex}}^{\text{BC}} \\ k_{\text{ex}} \\ k_B \\ k_C \\ k_{\text{AB}} \\ \tau_{\text{ex}} \end{pmatrix} \geq \begin{pmatrix} 0 \\ -2e^6 \\ 0 \\ -2e^6 \\ 0 \\ -2e^6 \\ 0 \\ -2e^6 \\ 0 \\ -2e^6 \\ 0 \\ -2e^6 \\ 0 \end{pmatrix}. \quad (10.82)$$

Through the isolation of each individual element, the constraints can be seen to be equivalent to

$$0 \leq R_2^0 \leq 200, \quad (10.83a)$$

$$0 \leq R_{2A}^0 \leq 200, \quad (10.83b)$$

$$0 \leq R_{2B}^0 \leq 200, \quad (10.83c)$$

$$\Phi_{\text{ex}} \geq 0, \quad (10.83d)$$

$$\Phi_{\text{ex},B} \geq 0, \quad (10.83e)$$

$$\Phi_{\text{ex},C} \geq 0, \quad (10.83f)$$

$$\Delta\omega \geq 0, \quad (10.83g)$$

$$\Delta\omega_{\text{AB}} \geq 0, \quad (10.83h)$$

$$\Delta\omega_{\text{BC}} \geq 0, \quad (10.83i)$$

$$\Delta\omega^{\text{H}} \geq 0, \quad (10.83j)$$

$$\Delta\omega_{\text{AB}}^{\text{H}} \geq 0, \quad (10.83k)$$

$$\Delta\omega_{\text{BC}}^{\text{H}} \geq 0, \quad (10.83l)$$

$$p_A \Delta\omega^2 \geq 0, \quad (10.83m)$$

$$0 \leq p_A \leq 1, \quad (10.83n)$$

$$0 \leq p_B \leq p_A, \quad (10.83o)$$

$$0 \leq p_C \leq p_A, \quad (10.83p)$$

$$p_A \geq 0.85 \quad (\text{the skewed condition, } p_A \gg p_B), \quad (10.83q)$$

$$0 \leq k_{\text{ex}} \leq 2e^6, \quad (10.83r)$$

$$0 \leq k_{\text{ex}}^{\text{AB}} \leq 2e^6, \quad (10.83\text{s})$$

$$0 \leq k_{\text{ex}}^{\text{BC}} \leq 2e^6, \quad (10.83\text{t})$$

$$0 \leq k_{\text{A}} \leq 2e^6, \quad (10.83\text{u})$$

$$0 \leq k_{\text{B}} \leq 2e^6, \quad (10.83\text{v})$$

$$0 \leq k_{\text{AB}} \leq 2e^6, \quad (10.83\text{w})$$

$$\tau_{\text{ex}} \geq 0. \quad (10.83\text{x})$$

Note that the  $\Delta\omega$  and  $\Delta\omega^{\text{H}}$  constraints are not used for any of the MMQ-type models as sign differentiation is possible. These constraints are also turned off for the ‘NS  $R_{1\rho}$  3-site linear’ and ‘NS  $R_{1\rho}$  3-site’ models. And that the  $p_{\text{A}} \geq 0.85$  constraint is used instead of the  $p_{\text{A}} \geq 0.5$  constraint for all models which require  $p_{\text{A}} \gg p_{\text{B}}$ . When not using the auto-analysis, constraints can be modified or turned off.

### 10.9.8 Relaxation dispersion diagonal scaling

The concept of diagonal scaling is explained in Section 12.6 on page 224.

For the dispersion analysis the scaling factor of 10 is used for the relaxation rates,  $1e^5$  for the exchange rates,  $1e^{-4}$  for exchange times, and 1 for all other parameters. The scaling matrix for the parameters  $\{R_2^0, R_{2\text{A}}^0, R_{2\text{B}}^0, \Phi_{\text{ex}}, \Phi_{\text{ex,B}}, \Phi_{\text{ex,C}}, p_{\text{A}}\Delta\omega^2, \Delta\omega, \Delta\omega^{\text{H}}, p_{\text{A}}, p_{\text{B}}, k_{\text{ex}}, k_{\text{B}}, k_{\text{C}}, k_{\text{AB}}, \tau_{\text{ex}}\}$  is

$$\begin{pmatrix} 10 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 10 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 10 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^5 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^5 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1e^{-4} \end{pmatrix}. \quad (10.84)$$

### 10.9.9 Relaxation dispersion model elimination

Relaxation dispersion models will often fail. This may be due to data quality and quantity issues, inherent instability in certain models, or the use of analytic models outside of the range of their defined viability. Model elimination is therefore required to remove these failed models prior to model selection, as failed models will often fit the experimental data statistically better than non-failed models. The user function `eliminate` (see

Section 14.2.41 on page 313) is used to remove the failed models. Model elimination was implement in relax as described in:

- d’Auvergne, E. J. and Gooley, P. R. (2006). Model-free model elimination: A new step in the model-free dynamic analysis of NMR relaxation data. *J. Biomol. NMR*, **35**(2), 117–135. ([10.1007/s10858-006-9007-z](https://doi.org/10.1007/s10858-006-9007-z))

The following hard coded rules are used to eliminate models:

$$p_A \leq 0.501, \quad (10.85a)$$

$$p_A \geq 0.999, \quad (10.85b)$$

$$\tau_{\text{ex}} \geq 1.0. \quad (10.85c)$$

If a parameter falls outside of these limits, the entire spin cluster will be deselected. When not using the auto-analysis, custom model elimination rules can be defined and used with the `eliminate` user function.

### 10.9.10 Monte Carlo simulation elimination

Just as models can fail, often Monte Carlo simulations will also experience optimisation failures (see Figure 4 of d’Auvergne and Gooley (2006) for such a failure in the model-free optimisation space). The minimum can be warped so much by the data randomisation that a new minimum appears at an unreasonable position in the optimisation space. Even when the original model optimisation is successful, this can affect a small portion of the simulations. These must be removed prior to calculating the parameter errors otherwise the errors will be significantly over estimated. The simulation model failures are outliers which skew the error estimate, introducing a bias. This can result in parameter error estimates which are too large. The solution is the use of the `eliminate` user function when Monte Carlo simulations are turned on – this will automatically deselect simulations rather than spins using the rules from the previous section. Note that relax is the only software which provides this feature.

### 10.9.11 Relaxation dispersion on a computer cluster using OpenMPI

If the optimisation is too slow on a single computer, the dispersion analysis has been parallelised on the level of both the spin cluster and the Monte Carlo simulation. The scaling efficiency is very close to perfect so if you have access to a computer cluster and the OpenMPI protocol, then the calculations can be run much faster. The implementation uses Gary Thompson’s multi-processor package. See Section 1.3 on page 17 for details on how to use this.

## 10.10 To do – dispersion features yet to be implemented

The capabilities of the relaxation dispersion analysis in relax is expansive but it cannot be called complete. There are a number of features and models yet to be implemented. Missing features include:

- The handling of off-resonance effects in the models of the numeric solution for CPMG-type data. This is specifically the ‘NS CPMG 2-site 3D’ and ‘NS CPMG 2-site star’ models and their ‘\* full’ equivalents. The necessary infrastructure is in place, but not activated yet (mainly due to a lack of synthetic data to test against).
- Multi-state data – the handling of data from two sets of peaks from the same spin system is not properly supported. It is currently handled by assuming each state is a separate spin system but this means that  $\Delta\omega$ ,  $\Delta\omega^H$  and related parameters are not shared as they should be.
- The van’t Hoff analysis of multi-temperature dispersion data (see [https://en.wikipedia.org/wiki/Van\\_%27t\\_Hoff\\_equation](https://en.wikipedia.org/wiki/Van_%27t_Hoff_equation)).
- ZZ exchange.
- HD exchange.
- The [Korzhnev et al. \(2005b\)](#) correction for constant-time  $R_{1\rho}$  experiments for the analytic models ( $R_{1\rho} = -\lambda_1 - 1/T_{\text{relax}} \log a_1$ , where  $a_1 = 1 - p_B \cos^2(\theta_A - \theta_B)$ , and  $\theta_A = \arctan(\omega_1/\omega_A)$  and  $\theta_B = \arctan(\omega_1/\omega_B)$ ).

If you would like one of these features, please contact the “relax-devel at gna.org” mailing list. The most useful would be if you have synthetic data whereby you know what the true solution should be. This can then be incorporated into a relax system test and the feature implemented to allow the test to pass. Note that such data should never be emailed to a public mailing list! Synthetic data, or experimental data, can be obtained from the literature.

Some of the missing models include:

- ‘**TP04**’: The  $R_{1\rho}$ -type data [Trott and Palmer \(2004\)](#) N-site analytic equation for all time scales with parameters  $\{R'_{1\rho}, \dots, p_1, \dots, p_N, \bar{\omega}, k_{12}, \dots, k_{1N}\}$ .
- ‘\*  $R_{1\rho}$ ’: All of the 3-site and N-site models as summarised in Table 1 of [Palmer and Massi \(2006\)](#).

Information for how these can be added is given in the next section.

## 10.11 Tutorial for adding relaxation dispersion models

As the field of NMR relaxation dispersion has a very long history, it is not possible to include all analytic and numeric relaxation dispersion models for both CPMG-type or  $R_{1\rho}$ -type experiments in relax. However it is not too difficult to add new models for your own needs if you have some Python, Matlab, Mathematica, or similar scripting skills. The steps required are detailed on the [relax wiki](http://wiki.nmr-relax.com/Tutorial_for_adding_relaxation_dispersion_models_to_relax) page [http://wiki.nmr-relax.com/Tutorial\\_for\\_adding\\_relaxation\\_dispersion\\_models\\_to\\_relax](http://wiki.nmr-relax.com/Tutorial_for_adding_relaxation_dispersion_models_to_relax).



## 10.12 Comparison of dispersion analysis software

Diverse software exists for analysing relaxation dispersion data. The following is a list of the officially released software which you can use instead of relax:

**CPMGFit** Art Palmer’s original dispersion analysis software at <http://www.palmer.hs.columbia.edu/software/cpmgfit.html>.

**cpmg\_fit** Dmitry Korzhnev’s dispersion software available upon request.

**CATIA** Flemming Hansen’s dispersion software at <http://www.biochem.ucl.ac.uk/hansen/catia/>. The reference is Hansen et al. (2008).

**NESSY** Michael Bieri’s dispersion software at <http://home.gna.org/nessy/>. The reference is Bieri and Gooley (2011).

**GUARDD** Ian Kleckner’s dispersion software at <http://code.google.com/p/guardd/>. The reference is Kleckner and Foster (2012).

**ShereKhan** See the web server at <http://sherekhan.bionmr.org/>. The reference is Mazur et al. (2013).

**GLOVE** Peter Wright’s dispersion software at <http://www.scripps.edu/wright/>. The reference is Sugase et al. (2013).

**chemex** Guillaume Bouvignies’ dispersion software which can be found at <http://code.google.com/p/chemex/>.

There is currently support in relax for generating the input files for CPMGFit, CATIA, NESSY, and ShereKhan and for running CPMGFit and CATIA from within relax.

The features of the different software are compared in Table 10.3 on page 178. Note that this table is likely to be incomplete so please see the websites of the respective software for an up to date list of features. The aim of this table is to provide a fair comparison between all of the available dispersion software. Therefore if you do find deficiencies or errors in this table please report these either to the relax users mailing list at “relax-users at gna.org”, submit a bug report (see section 3.3 on page 30), or send a private message to one of the relax developers (<http://gna.org/project/memberlist.php?group=relax>) so that the details can be corrected.

Table 10.3: Comparison of the features for the different dispersion software.

|   | CPMGFit | cpmg_fit | CATIA | NESSY | GUARDD | ShereKhan | GLOVE | chemex | relax |
|---|---------|----------|-------|-------|--------|-----------|-------|--------|-------|
| <b>Dispersion models</b>                        |         |          |       |       |        |           |       |        |       |
| <b>Base models</b>                              |         |          |       |       |        |           |       |        |       |
| $R_{2\text{eff}}/R'_{1\rho}$                    | -       | -        | -     | ✓     | ✓      | ✓         | ✓     | -      | ✓     |
| No Rex  | -       | ✓        | -     | ✓     | ✓      | -         | ✓     | -      | ✓     |
| <b>Single quantum (SQ) CPMG-type</b>            |         |          |       |       |        |           |       |        |       |
| LM63  | ✓       | -        | -     | ✓     | -      | ✓         | ✓     | -      | ✓     |
| LM63 3-site                                     | ✓       | -        | -     | ✓     | -      | -         | -     | -      | ✓     |
| CR72  | ✓       | -        | -     | ✓     | -      | ✓         | ✓     | -      | ✓     |
| IT99  | ✓       | -        | -     | -     | -      | -         | ✓     | -      | ✓     |
| TSMFK01   | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| NS 2-site                                       | -       | ✓        | ✓     | -     | -      | ✓         | ?     | -      | ✓     |
| <b>MMQ (SQ, ZQ, DQ, &amp; MQ) CPMG-type</b>     |         |          |       |       |        |           |       |        |       |
| MMQ CR72  | -       | ✓        | -     | -     | ✓      | -         | ?     | -      | ✓     |
| NS MMQ 2-site                                   | -       | ✓        | -     | -     | -      | -         | ?     | -      | ✓     |
| NS MMQ 3-site linear                            | -       | ✓        | -     | -     | -      | -         | ?     | -      | ✓     |
| NS MMQ 3-site                                   | -       | ✓        | -     | -     | -      | -         | ?     | -      | ✓     |
| <b><math>R_{1\rho}</math>-type</b>              |         |          |       |       |        |           |       |        |       |
| M61   | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| DPL94   | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| TP02  | -       | ✓        | -     | -     | -      | -         | -     | -      | ✓     |
| TAP03   | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| TP04  | -       | -        | -     | -     | -      | -         | -     | -      | -     |
| MP05  | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| NS $R_{1\rho}$ 2-site                           | -       | ✓        | -     | -     | -      | -         | ?     | -      | ✓     |
| NS $R_{1\rho}$ 3-site linear                    | -       | ✓        | -     | -     | -      | -         | -     | -      | ✓     |
| NS $R_{1\rho}$ 3-site                           | -       | ✓        | -     | -     | -      | -         | -     | -      | ✓     |
| <b>General features</b>                         |         |          |       |       |        |           |       |        |       |
| Parallelisation via MPI for running on clusters | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| Off-resonance effects (CPMG-type data)          | -       | -        | ✓     | -     | -      | -         | -     | -      | -     |
| Off-resonance effects ( $R_{1\rho}$ -type data) | -       | ✓        | -     | -     | -      | -         | -     | -      | ✓     |
| Support for CEST-type data                      | -       | -        | -     | -     | -      | -         | -     | ✓      | -     |
| Van't Hoff analysis                             | -       | -        | -     | ✓     | ✓      | -         | -     | -      | -     |
| Arrhenius analysis                              | -       | ✓        | -     | -     | ✓      | -         | -     | -      | -     |
| ZZ exchange                                     | -       | -        | -     | -     | -      | -         | -     | -      | -     |
| HD exchange                                     | -       | -        | -     | -     | -      | -         | -     | -      | -     |
| Dispersion data back calculation (BC)           | -       | ✓        | -     | ✓     | ✓      | -         | -     | -      | ✓     |

Table 10.3: Comparison of the features for the different dispersion software.

|  | CPMGfit | cpmg-fit | CATIA | NESSY | GUARDD | ShereKhan | GLOVE | chemex | relax |
|--|---------|----------|-------|-------|--------|-----------|-------|--------|-------|
| <b>User interface</b>                      |         |          |       |       |        |           |       |        |       |
| Graphical user interface (GUI)             | -       | -        | -     | ✓     | ✓      | -         | -     | -      | ✓     |
| Web user interface (Web UI)                | -       | -        | -     | -     | -      | ✓         | -     | -      | -     |
| Scripting user interface (Script UI)       | -       | ✓        | ✓     | -     | -      | ✓         | ✓     | -      | ✓     |
| Shell interface                            | ✓       | -        | -     | -     | -      | -         | -     | ✓      | -     |
| Temperature and field-dependent simulator  |         |          |       |       |        |           |       |        |       |
| UI for experimental planning (data BC)     | -       | -        | -     | -     | ✓      | -         | -     | -      | -     |
| <b>Optimisation</b>                        |         |          |       |       |        |           |       |        |       |
| Grid search algorithm                      | ✓       | -        | -     | ✓     | ✓      | ✓         | ✓     | -      | ✓     |
| Grid search (via scripting)                | -       | -        | ✓     | -     | -      | -         | -     | -      | -     |
| Nelder-Mead simplex algorithm              | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| Levenberg-Maquardt algorithm               | ✓       | ✓        | ✓     | ✓     | -      | ✓         | ✓     | ✓      | -     |
| Numeric gradient approximation             | ✓       | ✓        | ✓     | ✓     | -      | ✓         | ✓     | ✓      | -     |
| Logarithmic-barrier constraint algorithm   | -       | -        | -     | -     | -      | -         | ✓     | -      | ✓     |
| MATLAB interior-point black magic          | -       | -        | -     | -     | ✓      | -         | -     | -      | -     |
| Visualisation of the chi-squared space     | -       | -        | -     | -     | ✓      | -         | -     | -      | ✓     |
| <b>Error propagation</b>                   |         |          |       |       |        |           |       |        |       |
| Covariance matrix (lowest quality)         | ✓       | ✓        | ✓     | -     | ✓      | ✓         | ✓     | -      | -     |
| Jackknife simulations (for missing errors) | ✓       | -        | -     | -     | -      | -         | ✓     | -      | -     |
| Bootstrapping simulations (false errors)   | -       | -        | -     | -     | -      | -         | -     | -      | -     |
| Monte Carlo simulations (gold standard)    | ✓       | -        | -     | ✓     | ✓      | -         | ✓     | ✓      | ✓     |
| <b>Inbuilt statistical comparisons</b>     |         |          |       |       |        |           |       |        |       |
| Akaike's Information Criterion (AIC)       | -       | -        | -     | ✓     | -      | -         | -     | -      | ✓     |
| Small sample size AIC (AICc)               | -       | -        | -     | ✓     | -      | -         | -     | -      | ✓     |
| Bayesian Information Criterion (BIC)       | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| F-testing (ANOVA statistics)               | -       | -        | -     | ✓     | ✓      | -         | -     | -      | -     |
| <b>Data and model testing</b>              |         |          |       |       |        |           |       |        |       |
| Insignificant dispersion curve tests       | -       | -        | -     | ✓     | -      | -         | -     | -      | ✓     |
| Model elimination tests                    | -       | -        | -     | -     | -      | -         | -     | -      | ✓     |
| <b>Programming languages</b>               |         |          |       |       |        |           |       |        |       |
| Python                                     | -       | -        | -     | ✓     | -      | ✓         | -     | ✓      | ✓     |
| C  | -       | ✓        | ✓     | -     | -      | -         | ✓     | -      | ✓     |
| Perl                                       | -       | -        | -     | -     | -      | -         | ✓     | -      | -     |
| MATLAB                                     | -       | -        | -     | -     | ✓      | -         | -     | -      | -     |
| FORTRAN                                    | ✓       | -        | -     | -     | -      | -         | -     | -      | -     |
| Ruby on Rails                              | -       | -        | -     | -     | -      | ✓         | -     | -      | -     |
| <b>Open source licencing</b>               |         |          |       |       |        |           |       |        |       |
| GNU General Public Licence (version 2+)    | ✓       | -        | -     | -     | -      | -         | -     | -      | -     |
| GNU General Public Licence (version 3+)    | -       | -        | -     | ✓     | ✓      | -         | -     | ✓      | ✓     |
| Open source infrastructure                 | -       | -        | -     | ✓     | ✓      | -         | -     | ✓      | ✓     |
| Proprietary                                | -       | ✓        | ✓     | -     | -      | ✓         | ✓     | -      | -     |

## 10.13 Analysing dispersion in the prompt/script UI mode

Before reading this section, please read Chapter 4 covering the relax data model first. It will explain many of the concepts used within the following example script. For detailed information on how to run a relax script, please see section 1.2.8 on page 11. The dispersion analysis is parallelised on the level of the spin cluster and Monte Carlo simulations so, if you have access to an MPI cluster or multi-core system with OpenMPI installed, please see section 1.3 on page 17 for how to run the calculations much quicker.

### 10.13.1 Dispersion script mode – the sample script

The following is a verbatim copy of the contents of the `sample_scripts/relax_disp/cpmg_analysis.py` file. You will need to first copy this script to a dedicated analysis directory containing peak lists, a sequence or PDB file and a file listing unresolved spin systems, and then modify its contents to suit your specific analysis. The script contents are:

```

1  """Script for performing a full relaxation dispersion analysis using CPMG-type data."""
2
3
4  # Python module imports.
5  from os import sep
6
7  # relax module imports.
8  from auto_analyses.relax_disp import Relax_disp
9
10
11 # Analysis variables.
12 #####
13
14 # The dispersion models.
15 MODELS = ['R2eff', 'No Rex', 'CR72', 'N2 CPMG 2-site expanded']
16
17 # The grid search size (the number of increments per dimension).
18 GRID_INC = 11
19
20 # The number of Monte Carlo simulations to be used for error analysis at the end of the
    analysis.
21 MC_NUM = 500
22
23 # The results directory.
24 RESULTS_DIR = '.'
25
26 # The model selection technique to use.
27 MODSEL = 'AIC'
28
29 # The flag for only using numeric models in the final model selection.
30 NUMERIC_ONLY = False
31
32 # The R2eff value in rad/s by which to judge insignificance. If the maximum difference
    between two points on all dispersion curves for a spin is less than this value, that
    spin will be deselected.

```

```

33 INSIGNIFICANCE = 1.0
34
35
36
37 # Set up the data pipe.
38 #####
39
40 # Create the data pipe.
41 pipe_name = 'base pipe'
42 pipe_bundle = 'relax_disp'
43 pipe.create(pipe_name=pipe_name, bundle=pipe_bundle, pipe_type='relax_disp')
44
45 # Load the sequence.
46 sequence.read('fake_sequence.in', res_num_col=1, res_name_col=2)
47
48 # Name the spins so they can be matched to the assignments, and the isotope for field
   strength scaling.
49 spin.name(name='N')
50 spin.isotope(isotope='15N')
51
52 # The spectral data - spectrum ID, peak list file name, CPMG frequency (Hz), spectrometer
   frequency in Hertz.
53 data = [
54     ['500_reference.in',      '500_MHz'+sep+'reference.in_sparky',      None, 500e6],
55     ['500_66.667.in',        '500_MHz'+sep+'66.667.in_sparky',        66.6666, 500e6],
56     ['500_133.33.in',        '500_MHz'+sep+'133.33.in_sparky',        133.3333, 500e6],
57     ['500_133.33.in.bis',    '500_MHz'+sep+'133.33.in.bis_sparky',    133.3333, 500e6],
58     ['500_200.in',           '500_MHz'+sep+'200.in_sparky',           200.0000, 500e6],
59     ['500_266.67.in',        '500_MHz'+sep+'266.67.in_sparky',        266.6666, 500e6],
60     ['500_333.33.in',        '500_MHz'+sep+'333.33.in_sparky',        333.3333, 500e6],
61     ['500_400.in',           '500_MHz'+sep+'400.in_sparky',           400.0000, 500e6],
62     ['500_466.67.in',        '500_MHz'+sep+'466.67.in_sparky',        466.6666, 500e6],
63     ['500_533.33.in',        '500_MHz'+sep+'533.33.in_sparky',        533.3333, 500e6],
64     ['500_533.33.in.bis',    '500_MHz'+sep+'533.33.in.bis_sparky',    533.3333, 500e6],
65     ['500_600.in',           '500_MHz'+sep+'600.in_sparky',           600.0000, 500e6],
66     ['500_666.67.in',        '500_MHz'+sep+'666.67.in_sparky',        666.6666, 500e6],
67     ['500_733.33.in',        '500_MHz'+sep+'733.33.in_sparky',        733.3333, 500e6],
68     ['500_800.in',           '500_MHz'+sep+'800.in_sparky',           800.0000, 500e6],
69     ['500_866.67.in',        '500_MHz'+sep+'866.67.in_sparky',        866.6666, 500e6],
70     ['500_933.33.in',        '500_MHz'+sep+'933.33.in_sparky',        933.3333, 500e6],
71     ['500_933.33.in.bis',    '500_MHz'+sep+'933.33.in.bis_sparky',    933.3333, 500e6],
72     ['500_1000.in',          '500_MHz'+sep+'1000.in_sparky',          1000.0000, 500e6],
73     ['800_reference.in',      '800_MHz'+sep+'reference.in_sparky',      None, 800e6],
74     ['800_66.667.in',        '800_MHz'+sep+'66.667.in_sparky',        66.6666, 800e6],
75     ['800_133.33.in',        '800_MHz'+sep+'133.33.in_sparky',        133.3333, 800e6],
76     ['800_133.33.in.bis',    '800_MHz'+sep+'133.33.in.bis_sparky',    133.3333, 800e6],
77     ['800_200.in',           '800_MHz'+sep+'200.in_sparky',           200.0000, 800e6],
78     ['800_266.67.in',        '800_MHz'+sep+'266.67.in_sparky',        266.6666, 800e6],
79     ['800_333.33.in',        '800_MHz'+sep+'333.33.in_sparky',        333.3333, 800e6],
80     ['800_400.in',           '800_MHz'+sep+'400.in_sparky',           400.0000, 800e6],
81     ['800_466.67.in',        '800_MHz'+sep+'466.67.in_sparky',        466.6666, 800e6],
82     ['800_533.33.in',        '800_MHz'+sep+'533.33.in_sparky',        533.3333, 800e6],
83     ['800_533.33.in.bis',    '800_MHz'+sep+'533.33.in.bis_sparky',    533.3333, 800e6],
84     ['800_600.in',           '800_MHz'+sep+'600.in_sparky',           600.0000, 800e6],
85     ['800_666.67.in',        '800_MHz'+sep+'666.67.in_sparky',        666.6666, 800e6],
86     ['800_733.33.in',        '800_MHz'+sep+'733.33.in_sparky',        733.3333, 800e6],
87     ['800_800.in',           '800_MHz'+sep+'800.in_sparky',           800.0000, 800e6],
88     ['800_866.67.in',        '800_MHz'+sep+'866.67.in_sparky',        866.6666, 800e6],
89     ['800_933.33.in',        '800_MHz'+sep+'933.33.in_sparky',        933.3333, 800e6],
90     ['800_933.33.in.bis',    '800_MHz'+sep+'933.33.in.bis_sparky',    933.3333, 800e6],
91     ['800_1000.in',          '800_MHz'+sep+'1000.in_sparky',          1000.0000, 800e6]

```

```

92 ]
93
94 # Loop over the spectra.
95 for id, file, cpmg_frq, H_frq in data:
96     # Load the peak intensities.
97     spectrum.read_intensities(file=file, spectrum_id=id, int_method='height')
98
99     # Set the relaxation dispersion experiment type.
100    relax_disp.exp_type(spectrum_id=id, exp_type='SQ CPMG')
101
102    # Set the relaxation dispersion CPMG frequencies.
103    relax_disp.cpmg_frq(spectrum_id=id, cpmg_frq=cpmg_frq)
104
105    # Set the NMR field strength of the spectrum.
106    spectrometer.frequency(id=id, frq=H_frq)
107
108    # Relaxation dispersion CPMG constant time delay T (in s).
109    relax_disp.relax_time(spectrum_id=id, time=0.030)
110
111    # Specify the duplicated spectra.
112    spectrum.replicated(spectrum_ids=['500_133.33.in', '500_133.33.in.bis'])
113    spectrum.replicated(spectrum_ids=['500_533.33.in', '500_533.33.in.bis'])
114    spectrum.replicated(spectrum_ids=['500_933.33.in', '500_933.33.in.bis'])
115    spectrum.replicated(spectrum_ids=['800_133.33.in', '800_133.33.in.bis'])
116    spectrum.replicated(spectrum_ids=['800_533.33.in', '800_533.33.in.bis'])
117    spectrum.replicated(spectrum_ids=['800_933.33.in', '800_933.33.in.bis'])
118
119    # Peak intensity error analysis.
120    spectrum.error_analysis(subset=['500_reference.in', '500_66.667.in', '500_133.33.in', '500_
121    _133.33.in.bis', '500_200.in', '500_266.67.in', '500_333.33.in', '500_400.in', '500_
122    _466.67.in', '500_533.33.in', '500_533.33.in.bis', '500_600.in', '500_666.67.in', '500_
123    _733.33.in', '500_800.in', '500_866.67.in', '500_933.33.in', '500_933.33.in.bis', '500_
124    _1000.in'])
125    spectrum.error_analysis(subset=['800_reference.in', '800_66.667.in', '800_133.33.in', '800_
126    _133.33.in.bis', '800_200.in', '800_266.67.in', '800_333.33.in', '800_400.in', '800_
127    _466.67.in', '800_533.33.in', '800_533.33.in.bis', '800_600.in', '800_666.67.in', '800_
128    _733.33.in', '800_800.in', '800_866.67.in', '800_933.33.in', '800_933.33.in.bis', '800_
129    _1000.in'])
130
131    # Deselect unresolved spins.
132    deselect.read(file='unresolved', dir='500_MHz', res_num_col=1)
133    deselect.read(file='unresolved', dir='800_MHz', res_num_col=1)
134
135    # Auto-analysis execution.
136    #####
137
138    # Do not change!
139    Relax_disp(pipe_name=pipe_name, pipe_bundle=pipe_bundle, results_dir=RESULTS_DIR, models=
140    MODELS, grid_inc=GRID_INC, mc_sim_num=MC_NUM, modsel=MODSEL, insignificance=
141    INSIGNIFICANCE, numeric_only=NUMERIC_ONLY)

```

### 10.13.2 Dispersion script mode – imports

At the very start of the script are two import statements. This is simply the standard Python import system for modules. The first will import the `sep` variable which is the operating system independent directory separator:

```

4 # Python module imports.
5 from os import sep

```

This `sep` variable will be used later on in the script. The second import is that of the automated relaxation dispersion class `Relax_disp` which will be used at the very end of the script to perform the full analysis:

```

7 # relax module imports.
8 from auto_analyses.relax_disp import Relax_disp

```

### 10.13.3 Dispersion script mode – analysis variables

The next part of the script is the definition of a number of analysis variables. As the example in this section is for CPMG-type experiments, the relaxation dispersion models which will be used in the auto-analysis are:

```

14 # The dispersion models.
15 MODELS = ['R2eff', 'No Rex', 'CR72', 'N2 CPMG 2-site expanded']

```

This list can be expanded to most of the 2-site exchange models, for example as:

```
MODELS = ['R2eff', 'No Rex', 'LM63', 'CR72', 'IT99', 'TSMFK01', 'NS CPMG 2-site expanded']
```

But note that the selection of which models to use is incredibly important. Do not use models which are not suitable for the data as that will cause the final results to contain rubbish. If you have  $R_{1\rho}$ -type off-resonance data, the models could be changed to:

```
MODELS = ['R2eff', 'No Rex', 'DPL94', 'NS R1rho 2-site']
```

The next variable affects the optimisation precision:

```

17 # The grid search size (the number of increments per dimension).
18 GRID_INC = 21

```

The number of grid search increments may be decreased, but only after careful checking with a higher number of increments. Setting this value too low may place the initial optimisation too far away from the minimum. Although as-of-yet undetected and unpublished, if multiple local minima do exist then optimisation may not reach the global minimum. Too little grid search increments can also cause the total optimisation time to increase as the Nelder-Mead simplex optimisation together with the Logarithmic-barrier penalty function as used in the auto-analysis may require more time to reach the minimum.

The Monte Carlo simulation number `MC_NUM` variable affects the error estimate precision:

```

20 # The number of Monte Carlo simulations to be used for error analysis at the end of the
    analysis.
21 MC_NUM = 500

```

For accurate parameter errors this number should not be decreased. Ideally it should be increased however this will significantly increase the total analysis time. The next variable allows you to change the directory in which all results files from the auto-analysis will be saved.

```

23 # The results directory.
24 RESULTS_DIR = '.'

```

The MODSEL variable defines how the best dispersion model for the measured data is chosen:

```
26 # The model selection technique to use.
27 MODSEL = 'AIC'
```

For the automated analysis, currently only AIC, AICc, and BIC are supported. For details about these frequentist model selection techniques and their application to NMR data, see [d’Auvergne and Gooley \(2003\)](#). Post-analysis comparisons can also be preformed if desired. The NUMERIC\_ONLY variable can be used to choose if only numeric or all models will be used in the model selection for the final results:

```
29 # The flag for only using numeric models in the final model selection.
30 NUMERIC_ONLY = False
```

To only use numeric models in the model selection while allowing models such as 'CR72' to be optimised and used as the starting point for the numeric models, change this variable to:

```
NUMERIC_ONLY = True
```

The last variable allows spins with insignificant dispersion profiles to be deselected:

```
32 # The R2eff value in rad/s by which to judge insignificance. If the maximum difference
    between two points on all dispersion curves for a spin is less than this value, that
    spin will be deselected.
33 INSIGNIFICANCE = 1.0
```

This is often needed due to the errors in the dispersion curves being underestimated, hence the 'No Rex' model is not selected when clearly it should be. To use all data in the analysis, this variable should be set to 0.0.

#### 10.13.4 Dispersion script mode – initialisation of the data pipe

The data pipe is created using the lines:

```
40 # Create the data pipe.
41 pipe_name = 'base pipe'
42 pipe_bundle = 'relax_disp'
43 pipe.create(pipe_name=pipe_name, bundle=pipe_bundle, pipe_type='relax_disp')
```

The first two lines define variables for the data pipe name and the pipe bundle name. The pipe bundle is used to group together all of the data pipes created by the automated protocol. See section [4.2.1](#) on page [34](#) for more details.

The `pipe.create` user function will then create a relaxation dispersion specific data pipe labelled with the pipe and bundle names. The third argument sets the pipe type to that of relaxation dispersion. The rest of the script is used to fill this base data pipe with all of the data required for a dispersion analysis. The auto-analysis will then copy the data from this pipe as it sees fit.



### 10.13.5 Dispersion script mode – setting up the spin systems

The first thing which needs to be completed prior to any spin specific command is to generate the molecule, residue and spin data structures for storing the spin specific data. In the sample script above, this is generated from a plain text file with the sequence information, however a PDB file can be used instead (see the `structure.read_pdb` user function on page 460 for more details). In the case of the sample script, the command:

```
45 # Load the sequence.
46 sequence.read('fake_sequence.in', res_num_col=1, res_name_col=2)
```

will load residue names and numbers from the `fake_sequence.in` file into `relax`, creating one spin per residue. Then:

```
48 # Name the spins so they can be matched to the assignments, and the isotope for field
    strength scaling.
49 spin.name(name='N')
50 spin.isotope(isotope='15N')
```

will set up the spin information required for loading the peak intensity data from Sparky peak lists and for the analysis of the dispersion data.

### 10.13.6 Dispersion script mode – loading the data

To load the peak intensities into `relax`, a large data structure is first defined:

```
52 # The spectral data - spectrum ID, peak list file name, CPMG frequency (Hz), spectrometer
    frequency in Hertz.
53 data = [
54     ['500_reference.in',      '500_MHz'+sep+'reference.in_sparky',      None, 500e6],
55     ['500_66.667.in',        '500_MHz'+sep+'66.667.in_sparky',        66.6666, 500e6],
56     ['500_133.33.in',         '500_MHz'+sep+'133.33.in_sparky',         133.3333, 500e6],
57     ['500_133.33.in.bis',     '500_MHz'+sep+'133.33.in.bis_sparky',     133.3333, 500e6],
58     ['500_200.in',            '500_MHz'+sep+'200.in_sparky',            200.0000, 500e6],
59     ['500_266.67.in',         '500_MHz'+sep+'266.67.in_sparky',         266.6666, 500e6],
60     ['500_333.33.in',         '500_MHz'+sep+'333.33.in_sparky',         333.3333, 500e6],
61     ['500_400.in',            '500_MHz'+sep+'400.in_sparky',            400.0000, 500e6],
62     ['500_466.67.in',         '500_MHz'+sep+'466.67.in_sparky',         466.6666, 500e6],
63     ['500_533.33.in',         '500_MHz'+sep+'533.33.in_sparky',         533.3333, 500e6],
64     ['500_533.33.in.bis',     '500_MHz'+sep+'533.33.in.bis_sparky',     533.3333, 500e6],
65     ['500_600.in',            '500_MHz'+sep+'600.in_sparky',            600.0000, 500e6],
66     ['500_666.67.in',         '500_MHz'+sep+'666.67.in_sparky',         666.6666, 500e6],
67     ['500_733.33.in',         '500_MHz'+sep+'733.33.in_sparky',         733.3333, 500e6],
68     ['500_800.in',            '500_MHz'+sep+'800.in_sparky',            800.0000, 500e6],
69     ['500_866.67.in',         '500_MHz'+sep+'866.67.in_sparky',         866.6666, 500e6],
70     ['500_933.33.in',         '500_MHz'+sep+'933.33.in_sparky',         933.3333, 500e6],
71     ['500_933.33.in.bis',     '500_MHz'+sep+'933.33.in.bis_sparky',     933.3333, 500e6],
72     ['500_1000.in',           '500_MHz'+sep+'1000.in_sparky',           1000.0000, 500e6],
73     ['800_reference.in',      '800_MHz'+sep+'reference.in_sparky',      None, 800e6],
74     ['800_66.667.in',         '800_MHz'+sep+'66.667.in_sparky',         66.6666, 800e6],
75     ['800_133.33.in',         '800_MHz'+sep+'133.33.in_sparky',         133.3333, 800e6],
76     ['800_133.33.in.bis',     '800_MHz'+sep+'133.33.in.bis_sparky',     133.3333, 800e6],
77     ['800_200.in',            '800_MHz'+sep+'200.in_sparky',            200.0000, 800e6],
78     ['800_266.67.in',         '800_MHz'+sep+'266.67.in_sparky',         266.6666, 800e6],
79     ['800_333.33.in',         '800_MHz'+sep+'333.33.in_sparky',         333.3333, 800e6],
80     ['800_400.in',            '800_MHz'+sep+'400.in_sparky',            400.0000, 800e6],
81     ['800_466.67.in',         '800_MHz'+sep+'466.67.in_sparky',         466.6666, 800e6],
```

```

82     ['800_533.33.in',          '800_MHz'+sep+'533.33.in_sparky',          533.3333, 800e6],
83     ['800_533.33.in.bis',     '800_MHz'+sep+'533.33.in.bis_sparky',    533.3333, 800e6],
84     ['800_600.in',           '800_MHz'+sep+'600.in_sparky',          600.0000, 800e6],
85     ['800_666.67.in',        '800_MHz'+sep+'666.67.in_sparky',    666.6666, 800e6],
86     ['800_733.33.in',        '800_MHz'+sep+'733.33.in_sparky',    733.3333, 800e6],
87     ['800_800.in',           '800_MHz'+sep+'800.in_sparky',          800.0000, 800e6],
88     ['800_866.67.in',        '800_MHz'+sep+'866.67.in_sparky',    866.6666, 800e6],
89     ['800_933.33.in',        '800_MHz'+sep+'933.33.in_sparky',    933.3333, 800e6],
90     ['800_933.33.in.bis',     '800_MHz'+sep+'933.33.in.bis_sparky', 933.3333, 800e6],
91     ['800_1000.in',          '800_MHz'+sep+'1000.in_sparky',      1000.0000, 800e6]
92 ]

```

In Python terminology, this is a list of lists data structure. It is essentially a matrix of information which is used in the subsequent `for` loop. The comment explains what each element is. For  $R_{1\rho}$ -type experiments, the CPMG frequency column can be replaced with the spin-lock field strength. This data structure will need to be tailored to your data. It can be seen that the `sep` variable is now being used to specify that the Sparky files are either located in the `500_MHz` or `800_MHz` directories. It is used here to make this script independent of the operating system.

The Python `for` loop starts with the lines:

```

94 # Loop over the spectra.
95 for id, file, cpmg_freq, H_freq in data:

```

and includes all subsequently indented lines. This line of code takes the elements of the `data` data structure and splits it into 4 variables. Therefore for the first line, `id` will be set to `'500_reference.in'`, `file` will be set to `'500_MHz/reference.in_sparky'` on a Linux machine, `cpmg_freq` will be `None`, and `H_freq` will be 500 MHz. For  $R_{1\rho}$ -type data, you could change the `cpmg_freq` variable to `field` for example.

The first user function in the block loads the peak intensity data from the peak lists:

```

96 # Load the peak intensities.
97 spectrum.read_intensities(file=file, spectrum_id=id, int_method='height')

```

This assumes that peak heights were measured. All data will be tagged with the given ID string. For examples of peak list formats supported by `relax`, see Section 5.3.4 on page 56. The next step is to specify the dispersion experiment type for each spectrum:

```

99 # Set the relaxation dispersion experiment type.
100 relax_disp.exp_type(spectrum_id=id, exp_type='SQ CPMG')

```

This can be `'SQ CPMG'`, `'DQ CPMG'`, `'ZQ CPMG'`, `'MQ CPMG'`, `'1H SQ CPMG'`, `'1H MQ CPMG'` or `'R1rho'`. The next user function sets the CPMG frequencies for each spectrum:

```

102 # Set the relaxation dispersion CPMG frequencies.
103 relax_disp.cpmg_freq(spectrum_id=id, cpmg_freq=cpmg_freq)

```

For an  $R_{1\rho}$ -type experiment, these lines could be changed to:

```

# Set the relaxation dispersion R1rho spin lock field strength.
relax_disp.spin_lock_field(spectrum_id=id, field=field)

```

Then the NMR spectrometer field strength is set:

```

105     # Set the NMR field strength of the spectrum.
106     spectrometer.frequency(id=id, frq=H_frq)

```

And finally the relaxation time period is set with:

```

108     # Relaxation dispersion CPMG constant time delay T (in s).
109     relax_disp.relax_time(spectrum_id=id, time=0.030)

```

If exponential data has been collected rather than fixed time period data, then the data structure can have an additional column added for the relaxation times, and then this same user function can be used. The `for` loop will need one extra variable for the times, and this should be passed into this `relax_disp.relax_time` user function for the time argument.

Finally, once the `for` loop has completed, replicated spectra are defined with the commands:

```

111 # Specify the duplicated spectra.
112 spectrum.replicated(spectrum_ids=['500_133.33.in', '500_133.33.in.bis'])
113 spectrum.replicated(spectrum_ids=['500_533.33.in', '500_533.33.in.bis'])
114 spectrum.replicated(spectrum_ids=['500_933.33.in', '500_933.33.in.bis'])
115 spectrum.replicated(spectrum_ids=['800_133.33.in', '800_133.33.in.bis'])
116 spectrum.replicated(spectrum_ids=['800_533.33.in', '800_533.33.in.bis'])
117 spectrum.replicated(spectrum_ids=['800_933.33.in', '800_933.33.in.bis'])

```

### 10.13.7 Dispersion script mode – the rest of the setup

Once all the peak intensity data has been loaded a few calculations are required prior to optimisation. Firstly the peak intensities for individual spins needs to be averaged across replicated spectra. The peak intensity errors also have to be calculated using the standard deviation formula. These two operations are executed by the user functions:

```

119 # Peak intensity error analysis.
120 spectrum.error_analysis(subset=['500_reference.in', '500_66.667.in', '500_133.33.in', '500_133.33.in.bis', '500_200.in', '500_266.67.in', '500_333.33.in', '500_400.in', '500_466.67.in', '500_533.33.in', '500_533.33.in.bis', '500_600.in', '500_666.67.in', '500_733.33.in', '500_800.in', '500_866.67.in', '500_933.33.in', '500_933.33.in.bis', '500_1000.in'])
121 spectrum.error_analysis(subset=['800_reference.in', '800_66.667.in', '800_133.33.in', '800_133.33.in.bis', '800_200.in', '800_266.67.in', '800_333.33.in', '800_400.in', '800_466.67.in', '800_533.33.in', '800_533.33.in.bis', '800_600.in', '800_666.67.in', '800_733.33.in', '800_800.in', '800_866.67.in', '800_933.33.in', '800_933.33.in.bis', '800_1000.in'])

```

Here the 500 MHz and 800 MHz peak intensity errors have been calculated separately as they should not be the same.

Any spins which cannot be resolved due to peak overlap were included in a file called `unresolved`. This file can consist of optional columns of the molecule name, the residue name and number, and the spin name and number. The matching spins are excluded from the analysis by the user functions:

```

123 # Deselect unresolved spins.
124 deselect.read(file='unresolved', dir='500_MHz', res_num_col=1)
125 deselect.read(file='unresolved', dir='800_MHz', res_num_col=1)

```

### 10.13.8 Dispersion script mode – execution

Once the data has set up and you have modified your script to match your analysis needs, then the data pipe, pipe bundle and analysis variables are passed into the `Relax_disp` class. This is the final lines of the script:

```
129 # Auto-analysis execution.
130 #####
131
132 # Do not change!
133 Relax_disp(pipe_name=pipe_name, pipe_bundle=pipe_bundle, results_dir=RESULTS_DIR, models=
    MODELS, grid_inc=GRID_INC, mc_sim_num=MC_NUM, modsel=MODSEL, insignificance=
    INSIGNIFICANCE, numeric_only=NUMERIC_ONLY)
```

This will start the auto-analysis. If you are adventurous, you can replace this line with your own `grid_search`, `minimise`, and `monte_carlo.*` user function calls and design your own protocol. For ideas in designing your own advanced analysis, see the `auto_analysis/relax_disp.py` file.

## Part III

# Power users



## Chapter 11

# relax development

This chapter is for developers or those who would like to extend the functionality of relax. It is not required for using relax. If you would like to make modifications to the relax source code please subscribe to all the relax mailing lists (see the open source infrastructure chapter for more details). Announcements are sent to “relax-announce at gna.org” whereas “relax-users at gna.org” is the list where discussions about the usage of relax should be posted. “relax-devel at gna.org” is where all discussions about the development of relax including feature requests, program design, or any other discussions relating to relax’s structure or code should be posted. Finally, “relax-commits at gna.org” is where all changes to relax’s code and documentation, as well as changes to the web pages, are automatically sent to. Anyone interested in joining the project should subscribe to all four lists.

### 11.1 Version control using Subversion

The development of relax requires the use of the Subversion (SVN) version control software downloadable from <http://subversion.tigris.org/>. The source code to relax is stored in an SVN repository located at <http://svn.gna.org/svn/relax/>. Every single change which has ever made to the program is recorded within this repository. For more information see the open source infrastructure chapter 3 on page 29.

Although the downloadable distribution archives can be modified it is best that the most current and up to date revision (the *head* revision) is modified instead. More information about the basics of version control and how this is implemented in Subversion can be found in the Subversion book located at <http://svnbook.red-bean.com/>.

If you are not currently a relax developer you can check out the head revision by typing

```
$ svn co svn://svn.gna.org/svn/relax/trunk relax-trunk
```

Otherwise if you are a developer type

```
$ svn co svn+ssh://xxxxx@svn.gna.org/svn/relax/trunk relax-trunk
```

replacing xxxxx with your Gna! login name. If your version is out of date it can be updated to the latest revision by typing

```
$ svn up
```

Modifications can be made to these sources.

## 11.2 Coding conventions

The following conventions should be followed at all times for any code to be accepted into the relax repository. A Python script which tests if code meets relax's coding conventions is distributed with relax and is located at `scripts/code_validator`. The main reason for these conventions is for readability. By using a consistent coding style and a high comment ratio, the code becomes much easier to read for non-coders and those new to Python. It significantly decreases the barrier of entry into the relax source code for NMR spectroscopists.

### 11.2.1 Indentation

Indentation should be set to four spaces rather than a tab character. This is the recommendation given in the Python style guide found at <http://www.python.org/doc/essays/styleguide.html>. Emacs should automatically set the tabstop correctly. For vi add the following lines to the `vimrc` file:

```
set tabstop=4
set shiftwidth=4
set expandtab
```

For UNIX systems, including Linux and Mac OS X, the `vimrc` file is `~/.vimrc` whereas in MS Windows the file is `$VIM/_vimrc` which is usually `C:\Program Files\vim\_vimrc`. Certain versions of vim, those within the 6.2 series, contain a bug where the tabstop value cannot be changed using the `vimrc` file (although typing `:set tabstop=4` in vim will fix it). One solution is to edit the file `python.vim` which on GNU/Linux systems is located in the path `/usr/share/vim/ftplugin/`. It contains the two lines

```
" Python always uses a 'tabstop' of 8.
setlocal ts=8
```

If these lines are deleted the bug will be removed. Another way to fix the problem is to install newer versions of the run-time files (which will do the same thing).

### 11.2.2 Doc strings

The following are relax's conventions for docstrings. Many of these are Python conventions.

- The standard Python convention of a one line description separated from a detailed description by an empty line should be adhered to. This line must start with a capital letter and end in a period. This convention is required for certain docstring parsers (see the Python docs).



- All functions should have a docstring describing in detail the function, structure, and organisation of the code.
- A docstring should be followed by an empty line.
- Indentation of the docstring should be the same as that of the first line of code, excluding indented lists, etc.

An example of a single line docstring is:

```
1 def delete(self):
2     """Function for deleting all model-free data."""
```

An example of a multiline docstring is:

```
1 def aic(chi2, k, n):
2     """Akaike's Information Criteria (AIC).
3
4     The formula is::
5
6         AIC = chi2 + 2k
7
8     @param chi2:    The minimised chi-squared value.
9     @type chi2:    float
10    @param k:       The number of parameters in the model.
11    @type k:        int
12    @param n:       The dimension of the relaxation data set.
13    @type n:        int
14    @return:        The AIC value.
15    @rtype:         float
16    """
17
18    return chi2 + 2.0*k
19
```

In addition to the text descriptions, the docstrings use the [Epydoc](http://epydoc.sourceforge.net/fields.html) markup language to describe arguments, return values, and other information about the code. See <http://epydoc.sourceforge.net/fields.html> for a listing of all the epydoc fields allowed. This mark up language is important for the creation of the [API documentation](#) and to help developers understand the purpose and operation of the code.

### 11.2.3 Variable, function, and class names

In relax a mixture of both camel case (eg. CamelCase) and lower case with underscores is used. Despite the variability there are fixed rules which should be adhered to. These naming conventions should be observed at all times.

#### Variables and functions

For both variables and functions lower case with underscores between words is always used. This is for readability as the convention is much more fluent than camel case. A few rare exceptions exist, an example is the Brownian diffusion tensor parameter of anisotropy  $\mathfrak{D}_a$

which is referenced as `cdp.diff_tensor.Da`. As a rule though all new variable or function names should be kept as lower case. An example of this convention for both the variable name and function name is:

```

1  def assemble_param_vector(self, spin=None, spin_id=None, sim_index=None, model_type=
    None):
2      """Assemble the model-free parameter vector (as numpy array).
3
4      If the spin argument is supplied, then the spin_id argument will be ignored.
5
6      @keyword spin:      The spin data container.
7      @type spin:         SpinContainer instance
8      @keyword spin_id:   The spin identification string.
9      @type spin_id:      str
10     @keyword sim_index:  The optional MC simulation index.
11     @type sim_index:     int
12     @keyword model_type: The optional parameter set, one of 'all', 'diff', 'mf', or
        'local_tm'.
13     @type model_type:    str or None
14     @return:             An array of the parameter values of the model-free model.
15     @rtype:             numpy array
16     """
17
18     # Initialise.
19     param_vector = []
20
21     # Determine the model type.
22     if not model_type:
23         model_type = self.determine_param_set_type()
24
25     # Diffusion tensor parameters.
26     if model_type == 'diff' or model_type == 'all':
27         # Normal parameters.
28         if sim_index == None:
29             # Spherical diffusion.
30             if cdp.diff_tensor.type == 'sphere':
31                 param_vector.append(cdp.diff_tensor.tm)

```

## Classes

For classes relax uses a mix of camel case (for example all the `RelaxError` objects) and underscores (for example `Model_free`). The first letter in all cases is always capitalised. Generally the camel case is reserved for very low level classes which are involved in the program's infrastructure. Examples include the `RelaxError` code, the threading code, and the relax data store code. All the data analysis specific code, generic code, interface code, etc. uses underscores between the words with only the first letter capitalised. One exception is the space mapping class `OpenDX`, the reason being that the program is called `OpenDX`. An example is:

```

1  class Model_free_main:
2      """Class containing functions specific to model-free analysis."""
3
4      def are_mf_params_set(self, spin):
5          """Test if the model-free parameter values are set.
6
7          @param spin:    The spin container object.
8          @type spin:     SpinContainer instance

```

```

9         @return:          The name of the first parameter in the parameter list in which the
                           corresponding parameter value is None. If all parameters are set, then None is
                           returned.
10        @rtype:           str or None
11        """
12
13        # Deselected residue.
14        if spin.select == 0:
15            return

```

## Long names

If you have a look at a few relax source files, you will notice that the variable, function, and class names can be quite long. For example the model-free function `disassemble_param_vector()` and the RelaxError class `RelaxNoSequenceError`. While this is not normal for coding, it is an important component of relax as it facilitates the reading of the source code by a non-coder or someone not familiar with the codebase. Iteration counters can be single letter variables such as `i`, `j`, `k`, etc., however for all other variables, functions, and classes please attempt to use descriptive names which are instantly identifiable. Please minimise the amount of abbreviations used and only use those which are obvious. For example naming the parameter vector `self.param_vector`, the relaxation data `relax_data`, the model selection class `class Model_selection`, the type of spheroidal diffusion `spheroid_type`, etc.

### 11.2.4 Whitespace

The following conventions are for general code cleanliness and readability:

- Trailing whitespace should be avoided, although this is not very important.
- All functions should be preceded by two empty lines. The only exception is the first function of the class definition.
- Function arguments should be separated by a comma followed by a single space.
- The assignment operator should be surrounded by spaces, for example `tm_ = 1e-8`. The exception is function arguments where for example `self.classic\_colour(res\_num=None, width=0.3)`.
- The comparison operators should also be surrounded by spaces, e.g. `<`, `>`, `==`, `<=`, `>=`, `<>`, `!=`, `is`, and `in`.

An example which shows most of these conventions is:

```

1 class Internal:
2     """The internal relax structural data object.
3
4     The structural data object for this class is a container possessing a number of
5     different arrays corresponding to different structural information. These objects are
        described in the structural container docstring.
        """

```

```

6
7 def _bonded_atom(self, attached_atom, index, mol):
8     """Find the atom named attached_atom directly bonded to the atom located at the
9     index.
10
11     @param attached_atom: The name of the attached atom to return.
12     @type attached_atom: str
13     @param index: The index of the atom which the attached atom is attached
14     to.
15     @type index: int
16     @param mol: The molecule container.
17     @type mol: MolContainer instance
18     @return: A tuple of information about the bonded atom.
19     @rtype: tuple consisting of the atom number (int), atom name (str)
20     , element name (str), and atomic position (Numeric array of len 3)
21     """
22
23     # Init.
24     bonded_found = False
25
26     # No bonded atoms, so determine the connectivities.
27     if not mol.bonded[index]:
28         # Determine the molecule type if needed.
29         if not hasattr(mol, 'type'):
30             self._mol_type(mol)

```

### 11.2.5 Comments

Comments are a very important component within relax. In the current source code the percentage of comment lines relative to lines of code ranges from 15% to over 30% for different files. The average comment density would be close to 25%. The purpose of having so many comment lines, much more than you would expect from source code, is so that the relax's code is fully self documented. It allows someone who is not familiar with the codebase to read the code and quickly understand what is happening. It simplifies the process of learning and allows NMR spectroscopists who are not coders to dive into the code. If writing code for relax, please attempt to maintain the tradition by aiming towards a 25% comment ratio. The comment should be descriptive of what the code below it is supposed to do. Most importantly the comment explains why that code exists. The script `scripts/code_validator` can be used to check the comment density.

## 11.3 Submitting changes to the relax project

### 11.3.1 Submitting changes as a patch

The preferred method for submitting fixes and improvements to the relax source code is by the creation of a patch. If your changes are a fix make sure you have submitted a bug report to the bug tracker located at <https://gna.org/bugs/?group=relax> first. See section 3.3 on page 30 for more details. Two methods can be used to generate the patch – the Unix command `diff` or the Subversion program. The resultant file `patch` of either the `diff` or `svn` command described below can be posted to the “relax-devel at gna.org”

mailing list. Please label within your post which version of relax you modified or which revision the patch is for. Also try to create a commit log message according to the format described in section 11.4.4 on page 198 for one of the relax committers to use as a template for committing the change.

### 11.3.2 Modification of official releases – creating patches with diff

If your modifications have been made to the source code of one of the official relax releases (for example 2.1.1) then the Unix command `diff` can be used to create a patch. A patch file is simply the output of the diff command run with the recursive flag and presented in the ‘unified’ format. Therefore two directories need to be compared. If the original sources are located in the directory `relax_orig` and the modified sources in `relax_mod` then the patch can be created by typing

```
$ diff -ur relax_orig relax_mod > patch
```

### 11.3.3 Modification of the latest sources – creating patches with Subversion

If possible changes to the latest sources is preferred. Using the most up to date sources from the relax SVN repository will significantly aid the relax developers to incorporate your changes back into the main development line. To check out the current development line see section 11.1 on page 191 for details. Prior to submitting a patch to the mailing list your sources should be updated to include the most recent changes. To do this type

```
$ svn up
```

and note the revision number to include in your post. The update may cause a conflict if changes added to the repository clash with your modifications. If this occurs see the Subversion book at <http://svnbook.red-bean.com/> for details on how to resolve the conflict or submit a message to the relax-devel list.

Once the sources are up to date your changes can be converted into the patch text file. Using SVN creating a patch is easy. Just type

```
$ svn diff > patch
```

in the base relax directory.

## 11.4 Committers

### 11.4.1 Becoming a committer

Anyone can become a relax developer and obtain commit access to the relax repository. The main criteria for selection by the relax developers is to show good judgement, competence in producing good patches, compliance with the coding and commit log conventions, comportment on the mailing lists, not producing too many bugs, only taking on challenges which can be handled, and the skill in judging your own abilities. You will also need to

have an understanding of the concepts of version control specifically those relating to Subversion. The SVN book at <http://svnbook.red-bean.com/> contains all the version control information you will need. After a number of patches have been submitted and accepted any of the relax developers can propose that you receive commit access. If a number of developers agree while no one says no then commit access will be offered.

One area where coding ability can be demonstrated is within the relax test suite. The addition of tests, especially those where the relax internal data structures of the relax data store are scrutinised, can be a good starting point for learning the structure of relax. This is because the introduction of bugs has no effect on normal program execution. The relax test suite is an ideal proving ground.

If skills in only certain areas of relax development, for example in creation of the documentation, an understanding of C but not python, an understanding of solely the code of the user interface, or an understanding of the code specific to a certain type of data analysis methodology, then partial commit access may be granted. Although you will have the ability to make modifications to any part of the repository please make modifications only those areas for which you have permission.

### 11.4.2 Joining Gna!

The first step in becoming a committer is to create a Gna! account. Go to <https://gna.org/account/register.php> and type in a login name, password, real name, and the email address you would like to use. You will then get an automatic email from Gna! which will contain a link to activate your registration.

### 11.4.3 Joining the relax project

The second step in becoming a committer is to register to become a member of the relax project. Go to the Gna! website (<https://gna.org/>) and login. Click on ‘My Groups’ to go to <https://gna.org/my/groups.php>. In the section ‘Request for inclusion’ type ‘relax’ and hit enter. Select relax and write something in the comments. If you have been approved (see section 11.4.1) you will be added to the project committers list.

### 11.4.4 Format of the commit logs

If you are a relax developer and you have commit access to the repository the following conventions should be followed for all commit messages.

- The length of all lines in the commit log should never exceed 100 characters. This is so that the log message viewed in either emails or by the command prompt command `svn log` is legible.
- The first line of the commit log should be a short description or synopsis of the changes. If the change relates to a bug or a task, include the bug and task number using the notation `type #num` where type is either `bug`, `task` or `support` and `num` is the id number (for example `bug #6503`). This terminology is important because the

Gna! infrastructure knows how to translate this into a link to the issue. Also include a link to the issue.

- The second line should be blank.
- If the commit is a bug fix reported by a non-committer or if the commit originates from a patch posted by a non-committer the next lines should be reserved for crediting. The name of the person and their obfuscated email address (for example `edward_at_nmr-relax_dot_com`) should be included in the message.
- Next should be another blank line.
- If the commit relates to an entry in the bug tracker or to a discussion on the mailing lists then the web address of either the bug report or the mailing list archive message should be cited in the next section (separated from the synopsis or credit section by a blank line). All relevant links should be included to allow easy navigation between the repository, mailing lists, bug tracker, etc. An example is bug #5559 which is located at [https://gna.org/bugs/?func=detailitem&item\\_id=5559](https://gna.org/bugs/?func=detailitem&item_id=5559) and the post to “relax-devel at gna.org” describing the fix to that bug which is located at <https://mail.gna.org/public/relax-devel/2006-03/msg00013.html>.
- A full description with all the details can follow. This description should follow a blank line, can itself be sectioned using blank lines, and finally the log is terminated by one blank line at the end of the message.

An example of a commit message for the closure of a bug is:

Fixing the rest of bug #7241 (<https://gna.org/bugs/?7241>).

Bug #7241 was thought to be fixed in in r2591 and r2593, the commit messages describing the solution being located at <https://mail.gna.org/public/relax-commits/2006-09/msg00064.html> (Message-id: <E1GTgBi-0000R6-4h@subversion.gna.org>) for r2591 and <https://mail.gna.org/public/relax-commits/2006-10/msg00001.html> (Message-id: <E1GTt6C-0005rk-8q@subversion.gna.org>) for r2593.

However this was not the only place that the Scientific Python PDB data structure `peptide_chains` was being accessed. The chains were being accessed in the file ‘`pipe_control/sequence.py`’ when the sequence was being read out of the PDB file. This has now been modified with changes similar to r2591 and r2593.

An example of a commit message for changes relating to a task is:

This change implements half of task #3630 (<https://gna.org/task/?3630>).

The docstring in the generic optimisation function has been modified to clear up the ambiguity caused by supplying the option ‘None’ together with Newton optimisation.

One last commit message example is:

Added the API documentation creation (using Epydoc) to the Scons scripts.

The Scons target to create the HTML API documentation is called ‘`api_manual.html`’. The documentation can be created by typing: `$ scons api_manual.html`

The function ‘`compile_api_manual_html()`’ was added to the ‘`scons/manuals.py`’ file. This function runs the ‘`epydoc`’ command. All the Epydoc options are specified in that function.

### 11.4.5 Discussing major changes

If you are contemplating major changes, either for a bug fix, to add a completely new feature or user function for your own work, to improve the behaviour of part the program, or any other potentially disruptive modifications, please discuss these ideas on the relax-devel mailing list. If the planned changes have the potential to introduce problems the creation of a private branch may be suggested.

## 11.5 Branches

### 11.5.1 Branch creation

If a change is likely to be disruptive or cause breakages in the program, the use of your own temporary branch is recommended. This private branch is a complete copy of one of the main development lines wherein you can make changes without disrupting the other developers. Although called a private branch every change is visible to all other developers and each commit will result in an automatic email to the relax-commits mailing list. Other developers are even able to check out your branch and make modifications to it. Private branches can also be used for testing ideas. If the idea does not work the branch can be deleted from the repository (in reality the branch will always exist between the revision numbers of its creation and deletion and can always be resurrected). For example to create a branch from the main development line, the ‘trunk’, called `molmol_macros` whereby new Molmol macros are to be written, type

```
$ svn cp svn+ssh://xxxxx@svn.gna.org/svn/relax/trunk \  
svn+ssh://xxxxx@svn.gna.org/svn/relax/branches/molmol_macros
```

replacing `xxxxx` with your login name. You can then check out your private branch by typing

```
$ svn co svn+ssh://xxxxx@svn.gna.org/svn/relax/branches/molmol_macros
```

which will create a directory called `molmol_macros` containing all the relax source files. To have the files placed into a different directory, type the name of that directory at the end of the last command. Modifications can be made to this copy while normal development continues on the main line.

### 11.5.2 Keeping the branch up to date using `svnmerge.py`

As you develop your branch, changes will be occurring simultaneously within the main line. These changes should be merged into your branch on a regular basis to avoid large incompatible changes from forming between the two branches. To simplify this process, the `svnmerge.py` script located at <http://www.orcaware.com/svn/wiki/Svnmerge.py> can be used. It is best to download the trunk version from that page, unless that version is non-functional. Once you have this script, the merging from the main line to your private branch must be initialised by typing, from within the checked out copy of your branch,

```
$ svnmerge.py init
```



This then needs to be committed using the automatically generated log

```
$ svn ci -F svnmerge-commit-message.txt
```

To keep up to date, simply type

```
$ svnmerge.py merge
```

If conflicts have occurred please refer to the Subversion book at <http://svnbook.red-bean.com/> for information on how to resolve the problem. Otherwise, or once fixed, the main line revisions merged into your branch can be committed using the automatically generated log file:

```
$ svn ci -F svnmerge-commit-message.txt
```

### 11.5.3 Merging the branch back into the main line

Once you have completed the modifications desired for your branch, all changes which have occurred in the main line have been merged using `svnmerge.py`, and the changes have been approved for merging back into the main line – then your branch can be merged. First check out a copy of the main line,

```
$ svn co svn+ssh://xxxxx@svn.gna.org/svn/relax/trunk relax-trunk
```

or update a previously checked out version,

```
$ svn up
```

Then `svnmerge.py` can be utilised again. First initialise the merging process by typing, from within the checked out copy of the main line,

```
$ svnmerge.py init svn+ssh://xxxxx@svn.gna.org/svn/relax/branches/molmol_macros
```

Then commit the change

```
$ svn ci -F svnmerge-commit-message.txt
```

To merge the branch and commit the changes, type

```
$ svnmerge.py merge --bidirectional
```

```
$ svn ci -F svnmerge-commit-message.txt
```

Finally the merge properties need to be removed

```
$ svnmerge.py uninit -S svn+ssh://xxxxx@svn.gna.org/svn/relax/branches/molmol_macros
```

the changes committed

```
$ svn ci -F svnmerge-commit-message.txt
```

and your private branch deleted

```
$ svn rm svn+ssh://xxxxx@svn.gna.org/svn/relax/branches/molmol_macros
```

## 11.6 The SCons build system

The **SCons** build system was chosen over other build systems including **make** as it is a cross-platform build system which can be used in Unix, GNU/Linux, Mac OS X, and even MS Windows (the correct compilers are nevertheless required). Various components of the program **relax** can be created using the SCons utility. This includes C module compilation, manual creation, distribution creation, and cleaning up and removing certain files. The file **sconstruct** in the base **relax** directory, which consists of python code, directs the operation of SCons for the various functions.

### 11.6.1 SCons help

Multiple functions have been built into the **sconstruct** script and the modules of the **scons** directory. Each of these can be selected by specifying different “targets” when running SCons. A description of each target is given by the SCons help system which is accessible by typing **scons --help** in the base **relax** directory.

### 11.6.2 C module compilation

As described in the installation chapter, typing **scons** in the base directory will create the shared objects or dll files which are imported into Python as modules.

### 11.6.3 Compilation of the user manual (PDF version)

To create the PDF version of the **relax** user manual type

```
$ scons user_manual.pdf
```

in the base directory. SCons will then run a series of shell commands to create the manual from the **L<sup>A</sup>T<sub>E</sub>X** sources located in the **docs/latex** directory. This is dependent on the programs **latex**, **makeindex**, **dvips**, and **ps2pdf** being located within the environment’s path.

### 11.6.4 Compilation of the user manual (HTML version)

The HTML version of the **relax** user manual is made by typing

```
$ scons user_manual.html
```

in the base directory. One command calling the program **latex2html** will be executed which will create HTML pages from the **L<sup>A</sup>T<sub>E</sub>X** sources.

### 11.6.5 Compilation of the API documentation (HTML version)

The HTML version of the **relax** API documentation is made by typing

```
$ scons api_manual.html
```

in the base directory. The programs Epydoc and Graphviz are required for creating this documentation. The resultant HTML pages will be located in the directory `docs/api`.

### 11.6.6 Making distribution archives

Two types of distribution archive can be created from the currently checked out sources – the source and binary distributions. To create the source distribution type

```
$ scons source_dist
```

whereas to create the binary distribution, whereby the C modules are compiled and the resultant shared objects are included in the bziped tar file, type

```
$ scons binary_dist
```

If a binary distribution does not exist for your architecture feel free to create it yourself and contribute the archive to be included on the download pages. To do this you will need to check out the appropriate tagged branch from the relax subversion repository. If the current stable release is called 1.2.3 check out that branch by typing

```
$ svn co svn+ssh://bugman@svn.gna.org/svn/relax/tags/1.2.3 relax
```

replacing `bugman` with your user name if you are a relax developer, otherwise typing

```
$ svn co svn://svn.gna.org/svn/relax/tags/1.2.3 relax
```

Then build the binary distribution and send a message to the relax development mailing list. If compilation does not work please submit a bug to the bug tracker system at <https://gna.org/bugs/?group=relax> detailing the relax version, operation system, architecture, and any other information you believe will help to solve the problem. More information about donating binary distributions to the relax project is given in the open source infrastructure chapter (Chapter 3, page 29).

### 11.6.7 Cleaning up

If the command

```
$ scons clean
```

is run in the base directory all Python byte compiled files `*.pyc`, all C object files `*.o` and `*.os`, and any backup files with the extension `*.bak` are removed from all sub-directories. In addition any temporary L<sup>A</sup>T<sub>E</sub>X compilation files are removed from the `docs/latex` directory.

The more powerful command

```
$ scons clean_all
```

will, in addition to all the files removed by the `clean` target, remove all compiled C shared object files (`*.so`, `*.dylib`, `*.pyd`) and the `build` and `dist` directories created when building the Mac OS X application.

## 11.7 The core design of relax

To enable flexibility the internal structure of relax is modular. By construction the large collection of independent data analysis tools can be used individually and relatively easily by any new code implementing other forms of relaxation data analysis or even by other programs. The core modular design of the program is shown in Figure 11.1.

### 11.7.1 The divisions of relax's source code

relax's source code can be divided into five major areas: the initialisation code, the user interface (UI) code, the functional code, the number crunching code, and the code storing the program state.

**Initialisation:** The code belonging to this section initialises the program, processes the command-line arguments, and determines what mode the program will be run in including the choice of the UI.

**UI:** The current UI modes in relax include the prompt, the script and the GUI modes. These consist of separate code paths, all sitting on top of the underlying functional code. In the future, a web-based interface may be added.

**Functional code:** This code is the main part of the program. It includes anything which does not fit into the other sections and comprises the generic code, the specific code, and the specific setup code used as an interface between the two.

**Number crunching:** The computationally expensive code belongs in this section.

**Program state:** The state of the program is contained within the relax data store which is accessible from all parts of the program as a singleton object.

### 11.7.2 The major components of relax

Each of the boxes in Figure 11.1 represents a different grouping of code.

**relax:** The top level module. This initialises the entire program, tests the dependencies, sets up the multi-processor framework and specific processor fabric, and prints the program's introduction message.

**Command line arguments:** This code processes the arguments supplied to the program and decides whether to print the help message, initialise the prompt, execute a script, initialise a different UI, run the program in test mode, or run the program as a slave thread.

**Prompt:** The main user interface consisting of a Python prompt. The namespace of the interpreter contains the various user functions which are front ends to the generic code. The user functions are simply Python functions which test the supplied arguments to make sure they are of the correct type (string, integer, list, or any other type) before sending the values to the generic code. The code for the prompt is located in the directory `prompt/`.

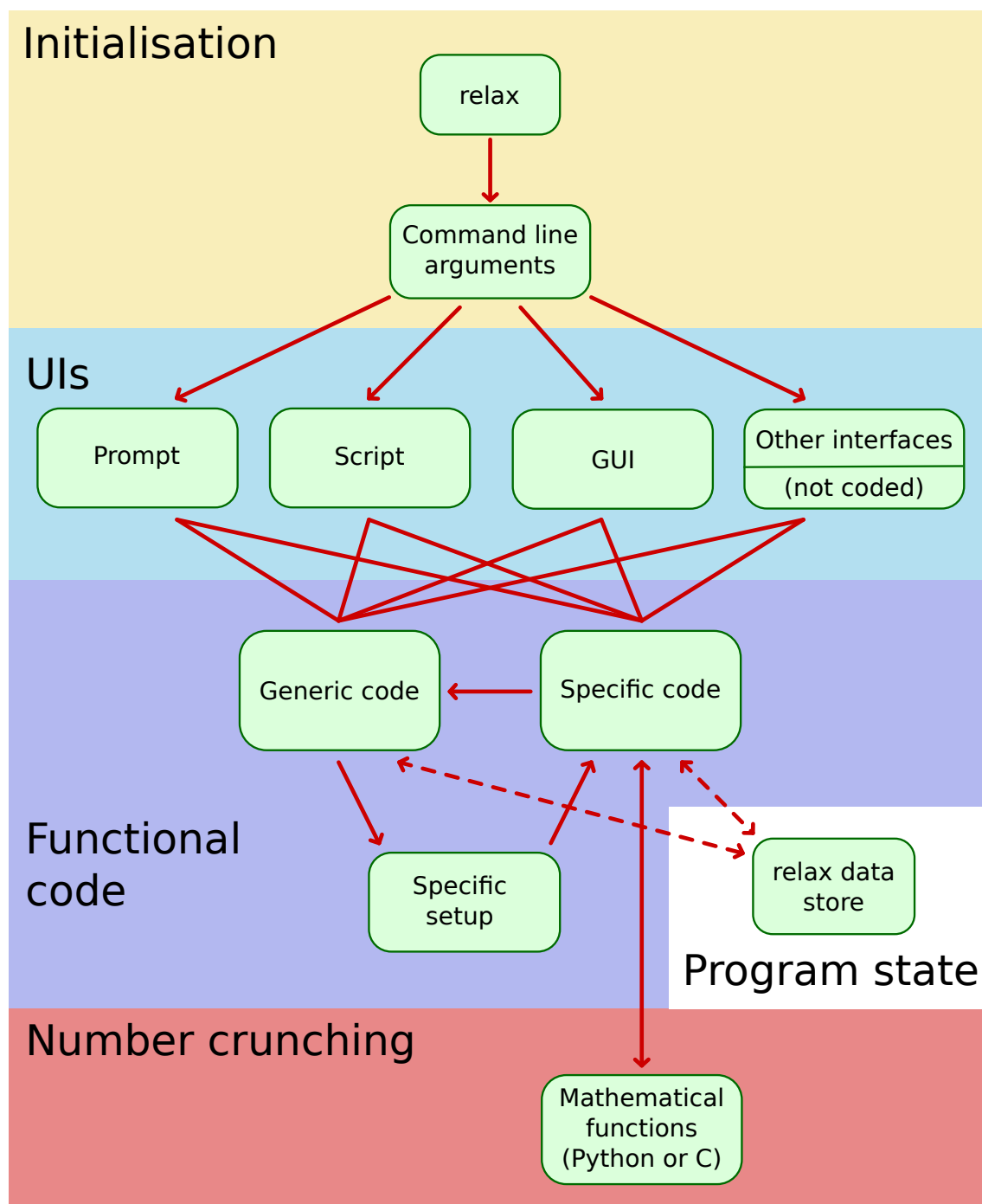


Figure 11.1: The core design of relax.

**Script:** If a script is supplied on the command line or executed within another user interface it will be run in the same namespace as that of the prompt. Hence the script has access to all the user functions available at the relax prompt. This allows commands which are typed at the prompt to be pasted directly and unmodified into a text file to be run as a script.

**GUI:** The graphical user interface code base is located in the `gui` directory.

**Other interfaces:** Any number of interfaces (for example a web-based interface or an ncurses interface) could be added to relax without modification of the current sources. This must be, without question, developed within the relax source code repository otherwise the code will not be maintainable in the future and will be almost impossible back into relax later on.

**Generic code:** This code includes classes and functions which are independent of the UI and not specific to a certain data pipe type, for example not being involved in model-free analysis, relaxation curve-fitting, the NOE calculation, and reduced spectral density mapping. All this code is located in the directory `pipe_control/`.

**Specific setup:** This code implements the internal interface between the generic and specific code. The generic code calls the specific setup asking for a specific function for the given data pipe type. For example by asking for the minimise function when the data pipe type is model-free analysis the model-free specific `minimise()` method is returned. Although the generic code accesses the specific code solely through this interface the specific code can access the generic code directly. The code is located in the file `specific_fns/specific_setup.py`.

**Specific code:** This is the code which is specific to the data pipe type – model-free analysis, relaxation curve-fitting, reduced spectral density mapping, and the NOE calculation. Each type is located in a separate file in the directory `specific_fns/`.

**Mathematical functions:** This is reserved for CPU intensive code involved in calculations. The code may be written in Python however C code can be used to significantly increase the speed of the calculations. For optimisation the code can include function evaluations, calculation of gradients, and calculation of Hessians. These functions are located in the directory `maths_fns/`.

**Data:** The program state stored in the relax data store singleton object. This class contains all the program data and is accessed by the generic and specific code. The mathematical functions may also access this data but this is not recommended. The structure is initialised by the file `data/__init__.py`.

## 11.8 The mailing lists for development

### 11.8.1 Private vs. public messages

If you would like to start a private discussion, please label your email as such. Private messages are however strongly discouraged, only start a private conversation if you really must.

If you receive a reply to a message you have sent, a bug report you have filed, etc. which has not been sent to the mailing list and has not been labelled as private, then the most likely explanation is that “reply-to-all” has not been used and hence the mailing list has not been included on the CC list. If this occurs, please ask the person if the message was meant to be private and refrain from discussing any of the comments within the post. Save these comments until after the person responds by saying that the message was private or re-sends the message to the mailing list. Try to encourage public messages if you think that the post need not be private and if you think that it would be useful for the mailing list archives.

For thread consistency, if you send a message which accidentally misses the mailing list, please do not then forward the previously sent message to the list. For better readability of the mailing list archives, it is best that you create an entirely new message responding to the original post. Just cut and paste your miss-directed message into your new message. That way the thread will be continuous – there will not be any messages missing from the middle of the thread in between the original post and your forwarded message.

To simplify the process of checking if the message was supposed to be private, you could copy-and-paste the following message (modifying it as you see fit):

```
Sorry in advance, but the following is the standard pre-composed response to a post not
sent to the relax mailing lists and not labelled as private.  If you would like to start
a private conversation about relax, please label your message as such.  If you really
must start a private exchange, please respond to this message saying so.  If your message
was meant to be sent to the relax mailing list, please send the message again.  For this,
please copy-and-paste your message, replying to the original (i.e. no forwarding), and
making sure that the mailing list is in the CC field by clicking on ‘reply-to-all’.
```

## 11.9 The bug, task, and support request trackers

relax’s infrastructure includes three different issue trackers. These are the [bug tracker](#), the [task tracker](#), and the [support request tracker](#).

### 11.9.1 Submitting a bug report

If someone reports a bug to one of the relax mailing lists, ask that person if they would like to create a bug report for that problem, pointing them to the submission web page. This is a good starting point to allow the person to become more involved in the relax project. If they do not respond or say that they would prefer not to, then you can create bug report for the issue linking to the original message and crediting the person for reporting the issue.

### 11.9.2 Assigning an issue to yourself

If you are a relax committer and see an issue which you would like to solve, please assign that issue to yourself before you start work on it. The assignment will prevent duplicated

efforts. If you can see an area where relax needs work, feel free to create a report within task tracker and then assign the task to yourself.

### 11.9.3 Closing an issue

When closing an issue (whether a bug report, a task, or a support request) a number of steps need to be taken. The tracker status should be changed to “Done” and the issue “Closed”. In addition, a message should be included which states the repository revision and the relax-commits mailing list archive link (with the message-id) in which the issue was solved. If multiple commits were required, then include all the revisions and as many links as possible (if a task required many commits, the relax-commits links could be skipped). An example is [bug #7402](#) where the closing comment was:

```
This documentation bug was fixed in r2641. The commit message is located at
https://mail.gna.org/public/relax-commits/2006-10/msg00073.html (Message-id:
<E1GYG41-0002kK-Jx@subversion.gna.org>).
```

## 11.10 Links, links, and more links

Creating links throughout the relax infrastructure is important for two major reasons – navigation and search engine indexing. When including a link to a post within the mailing list archives, please include the message-id email header. This enables subscribers to the mailing lists to search for the specific message within their local copy of the email messages.

### 11.10.1 Navigation

To be able to easily navigate between the relax infrastructure components – the bug tracker, the task tracker, the support request tracker, the relax-devel mailing list, the commit logs, and the SVN and CVS repositories – try to include as many links as possible.

For example a bug may first be reported on the relax-users mailing list, then placed within the bug tracker, discussed on relax-devel, a fix committed to the repository, and finally the bug report closed. To be able to follow this chain, links are very important (email message-ids are also important). When the bug is first added to the bug tracker, a link to the relax-users mailing list archive message and the message-id should be included. If you start a discussion on relax-devel, try to include links to the bug tracker entry and the relax-users message. When committing a fix to the repository, include links to the bug report, to the start of the thread in the mailing list archive, and the original message to relax-users. Then when the bug report is closed, include the revision number of the fix and a link to the relax-commits archive message (and message-id). By having all these links, it is then very easy for someone else to jump between the systems and follow the progression of the bug fix.

If you send a message referring to an old post which was sent the relax mailing lists, an old bug report, or any other archived information, please take the time to find that original information in the archives and include a link to it (including the message-id if relevant).



It is much more efficient for a single person to hunt down that message than for the many recipients of your post to search for the message themselves. By including the link, you decrease the overhead of following the mailing list.

### 11.10.2 Search engine indexing

Having a large web of links across relax's infrastructure aids in the search engine indexing of the mailing list archives and the <http://www.nmr-relax.com> web site. The web of links is useful for catching those Google bots. That way the Google searching of the mailing list archives located on the [communication web page](#) will be more up to date. However to increase the search engine ranking of the web site, links to <http://www.nmr-relax.com> from external sites is required. This is one reason why relax can be found at a number of sites across the web:

**Freecode:** New relax releases are announced not only on the [relax-announce](#) mailing list and on the relax [news](#) pages, but also on [Freecode](#). This used to be called Freshmeat.

**The mail archive:** This site archives all of the relax mailing lists, including [relax-announce](#), [relax-users](#), [relax-devel](#), and [relax-commits](#).

**Gmane:** Pronounced as “main”, the relax mailing lists are also archived at Gmane in numerous formats. The archived relax mailing lists include relax-announce ([thread](#), [blog](#), [NNTP](#), [RSS](#)), relax-users ([thread](#), [blog](#), [NNTP](#), [RSS](#)), relax-devel ([thread](#), [blog](#), [NNTP](#), [RSS](#)), and relax-commits ([thread](#), [blog](#), [NNTP](#), [RSS](#)).

**MARC - Mailing list ARChives:** This site archives all of the relax mailing lists, including [relax-announce](#), [relax-users](#), [relax-devel](#), and [relax-commits](#).

**CIA.vc:** This is the open source version control informant. CIA tracks open source projects in real-time. The relax real-time open source activity stats page is <http://cia.vc/stats/project/relax>. This website also has pages for each of the relax developers (in alphabetical order): [Edward d’Auvergne](#), [Michael Bieri](#), [Chris MacRaid](#), [Sébastien Morin](#), [Andrew Perry](#), [Han Sun](#), [Gary Thompson](#).

**LinuxLinks.com:** LinuxLinks.com, the Linux portal, is a website listing many Linux software projects. relax can be found on the [Software:Scientific:Biology:Proteins](#) page.

**Softpedia:** This is the encyclopedia of free software downloads. The relax page on Softpedia is <http://linux.softpedia.com/get/Science/relax-22351.shtml>. The relax developers pages are: [Edward d’Auvergne](#).

**Pro-Linux:** Diese ist eine der größten deutschsprachigen Seiten zum Thema Linux. The relax page is <http://www.pro-linux.de/cgi-bin/DBApp/check.cgi?ShowApp..10010.100>.



## Part IV

# Advanced topics



## Chapter 12

# Optimisation

### 12.1 Implementation

#### 12.1.1 The interface

Optimisation or minimisation is available in relax via the `grid_search` and `minimise` user functions. The mathematical model optimised depends on the current data pipe type – it is implemented differently for each specific analysis. For analyses such as the steady state NOE (Chapter 6) or reduced spectral density mapping (Chapter 8), the solution can be found by direct calculation rather than optimisation. In these cases, the `calc` user function should be used instead.

#### 12.1.2 The minfx package

To minimise target functions within relax, the minfx optimisation library is used (<https://gna.org/projects/minfx/>). This Python package is bundled with the official relax distribution archives. If you are using a version of relax checked out directly from the source code repository, you will need to manually install minfx as a standard Python package.

The minfx library originated as one of relax’s packages, but has been spun off as its own project for the benefit of other scientific, analytical, or numerical projects. Minfx is complete, very stable, well tested. Numerous optimisation algorithms are supported and can be clustered into three major categories – the line search methods, the trust-region methods, and the conjugate gradient methods.

The supported line search methods include:

- Steepest descent,
- Back-and-forth coordinate descent,
- Quasi-Newton BFGS,
- Newton,

- Newton-CG.

The supported trust-region methods include:

- Cauchy point,
- Dogleg,
- CG-Steihaug,
- Exact trust region.

The supported conjugate gradient methods include:

- Fletcher-Reeves,
- Polak-Ribière,
- Polak-Ribière +,
- Hestenes-Stiefel.

In addition, the following miscellaneous algorithms are implemented:

- Grid search,
- Nelder-Mead simplex,
- Levenberg-Marquardt.

The step selection subalgorithms include:

- Backtracking line search,
- Nocedal and Wright interpolation based line search,
- Nocedal and Wright line search for the Wolfe conditions,
- More and Thuente line search,
- No line search.

The Hessian modification subalgorithms include:

- Unmodified Hessian,
- Eigenvalue modification,
- Cholesky with added multiple of the identity,
- The Gill, Murray, and Wright modified Cholesky algorithm,

- The Schnabel and Eskow 1999 algorithm.

All methods can be constrained by:

- The Method of Multipliers (also known as the Augmented Lagrangian),
- The logarithmic barrier function.

These lists may be out of date, so please see the minfx website for additional information.

## 12.2 The optimisation space

The optimisation of the parameters of an arbitrary model is dependent on a function  $f$  which takes the current parameter values  $\theta \in \mathbb{R}^n$  and returns a single real value  $f(\theta) \in \mathbb{R}$  corresponding to position  $\theta$  in the  $n$ -dimensional space. For it is that single value which is minimised as

$$\hat{\theta} = \arg \min_{\theta} f(\theta), \quad (12.1)$$

where  $\hat{\theta}$  is the parameter vector which is equal to the argument which minimises the function  $f(\theta)$ . In most analyses in relax,  $f(\theta)$  is the chi-squared equation

$$\chi^2(\theta) = \sum_{i=1}^n \frac{(y_i - y_i(\theta))^2}{\sigma_i^2}, \quad (12.2)$$

where  $i$  is the summation index over all data,  $y_i$  is the experimental data,  $y_i(\theta)$  is the back calculated data, and  $\sigma_i$  is the experimental error.

## 12.3 Topology of the space

The problem of finding the minimum is complicated by the fact that optimisation algorithms are blind to the curvature of the complete space. Instead they rely on topological information about the current and, sometimes, the previous parameter positions in the space. The techniques use this information to walk iteratively downhill to the minimum.

### 12.3.1 The function value

At the simplest level all minimisation techniques require at least a function which will supply a single value for different parameter values  $\theta$ . Conceptually this is the height of the space at the current position. For certain algorithms, such as a simplex minimisation, this single value suffices.

### 12.3.2 The gradient

Most techniques also utilise the gradient at the current position. Although symbolically complex in the case of model-free analysis, for example, the gradient can simply be calculated as the vector of first partial derivatives of the chi-squared equation with respect to each parameter. It is defined as

$$\nabla = \begin{pmatrix} \frac{\partial}{\partial \theta_1} \\ \frac{\partial}{\partial \theta_2} \\ \vdots \\ \frac{\partial}{\partial \theta_n} \end{pmatrix} \quad (12.3)$$

where  $n$  is the total number of parameters in the model.

The gradient is supplied as a second function to the algorithm which is then utilised in diverse ways by different optimisation techniques. The function value together with the gradient can be combined to construct a linear or planar description of the space at the current parameter position by first-order Taylor series approximation

$$f(\theta_k + x) \approx f_k + x^T \nabla f_k, \quad (12.4)$$

where  $f_k$  is the function value at the current parameter position  $\theta_k$ ,  $\nabla f_k$  is the gradient at the same position, and  $x$  is an arbitrary vector. By accumulating information from previous parameter positions a more comprehensive geometric description of the curvature of the space can be exploited by the algorithm for more efficient optimisation.

An example of a powerful algorithm which requires both the value and gradient at current parameter values is the BFGS quasi-Newton minimisation. The gradient is also essential for the use of the Method of Multipliers constraints algorithm (also known as the Augmented Lagrangian algorithm).

### 12.3.3 The Hessian

The best and most comprehensive description of the space is given by the quadratic approximation of the topology which is generated from the combination of the function value, the gradient, and the Hessian. From the second-order Taylor series expansion the quadratic model of the space is

$$f(\theta_k + x) \approx f_k + x^T \nabla f_k + \frac{1}{2} x^T \nabla^2 f_k x, \quad (12.5)$$

where  $\nabla^2 f_k$  is the Hessian, which is the symmetric matrix of second partial derivatives of the function, at the position  $\theta_k$ . The Hessian is the matrix of second partial derivatives and is defined as

$$\nabla^2 = \begin{pmatrix} \frac{\partial^2}{\partial \theta_1^2} & \frac{\partial^2}{\partial \theta_1 \partial \theta_2} & \cdots & \frac{\partial^2}{\partial \theta_1 \partial \theta_n} \\ \frac{\partial^2}{\partial \theta_2 \partial \theta_1} & \frac{\partial^2}{\partial \theta_2^2} & \cdots & \frac{\partial^2}{\partial \theta_2 \partial \theta_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^2}{\partial \theta_n \partial \theta_1} & \frac{\partial^2}{\partial \theta_n \partial \theta_2} & \cdots & \frac{\partial^2}{\partial \theta_n^2} \end{pmatrix}. \quad (12.6)$$



The order in which the partial derivatives are calculated is inconsequential, hence the Hessian is symmetric.

As the Hessian is computationally expensive a number of optimisation algorithms try to approximate it, the BFGS algorithm being a notable example. The most powerful minimisation algorithm for model-free analysis – Newton optimisation – requires the value, gradient, and Hessian at the current parameter values.

## 12.4 Optimisation algorithms

Prior to minimisation, all optimisation algorithms require a starting position within the optimisation space. This initial parameter vector is found by employing a coarse grid search – chi-squared values at regular positions spanning the space are calculated and the grid point with the lowest value becomes the starting position. The grid search itself is an optimisation technique. As it is computationally expensive the number of grid points needs to be kept to a minimum. Hence the initial parameter values are a rough and imprecise approximation of the local minimum.

Once the starting position has been determined by the grid search the optimisation algorithm can be executed. The number of algorithms developed within the mathematical field of optimisation is considerable. They can nevertheless be grouped into one of a small number of major categories based on the fundamental principles of the technique. These include the line search methods, the trust region methods, and the conjugate gradient methods. For more details on the algorithms described below see [Nocedal and Wright \(1999\)](#).

### 12.4.1 Line search methods

The defining characteristic of a line search algorithm is to choose a search direction  $p_k$  and then to find the minimum along that vector starting from  $\theta_k$  ([Nocedal and Wright, 1999](#)). The distance travelled along  $p_k$  is the step length  $\alpha_k$  and the parameter values for the next iteration are

$$\theta_{k+1} = \theta_k + \alpha_k p_k. \quad (12.7)$$

The line search algorithm determines the search direction  $p_k$  whereas the value of  $\alpha_k$  is found using an auxiliary step-length selection algorithm.

#### The steepest descent algorithm

One of the simplest line search methods is the steepest descent algorithm. The search direction is simply the negative gradient,  $p_k = -\nabla f_k$ , and hence the direction of maximal descent is always followed. This method is inefficient – the linear rate of convergence requires many iterations of the algorithm to reach the minimum and it is susceptible to being trapped on saddle points within the space.

### The coordinate descent algorithm

The coordinate descent algorithms are a simplistic group of line search methods whereby the search directions alternate between vectors parallel to the parameter axes. For the back-and-forth coordinate descent the search directions cycle in one direction and then back again. For example for a three parameter model the search directions cycle  $\theta_1, \theta_2, \theta_3, \theta_2, \theta_1, \theta_2, \dots$ , which means that each parameter of the model is optimised one by one. The method becomes less efficient when approaching the minimum as the step length  $\alpha_k$  continually decreases (ibid.).

### The BFGS algorithm

The quasi-Newton methods begin with an initial guess of the Hessian and update it at each iteration using the function value and gradient. Therefore the benefits of using the quadratic model of (12.5) are obtained without calculating the computationally expensive Hessian. The Hessian approximation  $B_k$  is updated using various formulae, the most common being the BFGS formula (Broyden, 1970; Fletcher, 1970; Goldfarb, 1970; Shanno, 1970). The search direction is given by the equation  $p_k = -B_k^{-1}\nabla f_k$ . The quasi-Newton algorithms can attain a superlinear rate of convergence, being superior to the steepest descent or coordinate descent methods.

### The Newton algorithm

The most powerful line search method when close to the minimum is the Newton search direction

$$p_k = -\nabla^2 f_k^{-1} \nabla f_k. \quad (12.8)$$

This direction is obtained from the derivative of (12.5) which is assumed to be zero at the minimum of the quadratic model. The vector  $p_k$  points from the current position to the exact minimum of the quadratic model of the space. The rate of convergence is quadratic, being superior to both linear and superlinear convergence. The technique is computationally expensive due to the calculation of the Hessian. It is also susceptible to failure when optimisation commences from distant positions in the space as the Hessian may not be positive definite and hence not convex, a condition required for the search direction both to point downhill and to be reasonably oriented. In these cases the quadratic model is a poor description of the space. This algorithm is also known as the Newton-Raphson method.

### The Newton conjugate gradient algorithm

A practical Newton algorithm which is robust for distant starting points is the Newton conjugate gradient method (Newton-CG). This line search method, which is also called the truncated Newton algorithm, finds an approximate solution to Equation (12.8) by using a conjugate gradient (CG) sub-algorithm. Retaining the performance of the pure Newton algorithm, the CG sub-algorithm guarantees that the search direction is always downhill as the method terminates when negative curvature is encountered.

### The auxiliary step-length selection algorithm

Once the search direction has been determined by the above algorithms the minimum along that direction needs to be determined. Not to be confused with the methodology for determining the search direction  $p_k$ , the line search itself is performed by an auxiliary step-length selection algorithm to find the value  $\alpha_k$ . A number of step-length selection methods can be used to find a minimum along the line  $\theta_k + \alpha_k p_k$ . One is the backtracking line search of Nocedal and Wright (1999). This method is inexact – it takes a starting step length  $\alpha_k$  and decreases the value until a sufficient decrease in the function is found. Another is the line search method of Moré and Thunberg (1994). Designed to be robust, the MT algorithm finds the exact minimum along the search direction and guarantees sufficient decrease.

#### 12.4.2 Trust region methods

In the trust region class of algorithms the curvature of the space is modelled quadratically by (12.5). This model is assumed to be reliable only within a region of trust defined by the inequality  $\|p\| \leq \Delta_k$  where  $p$  is the step taken by the algorithm and  $\Delta_k$  is the radius of the  $n$ -dimensional sphere of trust (Nocedal and Wright, 1999). The solution sought for each iteration of the algorithm is

$$\min_{p \in \mathbb{R}^n} m_k(p) = f_k + p^T \nabla f_k + \frac{1}{2} p^T B_k p, \quad \text{s.t. } \|p\| \leq \Delta_k, \quad (12.9)$$

where  $m_k(p)$  is the quadratic model,  $B_k$  is a positive definite matrix which can be the true Hessian as in the Newton model or an approximation such as the BFGS matrix, and  $\|p\|$  is the Euclidean norm of  $p$ . The trust region radius  $\Delta_k$  is modified dynamically during optimisation – if the quadratic model is found to be a poor representation of the space the radius is decreased whereas if the quadratic model is found to be reasonable the radius is increased to allow larger, more efficient steps to be taken.

### The Cauchy point algorithm

The Cauchy point algorithm is similar in concept to the steepest descent line search algorithm. The Cauchy point is the point lying on the gradient which minimises the quadratic model subject to the step being within the trust region. By iteratively finding the Cauchy point the local minimum can be found. The convergence of the technique is inefficient, being similar to that of the steepest descent algorithm.

### The dogleg algorithm

In changing the trust region radius the exact solutions to (12.9) map out a curved trajectory which starts parallel to the gradient for small radii. The end of the trajectory, which occurs for radii greater than the step length, is the bottom of the quadratic model. The dogleg algorithm attempts to follow a similar path by first finding the minimum along the gradient and then finding the minimum along a trajectory from the current point to the bottom

of the quadratic model. The minimum along the second path is either the trust region boundary or the quadratic solution. The matrix  $B_k$  of (12.9) can be the BFGS matrix, the unmodified Hessian, or a Hessian modified to be positive definite.

### Steihaug's algorithm

Another trust region algorithm is Steihaug's modified conjugate gradient approach (Steihaug, 1983). For each step  $k$  an iterative technique is used which is almost identical to the standard conjugate gradient procedure except for two additional termination conditions. The first is if the next step is outside the trust region, the second is if a direction of zero or negative curvature is encountered.

### The exact trust region

An almost exact solution to (12.9) can be found using an algorithm described in Nocedal and Wright (1999). This exact trust region algorithm aims to precisely find the minimum of the quadratic model  $m_k$  of the space within the trust region  $\Delta_k$ . Any matrix  $B_k$  can be used to construct the quadratic model. However, the technique is computationally expensive.

## 12.4.3 Conjugate gradient methods

The conjugate gradient algorithm (CG) was originally designed as a mathematical technique for solving a large system of linear equations Hestenes and Stiefel (1952), but was later adapted to solving nonlinear optimisation problems (Fletcher and Reeves, 1964). The technique loops over a set of directions  $p_0, p_1, \dots, p_n$  which are all conjugate to the Hessian (Nocedal and Wright, 1999), a property defined as

$$p_i^T \nabla^2 f_k p_j = 0, \quad \text{for all } i \neq j. \quad (12.10)$$

By performing line searches over all directions  $p_j$  the solution to the quadratic model (12.5) of the position  $\theta_k$  will be found in  $n$  or less iterations of the CG algorithm where  $n$  is the total number of parameters in the model. The technique performs well on large problems with many parameters as no matrices are calculated or stored. The algorithms perform better than the steepest descent method and preconditioning of the system is used to improve optimisation. Preconditioned techniques include the Fletcher-Reeves algorithm which was the original conjugate gradient optimisation technique (Fletcher and Reeves, 1964), the Polak-Ribière method (Polak and Ribière, 1969), a modified Polak-Ribière method called the Polak-Ribière + method (Nocedal and Wright, 1999), and the Hestenes-Stiefel algorithm which originates from a formula in Hestenes and Stiefel (1952). As a line search is performed to find the minimum along each conjugate direction both the backtracking and Moré and Thuente auxiliary step-length selection algorithms will be tested with the CG algorithms.

### 12.4.4 Hessian modifications

The Newton search direction, used in both the line search and trust region methods, is dependent on the Hessian being positive definite for the quadratic model to be convex so that the search direction points sufficiently downhill. This is not always the case as saddle points and other non-quadratic features of the space can be problematic. Two classes of algorithms can be used to handle this situation. The first involves using the conjugate gradient method as a sub-algorithm for solving the Newton problem for the step  $k$ . The Newton-CG line search algorithm described above is one such example. The second class involves modifying the Hessian prior to, or at the same time as, finding the Newton step to guarantee that the replacement matrix  $B_k$  is positive definite. The convexity of  $B_k$  is ensured by its eigenvalues all being positive.

The first modification uses the Cholesky factorisation of the matrix  $B_k$ , initialised to the true Hessian, to test for convexity (Algorithm 6.3 of Nocedal and Wright (1999)). If factorisation fails the matrix is not positive definite and a constant  $\tau_k$  times the identity matrix  $I$  is then added to  $B_k$ . The constant originates from the Robbins norm of the Hessian  $\|\nabla^2 f_k\|_F$  and is steadily increased until the factorisation is successful. The resultant Cholesky lower triangular matrix  $L$  can then be used to find the approximate Newton direction. If  $\tau_k$  is too large the convergence of this technique can approach that of the steepest descent algorithm.

The second method is the Gill, Murray, and Wright (GMW) algorithm (Gill et al., 1981) which modifies the Hessian during the execution of the Cholesky factorisation  $\nabla^2 f_k = LIL^T$ , where  $L$  is a lower triangular matrix and  $D$  is a diagonal matrix. Only a single factorisation is required. As rows and columns are interchanged during the algorithm the technique may be slow for large problems such as the optimisation of the model-free parameters of all spins together with the diffusion tensor parameters. The rate of convergence of the technique is quadratic.

### 12.4.5 Other methods

#### Nelder-Mead simplex

Some optimisation algorithms cannot be classified within line search, trust region, or conjugate gradient categories. For example the well known Nelder-Mead simplex optimisation algorithm. The technique is often used as the only the function value is employed and hence the derivation of the gradient and Hessian can be avoided. The simplex is created as an  $n$ -dimensional geometric object with  $n + 1$  vertices. The first vertex is the starting position. Each of the other  $n$  vertices are created by shifting the starting position by a small amount parallel to one of unit vectors defining the coordinate system of the space. Four simple rules are used to move the simplex through the space: reflection, extension, contraction, and a shrinkage of the entire simplex. The result of these movements is that the simplex moves in an ameoboid-like fashion downhill, shrinking to pass through tight gaps and expanding to quickly move through non-convoluted space, eventually finding the minimum.

Key to these four movements is the pivot point, the centre of the face created by the  $n$  vertices with the lowest function values. The first movement is a reflection – the vertex

with the greatest function value is reflected through the pivot point on the opposite face of the simplex. If the function value at this new position is less than all others the simplex is allowed to extend – the point is moved along the line to twice the distance between the current position and the pivot point. Otherwise if the function value is greater than the second highest value but less than the highest value, the reflected simplex is contracted. The reflected point is moved to be closer to the simplex, its position being half way between the reflected position and the pivot point. Otherwise if the function value at the reflected point is greater than all other vertices, then the original simplex is contracted – the highest vertex is moved to a position half way between the current position and the pivot point. Finally if none of these four movements yield an improvement, then the simplex is shrunk halfway towards the vertex with the lowest function value.

### Levenberg-Marquardt algorithm

Another algorithm is the commonly used Levenberg-Marquardt algorithm ([Levenberg, 1944](#); [Marquardt, 1963](#)). This is the algorithm used by the model-free analysis programs `Modelfree4`, `Dasha`, and `Tensor2`. This technique is designed for least-squares problems to which the chi-squared equation ([12.2](#)) belongs. The key to the algorithm is the replacement of the Hessian with the Levenberg-Marquardt matrix  $J^T J + \lambda I$ , where  $J$  is the Jacobian of the system calculated as the matrix of partial derivatives of the residuals,  $\lambda > 0$  is a factor related to the trust-region radius, and  $I$  is the identity matrix. The algorithm is conceptually allied to the trust region methods and its performance varies finely between that of the steepest descent and the pure Newton step. When far from the minimum  $\lambda$  is large and the algorithm takes steps close to the gradient; when in vicinity of the minimum  $\lambda$  heads towards zero and the steps taken approximate the Newton direction. Hence the algorithm avoids the problems of the Newton algorithm when non-convex curvature is encountered and approximates the Newton step in convex regions of the space.

The technique does have one weak point though which is often mentioned only in the small print. That is that the algorithm catastrophically fails when the Levenberg-Marquardt matrix is singular. This occurs whenever a parameter is undefined. For example in a model-free analysis if the order parameter is one, then the corresponding internal correlation time can take any value. Performing a grid search with such undefined points greatly amplifies the problem and is the reason why many published model-free papers contain results with order parameters fixed at one ([d’Auvergne and Gooley, 2008a](#)).

## 12.5 Constraint algorithms

To guarantee that the minimum will still be reached the implementation of constraints limiting the parameter values together with optimisation algorithms is not a triviality. For this to occur the space and its boundaries must remain smooth thereby allowing the algorithm to move along the boundary to either find the minimum along the limit or to slide along the limit and then move back into the centre of the constrained space once the curvature allows it.

### 12.5.1 Method of Multipliers algorithm

One of the most powerful approaches is the Method of Multipliers (Nocedal and Wright, 1999), also known as the Augmented Lagrangian. Instead of a single optimisation the algorithm is iterative with each iteration consisting of an independent unconstrained minimisation on a sequentially modified space. When inside the limits the function value is unchanged but when outside a penalty, which is proportional to the distance outside the limit, is added to the function value. This penalty, which is based on the Lagrange multipliers, is smooth and hence the gradient and Hessian are continuous at and beyond the constraints. For each iteration of the Method of Multipliers the penalty is increased until it becomes impossible for the parameter vector to be in violation of the limits. This approach allows the parameter vector  $\theta$  outside the limits yet the successive iterations ensure that the final results will not be in violation of the constraint.

For inequality constraints, each iteration of the Method of Multipliers attempts to solve the quadratic sub-problem

$$\min_{\theta} \mathfrak{L}_A(\theta, \lambda^k; \mu_k) \stackrel{\text{def}}{=} f(\theta) + \sum_{i \in \mathfrak{I}} \Psi(c_i(\theta), \lambda_i^k; \mu_k), \quad (12.11)$$

where the function  $\Psi$  is defined as

$$\Psi(c_i(\theta), \lambda^k; \mu_k) = \begin{cases} -\lambda^k c_i(\theta) + \frac{1}{2\mu_k} c_i^2(\theta) & \text{if } c_i(\theta) - \mu_k \lambda^k \leq 0, \\ -\frac{\mu_k}{2} (\lambda^k)^2 & \text{otherwise.} \end{cases} \quad (12.12)$$

In (12.11),  $\theta$  is the parameter vector;  $\mathfrak{L}_A$  is the Augmented Lagrangian function;  $k$  is the current iteration of the Method of Multipliers;  $\lambda^k$  are the Lagrange multipliers which are positive factors such that, at the minimum  $\hat{\theta}$ ,  $\nabla f(\hat{\theta}) = \lambda_i \nabla c_i(\hat{\theta})$ ;  $\mu_k > 0$  is the penalty parameter which decreases to zero as  $k \rightarrow \infty$ ;  $\mathfrak{I}$  is the set of inequality constraints; and  $c_i(\theta)$  is an individual constraint value. The Lagrange multipliers are updated using the formula

$$\lambda_i^{k+1} = \max(\lambda_i^k - c_i(\theta)/\mu_k, 0), \quad \text{for all } i \in \mathfrak{I}. \quad (12.13)$$

The gradient of the Augmented Lagrangian is

$$\nabla \mathfrak{L}_A(\theta, \lambda^k; \mu_k) = \nabla f(\theta) - \sum_{i \in \mathfrak{I} | c_i(\theta) \leq \mu_k \lambda_i^k} \left( \lambda_i^k - \frac{c_i(\theta)}{\mu_k} \right) \nabla c_i(\theta), \quad (12.14)$$

and the Hessian is

$$\nabla^2 \mathfrak{L}_A(\theta, \lambda^k; \mu_k) = \nabla^2 f(\theta) + \sum_{i \in \mathfrak{I} | c_i(\theta) \leq \mu_k \lambda_i^k} \left[ \frac{1}{\mu_k} \nabla^2 c_i^2(\theta) - \left( \lambda_i^k - \frac{c_i(\theta)}{\mu_k} \right) \nabla^2 c_i(\theta) \right]. \quad (12.15)$$

The Augmented Lagrangian algorithm can accept any set of three arbitrary constraint functions  $c(\theta)$ ,  $\nabla c(\theta)$ , and  $\nabla^2 c(\theta)$ . When given the current parameter values  $c(\theta)$  returns a vector of constraint values whereby each position corresponds to one of the model parameters. The constraint is defined as  $c_i \geq 0$ . The function  $\nabla c(\theta)$  returns the matrix of



constraint gradients and  $\nabla^2 c(\theta)$  is the constraint Hessian function which should return the 3D matrix of constraint Hessians.

A more specific set of constraints accepted by the Method of Multipliers are bound constraints. These are defined by the function

$$l \leq \theta \leq u, \quad (12.16)$$

where  $l$  and  $u$  are the vectors of lower and upper bounds respectively and  $\theta$  is the parameter vector. For example for model-free model *m4* to place lower and upper bounds on the order parameter and lower bounds on the correlation time and chemical exchange parameters, the vectors are

$$\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \leq \begin{pmatrix} S^2 \\ \tau_e \\ R_{ex} \end{pmatrix} \leq \begin{pmatrix} 1 \\ \infty \\ \infty \end{pmatrix}. \quad (12.17)$$

The default setting in the program *relax* is to use linear constraints which are defined as

$$A \cdot \theta \geq b, \quad (12.18)$$

where  $A$  is an  $m \times n$  matrix where the rows are the transposed vectors  $a_i$  of length  $n$ ; the elements of  $a_i$  are the coefficients of the model parameters;  $\theta$  is the vector of model parameters of dimension  $n$ ;  $b$  is the vector of scalars of dimension  $m$ ;  $m$  is the number of constraints; and  $n$  is the number of model parameters.

In rearranging (12.18) the linear constraint function  $c(\theta)$  returns the vector  $A \cdot \theta - b$ . Because of the linearity of the constraints the gradient and Hessian are greatly simplified. The gradient  $\nabla c(\theta)$  is simply the matrix  $A$  and the Hessian  $\nabla^2 c(\theta)$  is zero.

### 12.5.2 Logarithmic barrier constraint algorithm

Another constraint method is that of the logarithmic barrier algorithm. As in the Method of Multipliers this method is iterative. The function being minimised is replaced with

$$\Phi(\theta) = \begin{cases} \epsilon \sum_{i=1}^m -\log(b_i - A_i^T \theta) & \text{if } A \cdot \theta < b, \\ +\infty & \text{otherwise.} \end{cases} \quad (12.19)$$

The value of  $\epsilon$  is increased with each iteration, increase the logarithmic penalty. An advantage of this method over the Method of Multipliers is that gradients are not required.

## 12.6 Diagonal scaling

Model scaling can have a significant effect on the optimisation algorithm – a poorly scaled model can cause certain techniques to fail. When two parameters of the model lie on very different numeric scales the model is said to be poorly scaled. For example in model-free analysis the order of magnitude of the order parameters is one whereas for the internal



correlation times the order of magnitude is between  $1e^{-12}$  to  $1e^{-8}$ . Most effected are the trust region algorithms – the multidimensional sphere of trust will either be completely ineffective against the correlation time parameters or severely restrict optimisation in the order parameter dimensions. Again in model-free analyses the significant scaling disparity can even cause failure of optimisation due to amplified effects of machine precision. Therefore the model parameters need to be scaled.

This can be done by supplying the optimisation algorithm with the scaled rather than unscaled parameters. When the chi-squared function, gradient, and Hessian are called the vector is then premultiplied with a diagonal matrix in which the diagonal elements are the scaling factors.



## Chapter 13

# Optimisation of relaxation data – values, gradients, and Hessians

### 13.1 Introduction to the mathematics behind the optimisation of relaxation data

A word of warning before reading this chapter, the topics covered here are quite advanced and are not necessary for understanding how to either use relax or to implement any of the data analysis techniques present within relax. The material of this chapter is intended as an in-depth explanation of the mathematics involved in the optimisation of the parameters of the model-free models, or any theory involving relaxation data. As such it contains the chi-squared equation, relaxation equations, spectral density functions, and diffusion tensor equations as well as their gradients (the vector of first partial derivatives) and Hessians (the matrix of second partial derivatives). All these equations are used in the optimisation of model-free models  $m0$  to  $m9$ ; models  $tm0$  to  $tm9$ ; the ellipsoidal, spheroidal, and spherical diffusion tensors; and the combination of the diffusion tensor and the model-free models. They also apply to all other theories involving the base  $R_1$ ,  $R_2$ , and steady-state NOE relaxation rates.

### 13.2 The four parameter combinations

In model-free analysis four different combinations of parameters can be optimised, each of which requires a different approach to the construction of the chi-squared value, gradient, and Hessian. These categories depend on whether the model-free parameter set  $\mathfrak{F}$ , the diffusion tensor parameter set  $\mathfrak{D}$ , or both sets are simultaneously optimised. The addition of the local  $\tau_m$  parameter to the model-free set  $\mathfrak{F}$  creates a fourth parameter combination.

#### 13.2.1 Optimisation of the model-free models

This is the simplest category as it involves solely the optimisation of the model-free parameters of an individual residue while the diffusion tensor parameters are held constant.

The model-free parameters belong to the set  $\mathfrak{F}_i$  of the residue  $i$ . The models include  $m0$  to  $m9$  and the dimensionality is low with

$$\dim \mathfrak{F}_i = k \leq 5 \quad (13.1)$$

for the most complex model  $m8 = \{S^2, \tau_f, S_f^2, \tau_s, R_{ex}\}$ . The relaxation data of a single residue is used to build the chi-squared value, gradient, and Hessian.

### 13.2.2 Optimisation of the local $\tau_m$ models

The addition of the local  $\tau_m$  parameter to the set  $\mathfrak{F}_i$  creates a new set of models which will be labelled  $\mathfrak{T}_i$ . These include models  $tm0$  to  $tm9$ . The local  $\tau_m$  parameter is the single member of the set  $\mathfrak{D}_i$  and in set notation

$$\mathfrak{T}_i = \mathfrak{D}_i \cup \mathfrak{F}_i. \quad (13.2)$$

Although the Brownian rotational diffusion parameter local  $\tau_m$  is optimised, this category is residue specific. As such the complexity of the optimisation is lower than the next two categories. It is slightly greater than the optimisation of the set  $\mathfrak{F}_i$  as

$$\dim \mathfrak{T}_i = 1 + k \leq 6, \quad (13.3)$$

where  $k$  is the number of model-free parameters.

### 13.2.3 Optimisation of the diffusion tensor parameters

The parameters of the Brownian rotational diffusion tensor belong to the set  $\mathfrak{D}$ . This set is the union of the geometric parameters  $\mathfrak{G} = \{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r\}$  and the orientational parameters  $\mathfrak{O}$ ,

$$\mathfrak{D} = \mathfrak{G} \cup \mathfrak{O}. \quad (13.4)$$

When diffusion is spherical solely the geometric parameter  $\mathfrak{D}_{iso}$  is optimised. When the molecule diffuses as a spheroid the geometric parameters  $\mathfrak{D}_{iso}$  and  $\mathfrak{D}_a$  and the orientational parameters  $\theta$  (the polar angle) and  $\phi$  (the azimuthal angle) are optimised. If the molecule diffuses as an ellipsoid the geometric parameters  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_a$ , and  $\mathfrak{D}_r$  are optimised together with the Euler angles  $\alpha$ ,  $\beta$ , and  $\gamma$ .

This category is defined as the optimisation of solely the parameters of  $\mathfrak{D}$ . The model-free parameters of  $\mathfrak{F}$  are held constant. As all selected residues of the macromolecule are involved in the optimisation, this category is global and can be more complex than the optimisation of  $\mathfrak{F}_i$  or  $\mathfrak{T}_i$ . The dimensionality of the problem nevertheless low with

$$\dim \mathfrak{D} = 1, \quad \dim \mathfrak{D} = 4, \quad \dim \mathfrak{D} = 6, \quad (13.5)$$

for the diffusion as a sphere, spheroid, and ellipsoid respectively.

### 13.2.4 Optimisation of the global model

The global model is defined as

$$\mathfrak{S} = \mathfrak{D} \cup \left( \bigcup_{i=1}^l \mathfrak{F}_i \right), \quad (13.6)$$

where  $i$  is the residue index and  $l$  is the total number of residues used in the analysis. This is the most complex of the four categories as both diffusion tensor parameters and model-free parameters of all selected residues are optimised simultaneously. The dimensionality of the model  $\mathfrak{S}$  is much greater than the other categories and is equal to

$$\dim \mathfrak{S} = \dim \mathfrak{D} + \sum_{i=1}^l k_i \leq 6 + 5l, \quad (13.7)$$

where  $k_i$  is the number of model-free parameters for the residue  $i$  and is equal to  $\dim \mathfrak{F}_i$ , the number six corresponds to the maximum dimensionality of  $\mathfrak{D}$ , and the number five corresponds to the maximum dimensionality of  $\mathfrak{F}_i$ .

## 13.3 Construction of the values, gradients, and Hessians

### 13.3.1 The sum of chi-squared values

For the single residue models of  $\mathfrak{F}_i$  and  $\mathfrak{T}_i$  the chi-squared value  $\chi_i^2$  which is optimised is simply Equation (13.13) on page 233 in which the relaxation data is that of residue  $i$ . However for the global models  $\mathfrak{D}$  and  $\mathfrak{S}$  in which all selected residues are involved the optimised chi-squared value is the sum of those for each residue,

$$\chi^2 = \sum_{i=1}^l \chi_i^2, \quad (13.8)$$

where  $i$  is the residue index and  $l$  is the total number of residues used in the analysis. This is equivalent to Equation (13.13) when the index  $i$  ranges over the relaxation data of all selected residues.

### 13.3.2 Construction of the gradient

The construction of the gradient is significantly different for the models  $\mathfrak{F}_i$ ,  $\mathfrak{T}_i$ ,  $\mathfrak{D}$ , and  $\mathfrak{S}$ . In Figure 13.1 the construction of the chi-squared gradient  $\nabla \chi^2$  for the global model  $\mathfrak{S}$  is demonstrated. In this case

$$\nabla \chi^2 = \sum_{i=1}^l \nabla \chi_i^2, \quad (13.9)$$

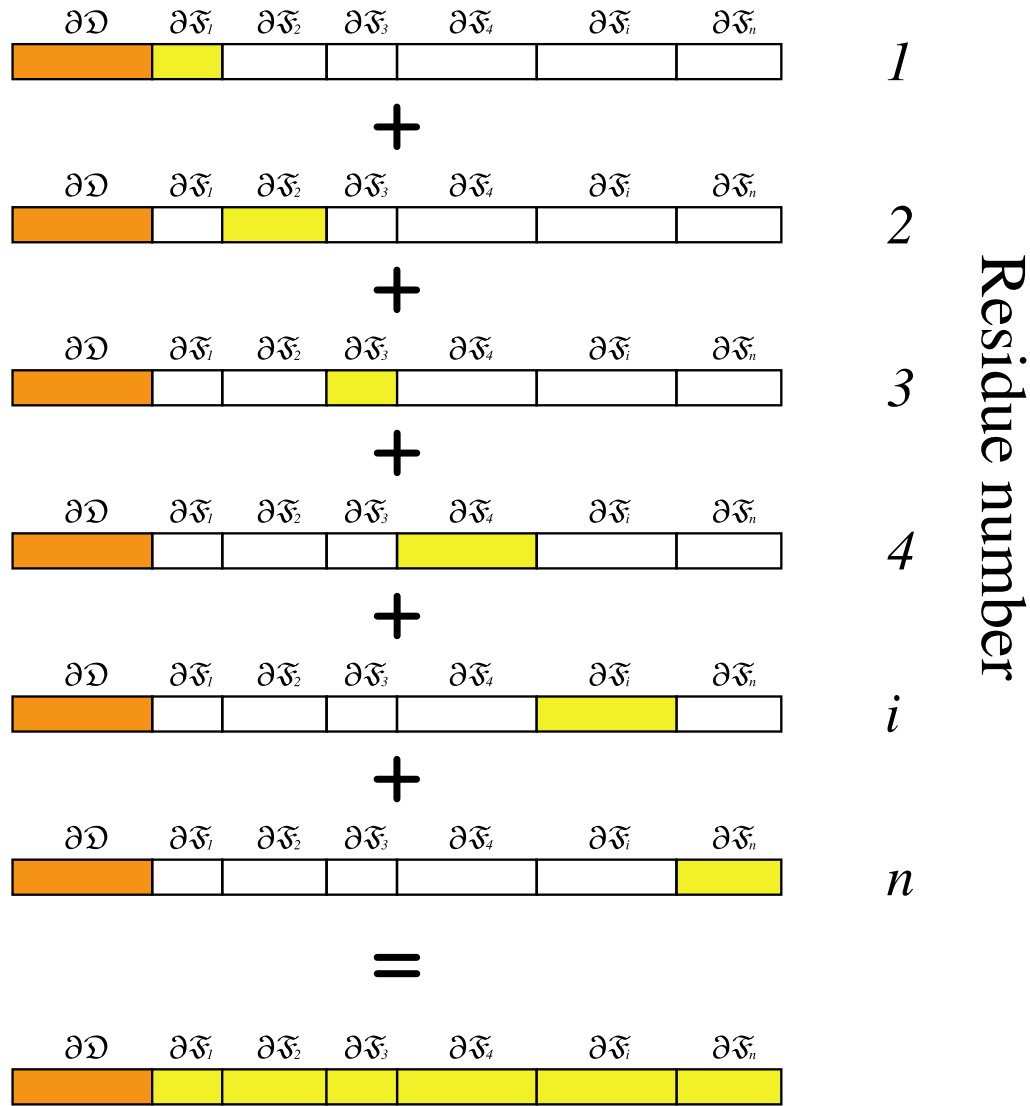


Figure 13.1: The construction of the model-free gradient  $\nabla\chi^2$  for the global model  $\mathfrak{S}$ . For each residue  $i$  a different vector  $\nabla\chi_i^2$  is constructed. The first element of the vector represented by the symbol  $\partial\mathfrak{D}$  (the orange block) is the sub-vector of chi-squared partial derivatives with respect to each of the diffusion tensor parameters  $\mathfrak{D}_j$ . The rest of the elements, grouped into blocks for each residue denoted by the symbol  $\partial\mathfrak{S}_i$ , are the sub-vectors of chi-squared partial derivatives with respect to each of the model-free parameters  $\mathfrak{S}_i^j$ . For the residue dependent vector  $\nabla\chi_i^2$  the partial derivatives with respect to the model-free parameters of  $\mathfrak{S}_j$  where  $i \neq j$  are zero. These blocks are left uncoloured. The complete gradient of  $\mathfrak{S}$  is the sum of the vectors  $\nabla\chi_i^2$ .

where  $\nabla\chi_i^2$  is the vector of partial derivatives of the chi-squared equation  $\chi_i^2$  for the residue  $i$ . The length of this vector is

$$\|\nabla\chi_i^2\| = \dim \mathfrak{S}, \quad (13.10)$$

with each position of the vector  $j$  equal to  $\frac{\partial\chi_i^2}{\partial\theta_j}$  where each  $\theta_j$  is a parameter of the model.

The construction of the gradient  $\nabla\chi^2$  for the model  $\mathfrak{D}$  is simply a subset of that of  $\mathfrak{S}$ . This is demonstrated in Figure 13.1 by simply taking the component of the gradient  $\nabla\chi_i^2$  denoted by the symbol  $\partial\mathfrak{D}$  (the orange blocks) and summing these for all residues. This sum is given by (13.9) and

$$\|\nabla\chi_i^2\| = \dim \mathfrak{D}. \quad (13.11)$$

For the parameter set  $\mathfrak{T}_i$ , which consists of the local  $\tau_m$  parameter and the model-free parameters of a single residue, the gradient  $\nabla\chi_i^2$  for the residue  $i$  is simply the combination of the single orange block and single yellow block of the index  $i$  (Figure 13.1).

The model-free parameter set  $\mathfrak{F}_i$  is even simpler. In Figure 13.1 the gradient  $\nabla\chi_i^2$  is simply the vector denoted by the single yellow block for the residue  $i$ .

### 13.3.3 Construction of the Hessian

The construction of the Hessian for the models  $\mathfrak{F}_i$ ,  $\mathfrak{T}_i$ ,  $\mathfrak{D}$ , and  $\mathfrak{S}$  is very similar to the procedure used for the gradient. The chi-squared Hessian for the global models  $\mathfrak{D}$  and  $\mathfrak{S}$  is

$$\nabla^2\chi^2 = \sum_{i=1}^l \nabla^2\chi_i^2. \quad (13.12)$$

Figure 13.2 demonstrates the construction of the full Hessian for the model  $\mathfrak{S}$ . The Hessian for the model  $\mathfrak{D}$  is the sum of all the red blocks. The Hessian for the model  $\mathfrak{T}_i$  is the combination of the single red block for residue  $i$ , the two orange blocks representing the sub-matrices of chi-squared second partial derivatives with respect to the diffusion parameter  $\mathfrak{D}_j$  and the model-free parameter  $\mathfrak{F}_i^k$ , and the single yellow block for that residue. The Hessian for the model-free model  $\mathfrak{F}_i$  is simply the sub-matrix for the residue  $i$  coloured yellow.

## 13.4 The value, gradient, and Hessian dependency chain

The dependency chain which was outlined in the model-free chapter – that the chi-squared function is dependent on the transformed relaxation equations which are dependent on the relaxation equations which themselves are dependent on the spectral density functions – combine with the values, gradients, and Hessians to create a complex web of dependencies. The relationship between all the values, gradients, and Hessians are outlined in Figure 13.3.

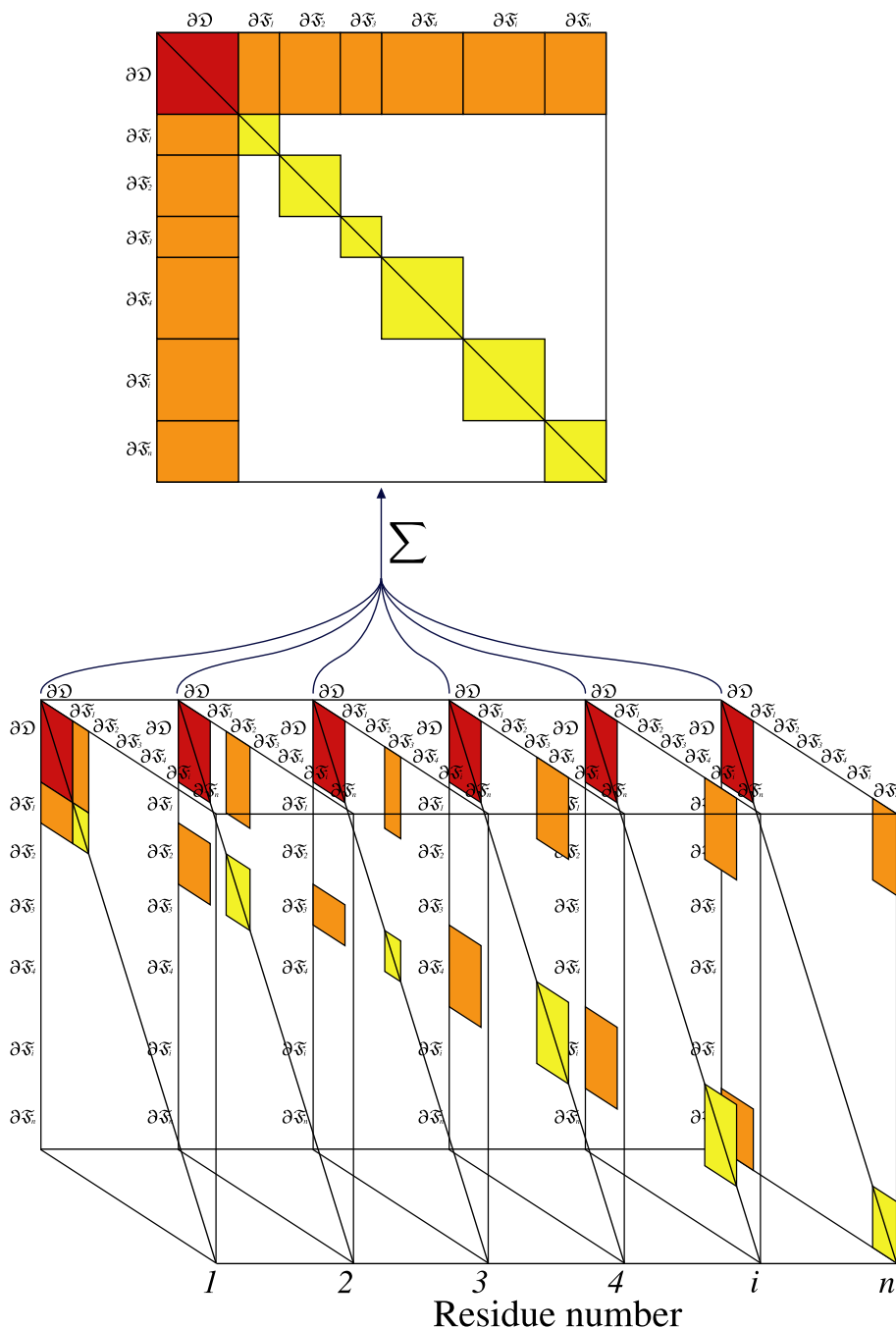


Figure 13.2: The model-free Hessian kite – a demonstration of the construction of the model-free Hessian  $\nabla^2\chi^2$  for the global model  $\mathfrak{S}$ . For each residue  $i$  a different matrix  $\nabla^2\chi_i^2$  is constructed. The first element of the matrix represented by the two symbols  $\partial\mathfrak{D}$  (the red block) is the sub-matrix of chi-squared second partial derivatives with respect to the diffusion tensor parameters  $\mathfrak{D}_j$  and  $\mathfrak{D}_k$ . The orange blocks are the sub-matrices of chi-squared second partial derivatives with respect to the diffusion parameter  $\mathfrak{D}_j$  and the model-free parameter  $\mathfrak{F}_i^k$ . The yellow blocks are the sub-matrices of chi-squared second partial derivatives with respect to the model-free parameters  $\mathfrak{F}_i^j$  and  $\mathfrak{F}_i^k$ . For the residue dependent matrix  $\nabla^2\chi_i^2$  the second partial derivatives with respect to the model-free parameters  $\mathfrak{F}_l^j$  and  $\mathfrak{F}_l^k$  where  $i \neq l$  are zero. In addition, the second partial derivatives with respect to the model-free parameters  $\mathfrak{F}_i^j$  and  $\mathfrak{F}_l^k$  where  $i \neq l$  are also zero. These blocks of sub-matrices are left uncoloured. The complete Hessian of  $\mathfrak{S}$  is the sum of the matrices  $\nabla^2\chi_i^2$ .



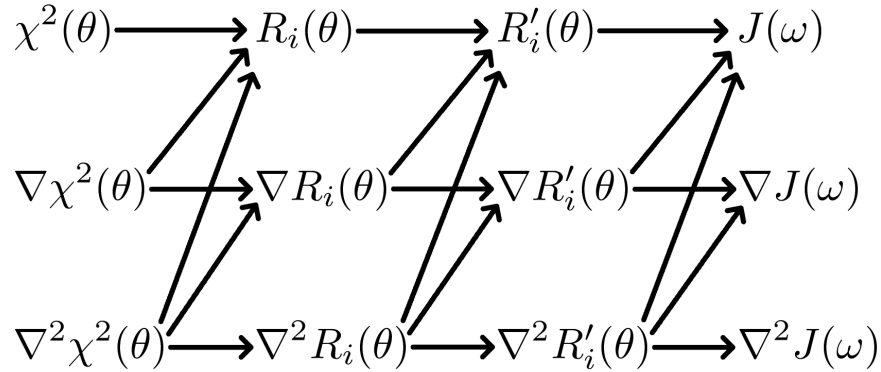


Figure 13.3: Dependencies between the  $\chi^2$ , transformed relaxation, relaxation, and spectral density equations, gradients, and Hessians.

## 13.5 The $\chi^2$ value, gradient, and Hessian

### 13.5.1 The $\chi^2$ value

The  $\chi^2$  value is defined as

$$\chi^2(\theta) = \sum_{i=1}^n \frac{(R_i - R_i(\theta))^2}{\sigma_i^2}, \quad (13.13)$$

where the summation index  $i$  ranges over all the relaxation data of all residues used in the analysis.

### 13.5.2 The $\chi^2$ gradient

The  $\chi^2$  gradient in vector notation is

$$\nabla \chi^2(\theta) = 2 \sum_{i=1}^n \frac{(R_i - R_i(\theta))^2}{\sigma_i^2} \nabla R_i(\theta). \quad (13.14)$$

### 13.5.3 The $\chi^2$ Hessian

The  $\chi^2$  Hessian in vector notation is

$$\nabla^2 \chi^2(\theta) = 2 \sum_{i=1}^n \frac{1}{\sigma_i^2} (\nabla R_i(\theta) \cdot \nabla R_i(\theta)^T - (R_i - R_i(\theta)) \nabla^2 R_i(\theta)). \quad (13.15)$$

## 13.6 The $R_i(\theta)$ values, gradients, and Hessians

### 13.6.1 The $R_i(\theta)$ values

The  $R_i(\theta)$  values are given by

$$R_1(\theta) = R'_1(\theta), \quad (13.16a)$$

$$R_2(\theta) = R'_2(\theta), \quad (13.16b)$$

$$\text{NOE}(\theta) = 1 + \frac{\gamma_H}{\gamma_X} \frac{\sigma_{\text{NOE}}(\theta)}{R_1(\theta)}. \quad (13.16c)$$

### 13.6.2 The $R_i(\theta)$ gradients

The  $R_i(\theta)$  gradients in vector notation are

$$\nabla R_1(\theta) = \nabla R'_1(\theta), \quad (13.17a)$$

$$\nabla R_2(\theta) = \nabla R'_2(\theta), \quad (13.17b)$$

$$\nabla \text{NOE}(\theta) = \frac{\gamma_H}{\gamma_X} \frac{1}{R_1(\theta)^2} \left( R_1(\theta) \nabla \sigma_{\text{NOE}}(\theta) - \sigma_{\text{NOE}}(\theta) \nabla R_1(\theta) \right). \quad (13.17c)$$

### 13.6.3 The $R_i(\theta)$ Hessians

The  $R_i(\theta)$  Hessians in vector notation are

$$\nabla^2 R_1(\theta) = \nabla^2 R'_1(\theta), \quad (13.18a)$$

$$\nabla^2 R_2(\theta) = \nabla^2 R'_2(\theta), \quad (13.18b)$$

$$\begin{aligned} \nabla^2 \text{NOE}(\theta) = \frac{\gamma_H}{\gamma_X} \frac{1}{R_1(\theta)^3} & \left[ \sigma_{\text{NOE}}(\theta) \left( 2 \nabla R_1(\theta) \cdot \nabla R_1(\theta)^T - R_1(\theta) \nabla^2 R_1(\theta) \right) \right. \\ & \left. - R_1(\theta) \left( \nabla \sigma_{\text{NOE}}(\theta) \cdot \nabla R_1(\theta)^T - R_1(\theta) \nabla^2 \sigma_{\text{NOE}}(\theta) \right) \right]. \end{aligned} \quad (13.18c)$$

## 13.7 $R'_i(\theta)$ values, gradients, and Hessians

The partial and second partial derivatives of the relaxation equations of the set  $R'(\theta)$  are different for each parameter of the vector  $\theta$ . The vector representation of the gradient  $\nabla R'_i(\theta)$  and the matrix representation of the Hessian  $\nabla^2 R'_i(\theta)$  can be reconstructed from the individual elements presented in the next section.

### 13.7.1 Components of the $R'_i(\theta)$ equations

To simplify the calculations of the gradients and Hessians the  $R'_i(\theta)$  equations have been broken down into a number of components. These include the dipolar and CSA constants as well as the dipolar and CSA spectral density terms for each of the three transformed relaxation data types  $\{R_1, R_2, \sigma_{\text{NOE}}\}$ . The segregation of these components simplifies the maths as many partial derivatives of the components are zero.

#### Dipolar constant

The dipolar constant is defined as

$$d = \frac{1}{4} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^6 \rangle}. \quad (13.19)$$

This component of the relaxation equations is independent of the parameter of the spectral density function  $\theta_j$ , the chemical exchange parameter  $\rho_{ex}$ , and the CSA parameter  $\Delta\sigma$ . Therefore the partial and second partial derivatives with respect to these parameters is zero. Only the derivative with respect to the bond length  $r$  is non-zero being

$$d' \equiv \frac{dd}{dr} = -\frac{3}{2} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^7 \rangle}. \quad (13.20)$$

The second derivative with respect to the bond length is

$$d'' \equiv \frac{d^2 d}{dr^2} = \frac{21}{2} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^8 \rangle}. \quad (13.21)$$

#### CSA constant

The CSA constant is defined as

$$c = \frac{(\omega_X \cdot \Delta\sigma)^2}{3}. \quad (13.22)$$

The partial derivative of this component with respect to all parameters but the CSA parameter  $\Delta\sigma$  is zero. This derivative is

$$c' \equiv \frac{dc}{d\Delta\sigma} = \frac{2\omega_X^2 \cdot \Delta\sigma}{3}. \quad (13.23)$$

The CSA constant second derivative with respect to  $\Delta\sigma$  is

$$c'' \equiv \frac{d^2 c}{d\Delta\sigma^2} = \frac{2\omega_X^2}{3}. \quad (13.24)$$

**$R_{ex}$  constant**

The  $R_{ex}$  constant is defined as

$$R_{ex} = \rho_{ex}(2\pi\omega_H)^2. \quad (13.25)$$

The partial derivative of this component with respect to all parameters but the chemical exchange parameter  $\rho_{ex}$  is zero. This derivative is

$$R'_{ex} \equiv \frac{dR_{ex}}{d\rho_{ex}} = (2\pi\omega_H)^2. \quad (13.26)$$

The  $R_{ex}$  constant second derivative with respect to  $\rho_{ex}$  is

$$R''_{ex} \equiv \frac{d^2R_{ex}}{d\rho_{ex}^2} = 0. \quad (13.27)$$

**Spectral density terms of the  $R_1$  dipolar component**

For the dipolar component of the  $R_1$  equation (7.2a) on page 84 the spectral density terms are

$$J_d^{R_1} = J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H + \omega_X). \quad (13.28)$$

The partial derivative of these terms with respect to the spectral density function parameter  $\theta_j$  is

$$J_d^{R_1'} \equiv \frac{\partial J_d^{R_1}}{\partial \theta_j} = \frac{\partial J(\omega_H - \omega_X)}{\partial \theta_j} + 3\frac{\partial J(\omega_X)}{\partial \theta_j} + 6\frac{\partial J(\omega_H + \omega_X)}{\partial \theta_j}. \quad (13.29)$$

The second partial derivative with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$  is

$$J_d^{R_1''} \equiv \frac{\partial^2 J_d^{R_1}}{\partial \theta_j \cdot \partial \theta_k} = \frac{\partial^2 J(\omega_H - \omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 3\frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 6\frac{\partial^2 J(\omega_H + \omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (13.30)$$

**Spectral density terms of the  $R_1$  CSA component**

For the CSA component of the  $R_1$  equation (7.2a) on page 84 the spectral density terms are

$$J_c^{R_1} = J(\omega_X). \quad (13.31)$$

The partial derivative of these terms with respect to the spectral density function parameter  $\theta_j$  is

$$J_c^{R_1'} \equiv \frac{\partial J_c^{R_1}}{\partial \theta_j} = \frac{\partial J(\omega_X)}{\partial \theta_j}. \quad (13.32)$$

The second partial derivative with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$  is

$$J_c^{R_1''} \equiv \frac{\partial^2 J_c^{R_1}}{\partial \theta_j \cdot \partial \theta_k} = \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (13.33)$$

**Spectral density terms of the  $R_2$  dipolar component**

For the dipolar component of the  $R_2$  equation (7.2b) on page 84 the spectral density terms are

$$J_d^{R_2} = 4J(0) + J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H) + 6J(\omega_H + \omega_X). \quad (13.34)$$

The partial derivative of these terms with respect to the spectral density function parameter  $\theta_j$  is

$$J_d^{R_2'} \equiv \frac{\partial J_d^{R_2}}{\partial \theta_j} = 4 \frac{\partial J(0)}{\partial \theta_j} + \frac{\partial J(\omega_H - \omega_X)}{\partial \theta_j} + 3 \frac{\partial J(\omega_X)}{\partial \theta_j} + 6 \frac{\partial J(\omega_H)}{\partial \theta_j} + 6 \frac{\partial J(\omega_H + \omega_X)}{\partial \theta_j}. \quad (13.35)$$

The second partial derivative with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$  is

$$J_d^{R_2''} \equiv \frac{\partial^2 J_d^{R_2}}{\partial \theta_j \cdot \partial \theta_k} = 4 \frac{\partial^2 J(0)}{\partial \theta_j \cdot \partial \theta_k} + \frac{\partial^2 J(\omega_H - \omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 3 \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 6 \frac{\partial^2 J(\omega_H)}{\partial \theta_j \cdot \partial \theta_k} + 6 \frac{\partial^2 J(\omega_H + \omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (13.36)$$

**Spectral density terms of the  $R_2$  CSA component**

For the CSA component of the  $R_2$  equation (7.2b) on page 84 the spectral density terms are

$$J_c^{R_2} = 4J(0) + 3J(\omega_X). \quad (13.37)$$

The partial derivative of these terms with respect to the spectral density function parameter  $\theta_j$  is

$$J_c^{R_2'} \equiv \frac{\partial J_c^{R_2}}{\partial \theta_j} = 4 \frac{\partial J(0)}{\partial \theta_j} + 3 \frac{\partial J(\omega_X)}{\partial \theta_j}. \quad (13.38)$$

The second partial derivative with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$  is

$$J_c^{R_2''} \equiv \frac{\partial^2 J_c^{R_2}}{\partial \theta_j \cdot \partial \theta_k} = 4 \frac{\partial^2 J(0)}{\partial \theta_j \cdot \partial \theta_k} + 3 \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (13.39)$$

**Spectral density terms of the  $\sigma_{\text{NOE}}$  dipolar component**

For the dipolar component of the  $\sigma_{\text{NOE}}$  equation (7.2c) on page 84 the spectral density terms are

$$J_d^{\sigma_{\text{NOE}}} = 6J(\omega_H + \omega_X) - J(\omega_H - \omega_X). \quad (13.40)$$

The partial derivative of these terms with respect to the spectral density function parameter  $\theta_j$  is

$$J_d^{\sigma_{\text{NOE}'}} \equiv \frac{\partial J_d^{\sigma_{\text{NOE}}}}{\partial \theta_j} = 6 \frac{\partial J(\omega_H + \omega_X)}{\partial \theta_j} - \frac{\partial J(\omega_H - \omega_X)}{\partial \theta_j}. \quad (13.41)$$

The second partial derivative with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$  is

$$J_d^{\sigma_{\text{NOE}}} \equiv \frac{\partial^2 J_d^{\sigma_{\text{NOE}}}}{\partial \theta_j \cdot \partial \theta_k} = 6 \frac{\partial^2 J(\omega_H + \omega_X)}{\partial \theta_j \cdot \partial \theta_k} - \frac{\partial^2 J(\omega_H - \omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (13.42)$$

### 13.7.2 $R'_i(\theta)$ values

Using the components of the relaxation equations defined above the three relaxation equations can be re-expressed as

$$R_1(\theta) = dJ_d^{R_1} + cJ_c^{R_1}, \quad (13.43a)$$

$$R_2(\theta) = \frac{d}{2}J_d^{R_2} + \frac{c}{6}J_c^{R_2}, \quad (13.43b)$$

$$\sigma_{\text{NOE}}(\theta) = dJ_d^{\sigma_{\text{NOE}}}. \quad (13.43c)$$

### 13.7.3 $R'_i(\theta)$ gradients

A different partial derivative exists for the spectral density function parameter  $\theta_j$ , the chemical exchange parameter  $\rho_{ex}$ , CSA parameter  $\Delta\sigma$ , and bond length parameter  $r$ . In model-free analysis the spectral density parameters include both the parameters of the diffusion tensor and the parameters of the various model-free models.

#### $\theta_j$ partial derivative

The partial derivatives of the relaxation equations with respect to the spectral density function parameter  $\theta_j$  are

$$\frac{\partial R_1(\theta)}{\partial \theta_j} = dJ_d^{R_1'} + cJ_c^{R_1'}, \quad (13.44a)$$

$$\frac{\partial R_2(\theta)}{\partial \theta_j} = \frac{d}{2}J_d^{R_2'} + \frac{c}{6}J_c^{R_2'}, \quad (13.44b)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial \theta_j} = dJ_d^{\sigma_{\text{NOE}}'}. \quad (13.44c)$$

#### $\rho_{ex}$ partial derivative

The partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $\rho_{ex}$  are

$$\frac{\partial R_1(\theta)}{\partial \rho_{ex}} = 0, \quad (13.45a)$$

$$\frac{\partial R_2(\theta)}{\partial \rho_{ex}} = (2\pi\omega_H)^2, \quad (13.45b)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial \rho_{ex}} = 0. \quad (13.45c)$$

**$\Delta\sigma$  partial derivative**

The partial derivatives of the relaxation equations with respect to the CSA parameter  $\Delta\sigma$  are

$$\frac{\partial R_1(\theta)}{\partial \Delta\sigma} = c' J_c^{R_1}, \quad (13.46a)$$

$$\frac{\partial R_2(\theta)}{\partial \Delta\sigma} = \frac{c'}{6} J_c^{R_2}, \quad (13.46b)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial \Delta\sigma} = 0. \quad (13.46c)$$

 **$r$  partial derivative**

The partial derivatives of the relaxation equations with respect to the bond length parameter  $r$  are

$$\frac{\partial R_1(\theta)}{\partial r} = d' J_d^{R_1}, \quad (13.47a)$$

$$\frac{\partial R_2(\theta)}{\partial r} = \frac{d'}{2} J_d^{R_2}, \quad (13.47b)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial r} = d' J_d^{\sigma_{\text{NOE}}}. \quad (13.47c)$$

**13.7.4  $R'_i(\theta)$  Hessians**

Again different second partial derivatives with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$ , the chemical exchange parameter  $\rho_{ex}$ , CSA parameter  $\Delta\sigma$ , and bond length parameter  $r$ . These second partial derivatives are the components of the  $R'_i(\theta)$  Hessian matrices.

 **$\theta_j - \theta_k$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the spectral density function parameters  $\theta_j$  and  $\theta_k$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial \theta_k} = d J_d^{R_1''} + c J_c^{R_1''}, \quad (13.48a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial \theta_k} = \frac{d}{2} J_d^{R_2''} + \frac{c}{6} J_c^{R_2''}, \quad (13.48b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial \theta_k} = d J_d^{\sigma_{\text{NOE}}''}. \quad (13.48c)$$

**$\theta_j - \rho_{ex}$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the spectral density function parameter  $\theta_j$  and the chemical exchange parameter  $\rho_{ex}$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial \rho_{ex}} = 0, \quad (13.49a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial \rho_{ex}} = 0, \quad (13.49b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial \rho_{ex}} = 0. \quad (13.49c)$$

 **$\theta_j - \Delta\sigma$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the spectral density function parameter  $\theta_j$  and the CSA parameter  $\Delta\sigma$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial \Delta\sigma} = c' J_c^{\text{R}_1'}, \quad (13.50a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial \Delta\sigma} = \frac{c'}{6} J_c^{\text{R}_2'}, \quad (13.50b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial \Delta\sigma} = 0. \quad (13.50c)$$

 **$\theta_j - r$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the spectral density function parameter  $\theta_j$  and the bond length parameter  $r$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial r} = d' J_d^{\text{R}_1'}, \quad (13.51a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial r} = \frac{d'}{2} J_d^{\text{R}_2'}, \quad (13.51b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial r} = d' J_d^{\sigma_{\text{NOE}}'}. \quad (13.51c)$$

 **$\rho_{ex} - \rho_{ex}$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $\rho_{ex}$  twice are

$$\frac{\partial^2 R_1(\theta)}{\partial \rho_{ex}^2} = 0, \quad (13.52a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \rho_{ex}^2} = 0, \quad (13.52b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \rho_{ex}^2} = 0. \quad (13.52c)$$



**$\rho_{ex} - \Delta\sigma$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $\rho_{ex}$  and the CSA parameter  $\Delta\sigma$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \rho_{ex} \cdot \partial \Delta\sigma} = 0, \quad (13.53a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \rho_{ex} \cdot \partial \Delta\sigma} = 0, \quad (13.53b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \rho_{ex} \cdot \partial \Delta\sigma} = 0. \quad (13.53c)$$

 **$\rho_{ex} - r$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $\rho_{ex}$  and the bond length parameter  $r$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \rho_{ex} \cdot \partial r} = 0, \quad (13.54a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \rho_{ex} \cdot \partial r} = 0, \quad (13.54b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \rho_{ex} \cdot \partial r} = 0. \quad (13.54c)$$

 **$\Delta\sigma - \Delta\sigma$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the CSA parameter  $\Delta\sigma$  twice are

$$\frac{\partial^2 R_1(\theta)}{\partial \Delta\sigma^2} = c'' J_c^{R_1}, \quad (13.55a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \Delta\sigma^2} = \frac{c''}{6} J_c^{R_2}, \quad (13.55b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \Delta\sigma^2} = 0. \quad (13.55c)$$

 **$\Delta\sigma - r$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the CSA parameter  $\Delta\sigma$  and the bond length parameter  $r$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \Delta\sigma \cdot \partial r} = 0, \quad (13.56a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \Delta\sigma \cdot \partial r} = 0, \quad (13.56b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \Delta\sigma \cdot \partial r} = 0. \quad (13.56c)$$

**$r - r$  partial derivative**

The second partial derivatives of the relaxation equations with respect to the bond length parameter  $r$  twice are

$$\frac{\partial^2 R_1(\theta)}{\partial r^2} = d'' J_d^{R_1}, \quad (13.57a)$$

$$\frac{\partial^2 R_2(\theta)}{\partial r^2} = \frac{d''}{2} J_d^{R_2}, \quad (13.57b)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial r^2} = d'' J_d^{\sigma_{\text{NOE}}}. \quad (13.57c)$$

## 13.8 Model-free analysis

### 13.8.1 The model-free equations

In the original model-free analysis of [Lipari and Szabo \(1982a\)](#) the correlation function  $C(\tau)$  of the XH bond vector is approximated by decoupling the internal fluctuations of the bond vector  $C_I(\tau)$  from the correlation function of the overall Brownian rotational diffusion  $C_O(\tau)$  by the equation

$$C(\tau) = C_O(\tau) \cdot C_I(\tau). \quad (13.58)$$

The overall correlation functions of the diffusion of a sphere, spheroid, and ellipsoid are presented respectively in section 13.9.1 on page 255, section 13.10.1 on page 268, and section 13.11.1 on page 272. These three different equations can be combined into one generic correlation function which is independent of the type of diffusion. This generic correlation function is

$$C_O(\tau) = \frac{1}{5} \sum_{i=-k}^k c_i \cdot e^{-\tau/\tau_i}, \quad (13.59)$$

where  $c_i$  are the weights and  $\tau_i$  are correlation times of the exponential terms. In the original model-free analysis of [Lipari and Szabo \(1982a,b\)](#) the internal motions are modelled by the correlation function

$$C_I(\tau) = S^2 + (1 - S^2)e^{-\tau/\tau_e}, \quad (13.60)$$

where  $S^2$  is the generalised Lipari and Szabo order parameter which is related to the amplitude of the motion and  $\tau_e$  is the effective correlation time which is an indicator of the timescale of the motion, albeit being dependent on the value of the order parameter. The order parameter ranges from one for complete rigidity to zero for unrestricted motions. Model-free theory was extended by [Clare et al. \(1990\)](#) to include motions on two timescales by the correlation function

$$C_I(\tau) = S^2 + (1 - S_f^2)e^{-\tau/\tau_f} + (S_f^2 - S^2)e^{-\tau/\tau_s}, \quad (13.61)$$

where the faster of the motions is defined by the order parameter  $S_f^2$  and the correlation time  $\tau_f$ , the slower by the parameters  $S_s^2$  and  $\tau_s$ , and the two order parameter are related by the equation  $S^2 = S_f^2 \cdot S_s^2$ .

The relaxation equations of [Abragam \(1961\)](#) are composed of a sum of power spectral density functions  $J(\omega)$  at five frequencies. The spectral density function is related to the correlation function as the two are a Fourier pair. Applying the Fourier transform to the correlation function composed of the generic diffusion equation and the original model-free correlation function results in the equation

$$J(\omega) = \frac{2}{5} \sum_{i=-k}^k c_i \cdot \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2} \right). \quad (13.62)$$

The Fourier transform using the extended model-free correlation function is

$$J(\omega) = \frac{2}{5} \sum_{i=-k}^k c_i \cdot \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i)\tau_f}{(\tau_f + \tau_i)^2 + (\omega\tau_f\tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i)\tau_s}{(\tau_s + \tau_i)^2 + (\omega\tau_s\tau_i)^2} \right). \quad (13.63)$$

### 13.8.2 The original model-free gradient

The model-free gradient of the original spectral density function (13.62) is the vector of partial derivatives of the function with respect to the geometric parameter  $\mathfrak{G}_i$ , the orientational parameter  $\mathfrak{D}_i$ , the order parameter  $S^2$ , and the internal correlation time  $\tau_e$ . The positions in the vector correspond to the model parameters which are being optimised.

#### $\mathfrak{G}_j$ partial derivative

The partial derivative of (13.62) with respect to the geometric parameter  $\mathfrak{G}_j$  is

$$\begin{aligned} \frac{\partial J(\omega)}{\partial \mathfrak{G}_j} = \frac{2}{5} \sum_{i=-k}^k \left( c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \left( S^2 \frac{1 - (\omega\tau_i)^2}{(1 + (\omega\tau_i)^2)^2} + (1 - S^2) \tau_e^2 \frac{(\tau_e + \tau_i)^2 - (\omega\tau_e\tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2)^2} \right) \right. \\ \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2} \right) \right). \quad (13.64) \end{aligned}$$

#### $\mathfrak{D}_j$ partial derivative

The partial derivative of (13.62) with respect to the orientational parameter  $\mathfrak{D}_j$  is

$$\frac{\partial J(\omega)}{\partial \mathfrak{D}_j} = \frac{2}{5} \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2} \right). \quad (13.65)$$

#### $S^2$ partial derivative

The partial derivative of (13.62) with respect to the order parameter  $S^2$  is

$$\frac{\partial J(\omega)}{\partial S^2} = \frac{2}{5} \sum_{i=-k}^k c_i \tau_i \left( \frac{1}{1 + (\omega\tau_i)^2} - \frac{(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2} \right). \quad (13.66)$$

#### $\tau_e$ partial derivative

The partial derivative of (13.62) with respect to the correlation time  $\tau_e$  is

$$\frac{\partial J(\omega)}{\partial \tau_e} = \frac{2}{5} (1 - S^2) \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_e + \tau_i)^2 - (\omega\tau_e\tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2)^2}. \quad (13.67)$$

### 13.8.3 The original model-free Hessian

The model-free Hessian of the original spectral density function (13.62) is the matrix of second partial derivatives. The matrix coordinates correspond to the model parameters which are being optimised.

#### $\mathfrak{G}_j - \mathfrak{G}_k$ partial derivative

The second partial derivative of (13.62) with respect to the geometric parameters  $\mathfrak{G}_j$  and  $\mathfrak{G}_k$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{G}_k} = & \frac{2}{5} \sum_{i=-k}^k \left( -2c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \cdot \frac{\partial \tau_i}{\partial \mathfrak{G}_k} \left( S^2 \omega^2 \tau_i \frac{3 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^3} \right. \right. \\ & \left. \left. + (1 - S^2) \tau_e^2 \frac{(\tau_e + \tau_i)^3 + 3\omega^2 \tau_e^3 \tau_i (\tau_e + \tau_i) - (\omega \tau_e)^4 \tau_i^3}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^3} \right) \right. \\ & \left. + \left( \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \cdot \frac{\partial c_i}{\partial \mathfrak{G}_k} + \frac{\partial \tau_i}{\partial \mathfrak{G}_k} \cdot \frac{\partial c_i}{\partial \mathfrak{G}_j} + c_i \frac{\partial^2 \tau_i}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{G}_k} \right) \left( S^2 \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} \right. \right. \\ & \left. \left. + (1 - S^2) \tau_e^2 \frac{(\tau_e + \tau_i)^2 - (\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^2} \right) \right. \\ & \left. + \left( \frac{\partial^2 c_i}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{G}_k} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2} \right) \right) \right). \quad (13.68) \end{aligned}$$

#### $\mathfrak{G}_j - \mathfrak{D}_k$ partial derivative

The second partial derivative of (13.62) with respect to the geometric parameter  $\mathfrak{G}_j$  and the orientational parameter  $\mathfrak{D}_k$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{D}_k} = & \frac{2}{5} \sum_{i=-k}^k \left( \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \frac{\partial c_i}{\partial \mathfrak{D}_k} \left( S^2 \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} + (1 - S^2) \tau_e^2 \frac{(\tau_e + \tau_i)^2 - (\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^2} \right) \right. \\ & \left. + \frac{\partial^2 c_i}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{D}_k} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2} \right) \right). \quad (13.69) \end{aligned}$$

#### $\mathfrak{G}_j - S^2$ partial derivative

The second partial derivative of (13.62) with respect to the geometric parameter  $\mathfrak{G}_j$  and the order parameter  $S^2$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial S^2} = & \frac{2}{5} \sum_{i=-k}^k \left( c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \left( \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} - \tau_e^2 \frac{(\tau_e + \tau_i)^2 - (\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^2} \right) \right. \\ & \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i \left( \frac{1}{1 + (\omega \tau_i)^2} - \frac{(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2} \right) \right). \quad (13.70) \end{aligned}$$

**$\mathfrak{G}_j - \tau_e$  partial derivative**

The second partial derivative of (13.62) with respect to the geometric parameter  $\mathfrak{G}_j$  and the correlation time  $\tau_e$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \tau_e} = \frac{2}{5}(1 - S^2) \sum_{i=-k}^k \left( 2c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \tau_e \tau_i (\tau_e + \tau_i) \frac{(\tau_e + \tau_i)^2 - 3(\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^3} + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i^2 \frac{(\tau_e + \tau_i)^2 - (\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^2} \right). \quad (13.71)$$

 **$\mathfrak{D}_j - \mathfrak{D}_k$  partial derivative**

The second partial derivative of (13.62) with respect to the orientational parameters  $\mathfrak{D}_j$  and  $\mathfrak{D}_k$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k} = \frac{2}{5} \sum_{i=-k}^k \frac{\partial^2 c_i}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2} \right). \quad (13.72)$$

 **$\mathfrak{D}_j - S^2$  partial derivative**

The second partial derivative of (13.62) with respect to the orientational parameter  $\mathfrak{D}_j$  and the order parameter  $S^2$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial S^2} = \frac{2}{5} \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i \left( \frac{1}{1 + (\omega \tau_i)^2} - \frac{(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2} \right). \quad (13.73)$$

 **$\mathfrak{D}_j - \tau_e$  partial derivative**

The second partial derivative of (13.62) with respect to the orientational parameter  $\mathfrak{D}_j$  and the correlation time  $\tau_e$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial \tau_e} = \frac{2}{5}(1 - S^2) \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i^2 \frac{(\tau_e + \tau_i)^2 - (\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^2}. \quad (13.74)$$

 **$S^2 - S^2$  partial derivative**

The second partial derivative of (13.62) with respect to the order parameter  $S^2$  twice is

$$\frac{\partial^2 J(\omega)}{(\partial S^2)^2} = 0. \quad (13.75)$$

**$S^2 - \tau_e$  partial derivative**

The second partial derivative of (13.62) with respect to the order parameter  $S^2$  and correlation time  $\tau_e$  is

$$\frac{\partial^2 J(\omega)}{\partial S^2 \cdot \partial \tau_e} = -\frac{2}{5} \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_e + \tau_i)^2 - (\omega \tau_e \tau_i)^2}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^2}. \quad (13.76)$$

 **$\tau_e - \tau_e$  partial derivative**

The second partial derivative of (13.62) with respect to the correlation time  $\tau_e$  twice is

$$\frac{\partial^2 J(\omega)}{\partial \tau_e^2} = -\frac{4}{5} (1 - S^2) \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_e + \tau_i)^3 + 3\omega^2 \tau_i^3 \tau_e (\tau_e + \tau_i) - (\omega \tau_i)^4 \tau_e^3}{((\tau_e + \tau_i)^2 + (\omega \tau_e \tau_i)^2)^3} \quad (13.77)$$

### 13.8.4 The extended model-free gradient

The model-free gradient of the extended spectral density function (13.63) is the vector of partial derivatives of the function with respect to the geometric parameter  $\mathfrak{G}_i$ , the orientational parameter  $\mathfrak{D}_i$ , the order parameters  $S^2$  and  $S_f^2$ , and the internal correlation times  $\tau_f$  and  $\tau_s$ . The positions in the vector correspond to the model parameters which are being optimised.

#### $\mathfrak{G}_j$ partial derivative

The partial derivative of (13.63) with respect to the geometric parameter  $\mathfrak{G}_j$  is

$$\begin{aligned} \frac{\partial J(\omega)}{\partial \mathfrak{G}_j} = \frac{2}{5} \sum_{i=-k}^k \left( c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \left( S^2 \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} \right. \right. \\ \left. \left. + (1 - S_f^2) \tau_f^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2} \right. \right. \\ \left. \left. + (S_f^2 - S^2) \tau_s^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2} \right) \right. \\ \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i) \tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right) \right). \end{aligned} \quad (13.78)$$

#### $\mathfrak{D}_j$ partial derivative

The partial derivative of (13.63) with respect to the orientational parameter  $\mathfrak{D}_j$  is

$$\frac{\partial J(\omega)}{\partial \mathfrak{D}_j} = \frac{2}{5} \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i) \tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right). \quad (13.79)$$

#### $S^2$ partial derivative

The partial derivative of (13.63) with respect to the order parameter  $S^2$  is

$$\frac{\partial J(\omega)}{\partial S^2} = \frac{2}{5} \sum_{i=-k}^k c_i \tau_i \left( \frac{1}{1 + (\omega \tau_i)^2} - \frac{(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right). \quad (13.80)$$

#### $S_f^2$ partial derivative

The partial derivative of (13.63) with respect to the order parameter  $S_f^2$  is

$$\frac{\partial J(\omega)}{\partial S_f^2} = -\frac{2}{5} \sum_{i=-k}^k c_i \tau_i \left( \frac{(\tau_f + \tau_i) \tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} - \frac{(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right). \quad (13.81)$$



**$\tau_f$  partial derivative**

The partial derivative of (13.63) with respect to the correlation time  $\tau_f$  is

$$\frac{\partial J(\omega)}{\partial \tau_f} = \frac{2}{5}(1 - S_f^2) \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2}. \quad (13.82)$$

 **$\tau_s$  partial derivative**

The partial derivative of (13.63) with respect to the correlation time  $\tau_s$  is

$$\frac{\partial J(\omega)}{\partial \tau_s} = \frac{2}{5}(S_f^2 - S^2) \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2}. \quad (13.83)$$

### 13.8.5 The extended model-free Hessian

The model-free Hessian of the extended spectral density function (13.63) is the matrix of second partial derivatives. The matrix coordinates correspond to the model parameters which are being optimised.

#### $\mathfrak{G}_j - \mathfrak{G}_k$ partial derivative

The second partial derivative of (13.63) with respect to the geometric parameters  $\mathfrak{G}_j$  and  $\mathfrak{G}_k$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{G}_k} = & \frac{2}{5} \sum_{i=-k}^k \left( -2c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \cdot \frac{\partial \tau_i}{\partial \mathfrak{G}_k} \left( S^2 \omega^2 \tau_i \frac{3 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^3} \right. \right. \\ & + (1 - S_f^2) \tau_f^2 \frac{(\tau_f + \tau_i)^3 + 3\omega^2 \tau_f^3 \tau_i (\tau_f + \tau_i) - (\omega \tau_f)^4 \tau_i^3}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^3} \\ & + (S_f^2 - S^2) \tau_s^2 \frac{(\tau_s + \tau_i)^3 + 3\omega^2 \tau_s^3 \tau_i (\tau_s + \tau_i) - (\omega \tau_s)^4 \tau_i^3}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^3} \Big) \\ & + \left( \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \cdot \frac{\partial c_i}{\partial \mathfrak{G}_k} + \frac{\partial \tau_i}{\partial \mathfrak{G}_k} \cdot \frac{\partial c_i}{\partial \mathfrak{G}_j} + c_i \frac{\partial^2 \tau_i}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{G}_k} \right) \left( S^2 \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} \right. \\ & + (1 - S_f^2) \tau_f^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2} \\ & + (S_f^2 - S^2) \tau_s^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2} \Big) \\ & \left. + \left( \frac{\partial^2 c_i}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{G}_k} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i) \tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right) \right) \right). \end{aligned} \quad (13.84)$$

#### $\mathfrak{G}_j - \mathfrak{Q}_k$ partial derivative

The second partial derivative of (13.63) with respect to the geometric parameter  $\mathfrak{G}_j$  and the orientational parameter  $\mathfrak{Q}_k$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{Q}_k} = & \frac{2}{5} \sum_{i=-k}^k \left( \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \frac{\partial c_i}{\partial \mathfrak{Q}_k} \left( S^2 \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} \right. \right. \\ & + (1 - S_f^2) \tau_f^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2} \\ & + (S_f^2 - S^2) \tau_s^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2} \Big) \\ & + \frac{\partial^2 c_i}{\partial \mathfrak{G}_j \cdot \partial \mathfrak{Q}_k} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i) \tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right) \Big). \end{aligned} \quad (13.85)$$

**$\mathfrak{G}_j - S^2$  partial derivative**

The second partial derivative of (13.63) with respect to the geometric parameter  $\mathfrak{G}_j$  and the order parameter  $S^2$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial S^2} = \frac{2}{5} \sum_{i=-k}^k \left( c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \left( \frac{1 - (\omega \tau_i)^2}{(1 + (\omega \tau_i)^2)^2} - \tau_s^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2} \right) \right. \\ \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i \left( \frac{1}{1 + (\omega \tau_i)^2} - \frac{(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right) \right). \quad (13.86) \end{aligned}$$

 **$\mathfrak{G}_j - S_f^2$  partial derivative**

The second partial derivative of (13.63) with respect to the geometric parameter  $\mathfrak{G}_j$  and the order parameter  $S_f^2$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial S_f^2} = -\frac{2}{5} \sum_{i=-k}^k \left( c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \left( \tau_f^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2} - \tau_s^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2} \right) \right. \\ \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i \left( \frac{(\tau_f + \tau_i) \tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} - \frac{(\tau_s + \tau_i) \tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right) \right). \quad (13.87) \end{aligned}$$

 **$\mathfrak{G}_j - \tau_f$  partial derivative**

The second partial derivative of (13.63) with respect to the geometric parameter  $\mathfrak{G}_j$  and the correlation time  $\tau_f$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \tau_f} = \frac{2}{5} (1 - S_f^2) \sum_{i=-k}^k \left( 2c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \tau_f \tau_i (\tau_f + \tau_i) \frac{(\tau_f + \tau_i)^2 - 3(\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^3} \right. \\ \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2} \right). \quad (13.88) \end{aligned}$$

 **$\mathfrak{G}_j - \tau_s$  partial derivative**

The second partial derivative of (13.63) with respect to the geometric parameter  $\mathfrak{G}_j$  and the correlation time  $\tau_s$  is

$$\begin{aligned} \frac{\partial^2 J(\omega)}{\partial \mathfrak{G}_j \cdot \partial \tau_s} = \frac{2}{5} (S_f^2 - S^2) \sum_{i=-k}^k \left( 2c_i \frac{\partial \tau_i}{\partial \mathfrak{G}_j} \tau_s \tau_i (\tau_s + \tau_i) \frac{(\tau_s + \tau_i)^2 - 3(\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^3} \right. \\ \left. + \frac{\partial c_i}{\partial \mathfrak{G}_j} \tau_i^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2} \right). \quad (13.89) \end{aligned}$$

**$\mathfrak{D}_j - \mathfrak{D}_k$  partial derivative**

The second partial derivative of (13.63) with respect to the orientational parameters  $\mathfrak{D}_j$  and  $\mathfrak{D}_k$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k} = \frac{2}{5} \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k} \tau_i \left( \frac{S^2}{1 + (\omega \tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i)\tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i)\tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right). \quad (13.90)$$

 **$\mathfrak{D}_j - S^2$  partial derivative**

The second partial derivative of (13.63) with respect to the orientational parameter  $\mathfrak{D}_j$  and the order parameter  $S^2$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial S^2} = \frac{2}{5} \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i \left( \frac{1}{1 + (\omega \tau_i)^2} - \frac{(\tau_s + \tau_i)\tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right). \quad (13.91)$$

 **$\mathfrak{D}_j - S_f^2$  partial derivative**

The second partial derivative of (13.63) with respect to the orientational parameter  $\mathfrak{D}_j$  and the order parameter  $S_f^2$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial S_f^2} = -\frac{2}{5} \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i \left( \frac{(\tau_f + \tau_i)\tau_f}{(\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2} - \frac{(\tau_s + \tau_i)\tau_s}{(\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2} \right). \quad (13.92)$$

 **$\mathfrak{D}_j - \tau_f$  partial derivative**

The second partial derivative of (13.63) with respect to the orientational parameter  $\mathfrak{D}_j$  and the correlation time  $\tau_f$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial \tau_f} = \frac{2}{5} (1 - S_f^2) \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2}. \quad (13.93)$$

 **$\mathfrak{D}_j - \tau_s$  partial derivative**

The second partial derivative of (13.63) with respect to the orientational parameter  $\mathfrak{D}_j$  and the correlation time  $\tau_s$  is

$$\frac{\partial^2 J(\omega)}{\partial \mathfrak{D}_j \cdot \partial \tau_s} = \frac{2}{5} (S_f^2 - S^2) \sum_{i=-k}^k \frac{\partial c_i}{\partial \mathfrak{D}_j} \tau_i^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2}. \quad (13.94)$$

**$S^2 - S^2$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameter  $S^2$  twice is

$$\frac{\partial^2 J(\omega)}{(\partial S^2)^2} = 0. \quad (13.95)$$

 **$S^2 - S_f^2$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameters  $S^2$  and  $S_f^2$  is

$$\frac{\partial^2 J(\omega)}{\partial S^2 \cdot \partial S_f^2} = 0. \quad (13.96)$$

 **$S^2 - \tau_f$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameter  $S^2$  and correlation time  $\tau_f$  is

$$\frac{\partial^2 J(\omega)}{\partial S^2 \cdot \partial \tau_f} = 0. \quad (13.97)$$

 **$S^2 - \tau_s$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameter  $S^2$  and correlation time  $\tau_s$  is

$$\frac{\partial^2 J(\omega)}{\partial S^2 \cdot \partial \tau_s} = -\frac{2}{5} \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2}. \quad (13.98)$$

 **$S_f^2 - S_f^2$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameter  $S_f^2$  twice is

$$\frac{\partial^2 J(\omega)}{(\partial S_f^2)^2} = 0. \quad (13.99)$$

 **$S_f^2 - \tau_f$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameter  $S_f^2$  and correlation time  $\tau_f$  is

$$\frac{\partial^2 J(\omega)}{\partial S_f^2 \cdot \partial \tau_f} = -\frac{2}{5} \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_f + \tau_i)^2 - (\omega \tau_f \tau_i)^2}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^2}. \quad (13.100)$$

**$S_f^2 - \tau_s$  partial derivative**

The second partial derivative of (13.63) with respect to the order parameter  $S_f^2$  and correlation time  $\tau_s$  is

$$\frac{\partial^2 J(\omega)}{\partial S_f^2 \cdot \partial \tau_s} = \frac{2}{5} \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_s + \tau_i)^2 - (\omega \tau_s \tau_i)^2}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^2}. \quad (13.101)$$

 **$\tau_f - \tau_f$  partial derivative**

The second partial derivative of (13.62) with respect to the correlation time  $\tau_f$  twice is

$$\frac{\partial^2 J(\omega)}{\partial \tau_f^2} = -\frac{4}{5} (1 - S_f^2) \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_f + \tau_i)^3 + 3\omega^2 \tau_i^3 \tau_f (\tau_f + \tau_i) - (\omega \tau_i)^4 \tau_f^3}{((\tau_f + \tau_i)^2 + (\omega \tau_f \tau_i)^2)^3} \quad (13.102)$$

 **$\tau_f - \tau_s$  partial derivative**

The second partial derivative of (13.62) with respect to the correlation times  $\tau_f$  and  $\tau_s$  is

$$\frac{\partial^2 J(\omega)}{\partial \tau_f \cdot \partial \tau_s} = 0. \quad (13.103)$$

 **$\tau_s - \tau_s$  partial derivative**

The second partial derivative of (13.62) with respect to the correlation time  $\tau_s$  twice is

$$\frac{\partial^2 J(\omega)}{\partial \tau_s^2} = -\frac{4}{5} (S_f^2 - S^2) \sum_{i=-k}^k c_i \tau_i^2 \frac{(\tau_s + \tau_i)^3 + 3\omega^2 \tau_i^3 \tau_s (\tau_s + \tau_i) - (\omega \tau_i)^4 \tau_s^3}{((\tau_s + \tau_i)^2 + (\omega \tau_s \tau_i)^2)^3} \quad (13.104)$$

## 13.9 Ellipsoidal diffusion tensor

### 13.9.1 The diffusion equation of the ellipsoid

The correlation function of the Brownian rotational diffusion of an ellipsoid is

$$C_O(\tau) = \frac{1}{5} \sum_{i=-2}^2 c_i e^{-\frac{\tau}{\tau_i}}. \quad (13.105)$$

where  $c_i$  are the weights of the five exponential terms which are dependent on the orientation of the XH bond vector and  $\tau_i$  are the correlation times of the five exponential terms.

### 13.9.2 The weights of the ellipsoid

#### Definitions

The three direction cosines defining the XH bond vector within the diffusion frame are

$$\delta_x = \widehat{XH} \cdot \widehat{\mathfrak{D}}_x, \quad (13.106a)$$

$$\delta_y = \widehat{XH} \cdot \widehat{\mathfrak{D}}_y, \quad (13.106b)$$

$$\delta_z = \widehat{XH} \cdot \widehat{\mathfrak{D}}_z. \quad (13.106c)$$

Let the set of geometric parameters be

$$\mathfrak{G} = \{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r\}, \quad (13.107)$$

and the set of orientational parameters be the Euler angles

$$\mathfrak{D} = \{\alpha, \beta, \gamma\}. \quad (13.108)$$

#### The weights

The five weights  $c_i$  in the correlation function of the Brownian rotational diffusion of an ellipsoid (13.105) are

$$c_{-2} = \frac{1}{4}(d - e), \quad (13.109a)$$

$$c_{-1} = 3\delta_y^2\delta_z^2, \quad (13.109b)$$

$$c_0 = 3\delta_x^2\delta_z^2, \quad (13.109c)$$

$$c_1 = 3\delta_x^2\delta_y^2, \quad (13.109d)$$

$$c_2 = \frac{1}{4}(d + e), \quad (13.109e)$$

where

$$d = 3 (\delta_x^4 + \delta_y^4 + \delta_z^4) - 1, \quad (13.110)$$

$$e = \frac{1}{\Re} \left[ (1 + 3\mathfrak{D}_r) (\delta_x^4 + 2\delta_y^2\delta_z^2) + (1 - 3\mathfrak{D}_r) (\delta_y^4 + 2\delta_x^2\delta_z^2) - 2 (\delta_z^4 + 2\delta_x^2\delta_y^2) \right]. \quad (13.111)$$

The factor  $\Re$  is defined as

$$\Re = \sqrt{1 + 3\mathfrak{D}_r^2}. \quad (13.112)$$

### 13.9.3 The weight gradients of the ellipsoid

#### $\mathfrak{D}_i$ partial derivative

The partial derivatives with respect to the orientational parameter  $\mathfrak{D}_i$  are

$$\frac{\partial c_{-2}}{\partial \mathfrak{D}_i} = 3 \left( \delta_x^3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} + \delta_y^3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_z^3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \right) - \frac{\partial e}{\partial \mathfrak{D}_i}, \quad (13.113a)$$

$$\frac{\partial c_{-1}}{\partial \mathfrak{D}_i} = 6\delta_y\delta_z \left( \delta_y \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_z \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \right), \quad (13.113b)$$

$$\frac{\partial c_0}{\partial \mathfrak{D}_i} = 6\delta_x\delta_z \left( \delta_x \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_z \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \right), \quad (13.113c)$$

$$\frac{\partial c_1}{\partial \mathfrak{D}_i} = 6\delta_x\delta_y \left( \delta_x \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_y \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \right), \quad (13.113d)$$

$$\frac{\partial c_2}{\partial \mathfrak{D}_i} = 3 \left( \delta_x^3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} + \delta_y^3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_z^3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \right) + \frac{\partial e}{\partial \mathfrak{D}_i}, \quad (13.113e)$$

where

$$\begin{aligned} \frac{\partial e}{\partial \mathfrak{D}_i} = \frac{1}{\Re} & \left[ (1 + 3\mathfrak{D}_r) \left( \delta_x^3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} + \delta_y\delta_z \left( \delta_y \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_z \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \right) \right) \right. \\ & + (1 - 3\mathfrak{D}_r) \left( \delta_y^3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_x\delta_z \left( \delta_x \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_z \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \right) \right) \\ & \left. - 2 \left( \delta_z^3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_x\delta_y \left( \delta_x \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_y \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \right) \right) \right]. \end{aligned} \quad (13.114)$$



**$\tau_m$  partial derivative**

The partial derivatives with respect to the  $\tau_m$  geometric parameter are

$$\frac{\partial c_{-2}}{\partial \tau_m} = 0, \quad (13.115a)$$

$$\frac{\partial c_{-1}}{\partial \tau_m} = 0, \quad (13.115b)$$

$$\frac{\partial c_0}{\partial \tau_m} = 0, \quad (13.115c)$$

$$\frac{\partial c_1}{\partial \tau_m} = 0, \quad (13.115d)$$

$$\frac{\partial c_2}{\partial \tau_m} = 0. \quad (13.115e)$$

 **$\mathfrak{D}_a$  partial derivative**

The partial derivatives with respect to the  $\mathfrak{D}_a$  geometric parameter are

$$\frac{\partial c_{-2}}{\partial \mathfrak{D}_a} = 0, \quad (13.116a)$$

$$\frac{\partial c_{-1}}{\partial \mathfrak{D}_a} = 0, \quad (13.116b)$$

$$\frac{\partial c_0}{\partial \mathfrak{D}_a} = 0, \quad (13.116c)$$

$$\frac{\partial c_1}{\partial \mathfrak{D}_a} = 0, \quad (13.116d)$$

$$\frac{\partial c_2}{\partial \mathfrak{D}_a} = 0. \quad (13.116e)$$

 **$\mathfrak{D}_r$  partial derivative**

The partial derivatives with respect to the  $\mathfrak{D}_r$  geometric parameter are

$$\frac{\partial c_{-2}}{\partial \mathfrak{D}_r} = -\frac{3}{4} \frac{\partial e}{\partial \mathfrak{D}_r}, \quad (13.117a)$$

$$\frac{\partial c_{-1}}{\partial \mathfrak{D}_r} = 0, \quad (13.117b)$$

$$\frac{\partial c_0}{\partial \mathfrak{D}_r} = 0, \quad (13.117c)$$

$$\frac{\partial c_1}{\partial \mathfrak{D}_r} = 0, \quad (13.117d)$$

$$\frac{\partial c_2}{\partial \mathfrak{D}_r} = \frac{3}{4} \frac{\partial e}{\partial \mathfrak{D}_r}, \quad (13.117e)$$

where

$$\frac{\partial e}{\partial \mathfrak{D}_r} = \frac{1}{\mathfrak{N}^3} \left[ (1 - \mathfrak{D}_r) (\delta_x^4 + 2\delta_y^2 \delta_z^2) - (1 + \mathfrak{D}_r) (\delta_y^4 + 2\delta_x^2 \delta_z^2) + 2\mathfrak{D}_r (\delta_z^4 + 2\delta_x^2 \delta_y^2) \right]. \quad (13.118)$$

### 13.9.4 The weight Hessians of the ellipsoid

#### $\mathfrak{D}_i - \mathfrak{D}_j$ partial derivative

The second partial derivatives with respect to the orientational parameters  $\mathfrak{D}_i$  and  $\mathfrak{D}_j$  are

$$\begin{aligned} \frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = & 3 \left( \delta_x^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \right. \\ & + \delta_y^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \\ & \left. + \delta_z^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \right) - \frac{\partial^2 e}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j}, \end{aligned} \quad (13.119a)$$

$$\begin{aligned} \frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = & 6\delta_y^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \\ & + 12\delta_y \delta_z \left( \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \\ & + 6\delta_z^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right), \end{aligned} \quad (13.119b)$$

$$\begin{aligned} \frac{\partial^2 c_0}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = & 6\delta_x^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \\ & + 12\delta_x \delta_z \left( \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \\ & + 6\delta_z^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right), \end{aligned} \quad (13.119c)$$

$$\begin{aligned} \frac{\partial^2 c_1}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = & 6\delta_x^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \\ & + 12\delta_x \delta_y \left( \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} + \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \\ & + 6\delta_y^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right), \end{aligned} \quad (13.119d)$$

$$\begin{aligned} \frac{\partial^2 c_2}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = & 3 \left( \delta_x^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \right. \\ & + \delta_y^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \\ & \left. + \delta_z^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \right) + \frac{\partial^2 e}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j}, \end{aligned} \quad (13.119e)$$

where

$$\begin{aligned}
\frac{\partial^2 e}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = \frac{1}{\Re} \Bigg[ & (1 + 3\mathfrak{D}_r) \left( \delta_x^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \right. \\
& + \delta_y^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \\
& + \delta_z^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \\
& \left. + 2\delta_y \delta_z \left( \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \right) \\
& + (1 - 3\mathfrak{D}_r) \left( \delta_y^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \right. \\
& + \delta_x^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \\
& + \delta_z^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \\
& \left. + 2\delta_x \delta_z \left( \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \right) \\
& - 2 \left( \delta_z^2 \left( \delta_z \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + 3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} \right) \right. \\
& + \delta_x^2 \left( \delta_y \frac{\partial^2 \delta_y}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} \right) \\
& + \delta_y^2 \left( \delta_x \frac{\partial^2 \delta_x}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} + \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \\
& \left. + 2\delta_x \delta_y \left( \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_y}{\partial \mathfrak{D}_j} + \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_x}{\partial \mathfrak{D}_j} \right) \right) \Bigg]. \quad (13.120)
\end{aligned}$$

#### $\mathfrak{D}_i - \tau_m$ partial derivative

The second partial derivatives with respect to the orientational parameter  $\mathfrak{D}_i$  and the geometric parameter  $\tau_m$  are

$$\frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_i \cdot \partial \tau_m} = 0, \quad (13.121a)$$

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_i \cdot \partial \tau_m} = 0, \quad (13.121b)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_i \cdot \partial \tau_m} = 0, \quad (13.121c)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_i \cdot \partial \tau_m} = 0, \quad (13.121d)$$

$$\frac{\partial^2 c_2}{\partial \mathfrak{D}_i \cdot \partial \tau_m} = 0. \quad (13.121e)$$

### $\mathfrak{D}_i - \mathfrak{D}_a$ partial derivative

The second partial derivatives with respect to the orientational parameter  $\mathfrak{D}_i$  and the geometric parameter  $\mathfrak{D}_a$  are

$$\frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_a} = 0, \quad (13.122a)$$

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_a} = 0, \quad (13.122b)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_a} = 0, \quad (13.122c)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_a} = 0, \quad (13.122d)$$

$$\frac{\partial^2 c_2}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_a} = 0. \quad (13.122e)$$

### $O_i - D_r$ partial derivative

The second partial derivatives with respect to the orientational parameter  $\mathfrak{D}_i$  and the geometric parameter  $\mathfrak{D}_r$  are

$$\frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r} = -3 \frac{\partial^2 e}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r}, \quad (13.123a)$$

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r} = 0, \quad (13.123b)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r} = 0, \quad (13.123c)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r} = 0, \quad (13.123d)$$

$$\frac{\partial^2 c_2}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r} = 3 \frac{\partial^2 e}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r}, \quad (13.123e)$$

where

$$\begin{aligned} \frac{\partial^2 e}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_r} = \frac{1}{\mathfrak{R}^3} & \left[ (1 - \mathfrak{D}_r) \left( \delta_x^3 \frac{\partial \delta_x}{\partial \mathfrak{D}_i} + \delta_y \delta_z \left( \delta_y \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_z \frac{\partial \delta_y}{\partial \mathfrak{D}_i} \right) \right) \right. \\ & - (1 + \mathfrak{D}_r) \left( \delta_y^3 \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_x \delta_z \left( \delta_x \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_z \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \right) \right) \\ & \left. + 2\mathfrak{D}_r \left( \delta_z^3 \frac{\partial \delta_z}{\partial \mathfrak{D}_i} + \delta_x \delta_y \left( \delta_x \frac{\partial \delta_y}{\partial \mathfrak{D}_i} + \delta_y \frac{\partial \delta_x}{\partial \mathfrak{D}_i} \right) \right) \right]. \quad (13.124) \end{aligned}$$

**$\tau_m - \tau_m$  partial derivative**

The second partial derivatives with respect to the geometric parameter  $\tau_m$  twice are

$$\frac{\partial^2 c_{-2}}{\partial \tau_m^2} = 0, \quad (13.125a)$$

$$\frac{\partial^2 c_{-1}}{\partial \tau_m^2} = 0, \quad (13.125b)$$

$$\frac{\partial^2 c_0}{\partial \tau_m^2} = 0, \quad (13.125c)$$

$$\frac{\partial^2 c_1}{\partial \tau_m^2} = 0, \quad (13.125d)$$

$$\frac{\partial^2 c_2}{\partial \tau_m^2} = 0. \quad (13.125e)$$

 **$\tau_m - \mathfrak{D}_a$  partial derivative**

The second partial derivatives with respect to the geometric parameters  $\tau_m$  and  $\mathfrak{D}_a$  are

$$\frac{\partial^2 c_{-2}}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 0, \quad (13.126a)$$

$$\frac{\partial^2 c_{-1}}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 0, \quad (13.126b)$$

$$\frac{\partial^2 c_0}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 0, \quad (13.126c)$$

$$\frac{\partial^2 c_1}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 0, \quad (13.126d)$$

$$\frac{\partial^2 c_2}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 0. \quad (13.126e)$$

 **$\tau_m - \mathfrak{D}_r$  partial derivative**

The second partial derivatives with respect to the geometric parameters  $\tau_m$  and  $\mathfrak{D}_r$  are

$$\frac{\partial^2 c_{-2}}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 0, \quad (13.127a)$$

$$\frac{\partial^2 c_{-1}}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 0, \quad (13.127b)$$

$$\frac{\partial^2 c_0}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 0, \quad (13.127c)$$

$$\frac{\partial^2 c_1}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 0, \quad (13.127d)$$

$$\frac{\partial^2 c_2}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 0. \quad (13.127e)$$

**$\mathfrak{D}_a - \mathfrak{D}_a$  partial derivative**

The second partial derivatives with respect to the geometric parameter  $\mathfrak{D}_a$  twice are

$$\frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_a^2} = 0, \quad (13.128a)$$

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_a^2} = 0, \quad (13.128b)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_a^2} = 0, \quad (13.128c)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_a^2} = 0, \quad (13.128d)$$

$$\frac{\partial^2 c_2}{\partial \mathfrak{D}_a^2} = 0. \quad (13.128e)$$

 **$\mathfrak{D}_a - \mathfrak{D}_r$  partial derivative**

The second partial derivatives with respect to the geometric parameters  $\mathfrak{D}_a$  and  $\mathfrak{D}_r$  are

$$\frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 0, \quad (13.129a)$$

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 0, \quad (13.129b)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 0, \quad (13.129c)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 0, \quad (13.129d)$$

$$\frac{\partial^2 c_2}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 0. \quad (13.129e)$$

 **$\mathfrak{D}_r - \mathfrak{D}_r$  partial derivative**

The second partial derivatives with respect to the geometric parameter  $\mathfrak{D}_r$  twice are

$$\frac{\partial^2 c_{-2}}{\partial \mathfrak{D}_r^2} = -\frac{3}{4} \frac{\partial^2 e}{\partial \mathfrak{D}_r^2}, \quad (13.130a)$$

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_r^2} = 0, \quad (13.130b)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_r^2} = 0, \quad (13.130c)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_r^2} = 0, \quad (13.130d)$$

$$\frac{\partial^2 c_2}{\partial \mathfrak{D}_r^2} = \frac{3}{4} \frac{\partial^2 e}{\partial \mathfrak{D}_r^2}, \quad (13.130e)$$

where

$$\begin{aligned} \frac{\partial^2 e}{\partial \mathfrak{D}_r^2} = \frac{1}{\mathfrak{R}^5} & \left[ (6\mathfrak{D}_r^2 - 9\mathfrak{D}_r - 1) (\delta_x^4 + 2\delta_y^2 \delta_z^2) \right. \\ & + (6\mathfrak{D}_r^2 + 9\mathfrak{D}_r - 1) (\delta_y^4 + 2\delta_x^2 \delta_z^2) \\ & \left. - 2(6\mathfrak{D}_r^2 - 1) (\delta_z^4 + 2\delta_x^2 \delta_y^2) \right]. \end{aligned} \quad (13.131)$$

### 13.9.5 The correlation times of the ellipsoid

The five correlation times  $\tau_i$  in the correlation function of the Brownian rotational diffusion of an ellipsoid (13.105) on page 255 are

$$\tau_{-2} = (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-1}, \quad (13.132a)$$

$$\tau_{-1} = (6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-1}, \quad (13.132b)$$

$$\tau_0 = (6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-1}, \quad (13.132c)$$

$$\tau_1 = (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-1}, \quad (13.132d)$$

$$\tau_2 = (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-1}, \quad (13.132e)$$

where  $\mathfrak{R}$  is defined in Equation (13.112) on page 256.

### 13.9.6 The correlation time gradients of the ellipsoid

#### $\tau_m$ partial derivative

The partial derivatives with respect to the geometric parameter  $\tau_m$  are

$$\frac{\partial \tau_{-2}}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-2}, \quad (13.133a)$$

$$\frac{\partial \tau_{-1}}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-2}, \quad (13.133b)$$

$$\frac{\partial \tau_0}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-2}, \quad (13.133c)$$

$$\frac{\partial \tau_1}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-2}, \quad (13.133d)$$

$$\frac{\partial \tau_2}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-2}. \quad (13.133e)$$

#### $\mathfrak{D}_a$ partial derivative

The partial derivatives with respect to the geometric parameter  $\mathfrak{D}_a$  are

$$\frac{\partial \tau_{-2}}{\partial \mathfrak{D}_a} = 2\mathfrak{R}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-2}, \quad (13.134a)$$

$$\frac{\partial \tau_{-1}}{\partial \mathfrak{D}_a} = (1 + 3\mathfrak{D}_r)(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-2}, \quad (13.134b)$$

$$\frac{\partial \tau_0}{\partial \mathfrak{D}_a} = (1 - 3\mathfrak{D}_r)(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-2}, \quad (13.134c)$$

$$\frac{\partial \tau_1}{\partial \mathfrak{D}_a} = -2(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-2}, \quad (13.134d)$$

$$\frac{\partial \tau_2}{\partial \mathfrak{D}_a} = -2\mathfrak{R}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-2}. \quad (13.134e)$$



**$\mathfrak{D}_r$  partial derivative**

The partial derivatives with respect to the geometric parameter  $\mathfrak{D}_r$  are

$$\frac{\partial \tau_{-2}}{\partial \mathfrak{D}_r} = 6 \frac{\mathfrak{D}_a \mathfrak{D}_r}{\mathfrak{R}} (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a \mathfrak{R})^{-2}, \quad (13.135a)$$

$$\frac{\partial \tau_{-1}}{\partial \mathfrak{D}_r} = 3\mathfrak{D}_a (6\mathfrak{D}_{iso} - \mathfrak{D}_a (1 + 3\mathfrak{D}_r))^{-2}, \quad (13.135b)$$

$$\frac{\partial \tau_0}{\partial \mathfrak{D}_r} = -3\mathfrak{D}_a (6\mathfrak{D}_{iso} - \mathfrak{D}_a (1 - 3\mathfrak{D}_r))^{-2}, \quad (13.135c)$$

$$\frac{\partial \tau_1}{\partial \mathfrak{D}_r} = 0, \quad (13.135d)$$

$$\frac{\partial \tau_2}{\partial \mathfrak{D}_r} = -6 \frac{\mathfrak{D}_a \mathfrak{D}_r}{\mathfrak{R}} (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a \mathfrak{R})^{-2}. \quad (13.135e)$$

### 13.9.7 The correlation time Hessians of the ellipsoid

#### $\tau_m - \tau_m$ partial derivative

The second partial derivatives with respect to the geometric parameter  $\tau_m$  twice are

$$\frac{\partial^2 \tau_{-2}}{\partial \tau_m^2} = 2\tau_m^{-4}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-3} - 2\tau_m^{-3}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-2}, \quad (13.136a)$$

$$\frac{\partial^2 \tau_{-1}}{\partial \tau_m^2} = 2\tau_m^{-4}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-3} - 2\tau_m^{-3}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-2}, \quad (13.136b)$$

$$\frac{\partial^2 \tau_0}{\partial \tau_m^2} = 2\tau_m^{-4}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-3} - 2\tau_m^{-3}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-2}, \quad (13.136c)$$

$$\frac{\partial^2 \tau_1}{\partial \tau_m^2} = 2\tau_m^{-4}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-3} - 2\tau_m^{-3}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-2}, \quad (13.136d)$$

$$\frac{\partial^2 \tau_2}{\partial \tau_m^2} = 2\tau_m^{-4}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-3} - 2\tau_m^{-3}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-2}. \quad (13.136e)$$

#### $\tau_m - \mathfrak{D}_a$ partial derivative

The second partial derivatives with respect to the geometric parameters  $\tau_m$  and  $\mathfrak{D}_a$  are

$$\frac{\partial^2 \tau_{-2}}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 4\mathfrak{R}\tau_m^{-2}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-3}, \quad (13.137a)$$

$$\frac{\partial^2 \tau_{-1}}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 2(1 + 3\mathfrak{D}_r)\tau_m^{-2}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-3}, \quad (13.137b)$$

$$\frac{\partial^2 \tau_0}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 2(1 - 3\mathfrak{D}_r)\tau_m^{-2}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-3}, \quad (13.137c)$$

$$\frac{\partial^2 \tau_1}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = -4\tau_m^{-2}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-3}, \quad (13.137d)$$

$$\frac{\partial^2 \tau_2}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = -4\mathfrak{R}\tau_m^{-2}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-3}. \quad (13.137e)$$

#### $\tau_m - \mathfrak{D}_r$ partial derivative

The second partial derivatives with respect to the geometric parameters  $\tau_m$  and  $\mathfrak{D}_r$  are

$$\frac{\partial^2 \tau_{-2}}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 12\frac{\mathfrak{D}_a\mathfrak{D}_r}{\mathfrak{R}}\tau_m^{-2}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{R})^{-3}, \quad (13.138a)$$

$$\frac{\partial^2 \tau_{-1}}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 6\mathfrak{D}_a\tau_m^{-2}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-3}, \quad (13.138b)$$

$$\frac{\partial^2 \tau_0}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = -6\mathfrak{D}_a\tau_m^{-2}(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-3}, \quad (13.138c)$$

$$\frac{\partial^2 \tau_1}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = 0, \quad (13.138d)$$

$$\frac{\partial^2 \tau_2}{\partial \tau_m \cdot \partial \mathfrak{D}_r} = -12\frac{\mathfrak{D}_a\mathfrak{D}_r}{\mathfrak{R}}\tau_m^{-2}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{R})^{-3}. \quad (13.138e)$$

**$\mathfrak{D}_a - \mathfrak{D}_a$  partial derivative**

The second partial derivatives with respect to the geometric parameter  $\mathfrak{D}_a$  twice are

$$\frac{\partial^2 \tau_{-2}}{\partial \mathfrak{D}_a^2} = 8\mathfrak{K}^2(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{K})^{-3}, \quad (13.139a)$$

$$\frac{\partial^2 \tau_{-1}}{\partial \mathfrak{D}_a^2} = 2(1 + 3\mathfrak{D}_r)^2(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-3}, \quad (13.139b)$$

$$\frac{\partial^2 \tau_0}{\partial \mathfrak{D}_a^2} = 2(1 - 3\mathfrak{D}_r)^2(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-3}, \quad (13.139c)$$

$$\frac{\partial^2 \tau_1}{\partial \mathfrak{D}_a^2} = 8(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-3}, \quad (13.139d)$$

$$\frac{\partial^2 \tau_2}{\partial \mathfrak{D}_a^2} = 8\mathfrak{K}^2(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{K})^{-3}. \quad (13.139e)$$

 **$\mathfrak{D}_a - \mathfrak{D}_r$  partial derivative**

The second partial derivatives with respect to the geometric parameters  $\mathfrak{D}_a$  and  $\mathfrak{D}_r$  are

$$\frac{\partial^2 \tau_{-2}}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 24\mathfrak{D}_a\mathfrak{D}_r(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{K})^{-3} + 6\frac{\mathfrak{D}_r}{\mathfrak{K}}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{K})^{-2}, \quad (13.140a)$$

$$\frac{\partial^2 \tau_{-1}}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 6\mathfrak{D}_a(1 + 3\mathfrak{D}_r)(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-3} + 3(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-2}, \quad (13.140b)$$

$$\frac{\partial^2 \tau_0}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = -6\mathfrak{D}_a(1 - 3\mathfrak{D}_r)(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-3} - 3(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-2}, \quad (13.140c)$$

$$\frac{\partial^2 \tau_1}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 0, \quad (13.140d)$$

$$\frac{\partial^2 \tau_2}{\partial \mathfrak{D}_a \cdot \partial \mathfrak{D}_r} = 24\mathfrak{D}_a\mathfrak{D}_r(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{K})^{-3} - 6\frac{\mathfrak{D}_r}{\mathfrak{K}}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{K})^{-2}. \quad (13.140e)$$

 **$\mathfrak{D}_r - \mathfrak{D}_r$  partial derivative**

The second partial derivatives with respect to the geometric parameter  $\mathfrak{D}_r$  twice are

$$\frac{\partial^2 \tau_{-2}}{\partial \mathfrak{D}_r^2} = 72 \left( \frac{\mathfrak{D}_a\mathfrak{D}_r}{\mathfrak{K}} \right)^2 (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{K})^{-3} + 6\frac{\mathfrak{D}_a}{\mathfrak{K}^3}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{K})^{-2}, \quad (13.141a)$$

$$\frac{\partial^2 \tau_{-1}}{\partial \mathfrak{D}_r^2} = 18\mathfrak{D}_a^2(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r))^{-3}, \quad (13.141b)$$

$$\frac{\partial^2 \tau_0}{\partial \mathfrak{D}_r^2} = 18\mathfrak{D}_a^2(6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r))^{-3}, \quad (13.141c)$$

$$\frac{\partial^2 \tau_1}{\partial \mathfrak{D}_r^2} = 0, \quad (13.141d)$$

$$\frac{\partial^2 \tau_2}{\partial \mathfrak{D}_r^2} = 72 \left( \frac{\mathfrak{D}_a\mathfrak{D}_r}{\mathfrak{K}} \right)^2 (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\mathfrak{K})^{-3} - 6\frac{\mathfrak{D}_a}{\mathfrak{K}^3}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\mathfrak{K})^{-2}. \quad (13.141e)$$

## 13.10 Spheroidal diffusion tensor

### 13.10.1 The diffusion equation of the spheroid

The correlation function of the Brownian rotational diffusion of a spheroid is

$$C_O(\tau) = \frac{1}{5} \sum_{i=-1}^1 c_i e^{-\frac{\tau}{\tau_i}}. \quad (13.142)$$

where  $c_i$  are the weights of the three exponential terms which are dependent on the orientation of the XH bond vector and  $\tau_i$  are the correlation times of the three exponential terms.

### 13.10.2 The weights of the spheroid

#### Definitions

The direction cosine defining the XH bond vector within the spheroidal diffusion frame is

$$\delta_z = \widehat{XH} \cdot \widehat{\mathfrak{D}}_z. \quad (13.143)$$

Let the set of geometric parameters be

$$\mathfrak{G} = \{\mathfrak{D}_{iso}, \mathfrak{D}_a\}, \quad (13.144)$$

and the set of orientational parameters be the spherical angles

$$\mathfrak{D} = \{\theta, \phi\}. \quad (13.145)$$

#### The weights

The three spheroid weights  $c_i$  in the correlation function of the Brownian rotational diffusion of a spheroid (13.142) are

$$c_{-1} = \frac{1}{4}(3\delta_z^2 - 1)^2, \quad (13.146a)$$

$$c_0 = 3\delta_z^2(1 - \delta_z^2), \quad (13.146b)$$

$$c_1 = \frac{3}{4}(\delta_z^2 - 1)^2. \quad (13.146c)$$

### 13.10.3 The weight gradients of the spheroid

#### $\mathfrak{D}_i$ partial derivative

The partial derivatives with respect to the orientational parameter  $\mathfrak{D}_i$  are

$$\frac{\partial c_{-1}}{\partial \mathfrak{D}_i} = 3\delta_z(3\delta_z^2 - 1)\frac{\partial \delta_z}{\partial \mathfrak{D}_i}, \quad (13.147a)$$

$$\frac{\partial c_0}{\partial \mathfrak{D}_i} = 6\delta_z(1 - 2\delta_z^2)\frac{\partial \delta_z}{\partial \mathfrak{D}_i}, \quad (13.147b)$$

$$\frac{\partial c_1}{\partial \mathfrak{D}_i} = 3\delta_z(\delta_z^2 - 1)\frac{\partial \delta_z}{\partial \mathfrak{D}_i}. \quad (13.147c)$$

### 13.10.4 The weight Hessians of the spheroid

#### $\mathfrak{D}_i - \mathfrak{D}_j$ partial derivative

The second partial derivatives with respect to the orientational parameters  $\mathfrak{D}_i$  and  $\mathfrak{D}_j$  are

$$\frac{\partial^2 c_{-1}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = 3 \left( (9\delta_z^2 - 1) \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \delta_z(3\delta_z^2 - 1) \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} \right), \quad (13.148a)$$

$$\frac{\partial^2 c_0}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = 6 \left( (1 - 6\delta_z^2) \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \delta_z(1 - 2\delta_z^2) \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} \right), \quad (13.148b)$$

$$\frac{\partial^2 c_1}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = 3 \left( (3\delta_z^2 - 1) \frac{\partial \delta_z}{\partial \mathfrak{D}_i} \cdot \frac{\partial \delta_z}{\partial \mathfrak{D}_j} + \delta_z(\delta_z^2 - 1) \frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} \right). \quad (13.148c)$$

### 13.10.5 The correlation times of the spheroid

The three spheroid correlation times  $\tau_i$  in the correlation function of the Brownian rotational diffusion of a spheroid (13.142) are

$$\tau_{-1} = (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-1}, \quad (13.149a)$$

$$\tau_0 = (6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-1}, \quad (13.149b)$$

$$\tau_1 = (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-1}. \quad (13.149c)$$

### 13.10.6 The correlation time gradients of the spheroid

#### $\tau_m$ partial derivative

The partial derivatives with respect to the geometric parameter  $\tau_m$  are

$$\frac{\partial \tau_{-1}}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-2}, \quad (13.150a)$$

$$\frac{\partial \tau_0}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-2}, \quad (13.150b)$$

$$\frac{\partial \tau_1}{\partial \tau_m} = \tau_m^{-2} (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-2}. \quad (13.150c)$$

#### $\mathfrak{D}_a$ partial derivative

The partial derivatives with respect to the geometric parameter  $\mathfrak{D}_a$  are

$$\frac{\partial \tau_{-1}}{\partial \mathfrak{D}_a} = 2(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-2}, \quad (13.151a)$$

$$\frac{\partial \tau_0}{\partial \mathfrak{D}_a} = (6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-2}, \quad (13.151b)$$

$$\frac{\partial \tau_1}{\partial \mathfrak{D}_a} = -2(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-2}. \quad (13.151c)$$

### 13.10.7 The correlation time Hessians of the spheroid

#### $\tau_m - \tau_m$ partial derivative

The second partial derivatives with respect to the geometric parameter  $\tau_m$  twice are

$$\frac{\partial^2 \tau_{-1}}{\partial \tau_m^2} = 2\tau_m^{-4} (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-3} - 2\tau_m^{-3} (6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-2}, \quad (13.152a)$$

$$\frac{\partial^2 \tau_0}{\partial \tau_m^2} = 2\tau_m^{-4} (6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-3} - 2\tau_m^{-3} (6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-2}, \quad (13.152b)$$

$$\frac{\partial^2 \tau_1}{\partial \tau_m^2} = 2\tau_m^{-4} (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-3} - 2\tau_m^{-3} (6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-2}. \quad (13.152c)$$

**$\tau_m - \mathfrak{D}_a$  partial derivative**

The second partial derivatives with respect to the geometric parameters  $\tau_m$  and  $\mathfrak{D}_a$  are

$$\frac{\partial^2 \tau_{-1}}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 4\tau_m^{-2}(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-3}, \quad (13.153a)$$

$$\frac{\partial^2 \tau_0}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = 2\tau_m^{-2}(6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-3}, \quad (13.153b)$$

$$\frac{\partial^2 \tau_1}{\partial \tau_m \cdot \partial \mathfrak{D}_a} = -4\tau_m^{-2}(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-3}. \quad (13.153c)$$

 **$\mathfrak{D}_a - \mathfrak{D}_a$  partial derivative**

The second partial derivatives with respect to the geometric parameter  $\mathfrak{D}_a$  twice are

$$\frac{\partial^2 \tau_{-1}}{\partial \mathfrak{D}_a^2} = 8(6\mathfrak{D}_{iso} - 2\mathfrak{D}_a)^{-3}, \quad (13.154a)$$

$$\frac{\partial^2 \tau_0}{\partial \mathfrak{D}_a^2} = 2(6\mathfrak{D}_{iso} - \mathfrak{D}_a)^{-3}, \quad (13.154b)$$

$$\frac{\partial^2 \tau_1}{\partial \mathfrak{D}_a^2} = 8(6\mathfrak{D}_{iso} + 2\mathfrak{D}_a)^{-3}. \quad (13.154c)$$

## 13.11 Spherical diffusion tensor

### 13.11.1 The diffusion equation of the sphere

The correlation function of the Brownian rotational diffusion of a sphere is

$$C_O(\tau) = \frac{1}{5} e^{-\frac{\tau}{\tau_m}}, \quad (13.155)$$

$$= \frac{1}{5} \sum_{i=0}^0 c_i e^{-\frac{\tau}{\tau_i}}. \quad (13.156)$$

where  $c_i$  is the weight of the single exponential term and  $\tau_i$  is the correlation time of the single exponential term.

### 13.11.2 The weight of the sphere

#### Definitions

The entire diffusion parameter set consists of a single geometric parameter and is

$$\mathfrak{D} = \{\tau_m\}. \quad (13.157)$$

#### Summation terms

The summation indices of the correlation function of the Brownian rotational diffusion of a sphere (13.142) range from  $k = 0$  to  $k = 0$  therefore

$$i \in \{0\}. \quad (13.158)$$

#### The weights

The single weight  $c_i$  in the correlation function of the Brownian rotational diffusion of a sphere (13.142) is

$$c_0 = 1. \quad (13.159)$$

### 13.11.3 The weight gradient of the sphere

#### $\tau_m$ partial derivative

The partial derivative with respect to the geometric parameter  $\tau_m$  is

$$\frac{\partial c_0}{\partial \tau_m} = 0. \quad (13.160)$$



**13.11.4 The weight Hessian of the sphere** $\tau_m - \tau_m$  **partial derivative**

The second partial derivatives with respect to the geometric parameter  $\tau_m$  twice is

$$\frac{\partial^2 c_0}{\partial \tau_m^2} = 0. \quad (13.161)$$

**13.11.5 The correlation time of the sphere**

The single correlation time  $\tau_i$  of the correlation function of the Brownian rotational diffusion of a sphere (13.142) is

$$\tau_0 = \tau_m. \quad (13.162)$$

**13.11.6 The correlation time gradient of the sphere** $\tau_m$  **partial derivative**

The partial derivative with respect to the geometric parameter  $\tau_m$  is

$$\frac{\partial \tau_0}{\partial \tau_m} = 1. \quad (13.163)$$

**13.11.7 The correlation time Hessian of the sphere** $\tau_m - \tau_m$  **partial derivative**

The second partial derivative with respect to the geometric parameter  $\tau_m$  twice is

$$\frac{\partial^2 \tau_0}{\partial \tau_m^2} = 0. \quad (13.164)$$

## 13.12 Ellipsoidal dot product derivatives

### 13.12.1 The dot product of the ellipsoid

The dot product is defined as

$$\delta_i = \widehat{XH} \cdot \widehat{\mathfrak{D}}_i, \quad (13.165)$$

where  $i$  is one of  $\{x, y, z\}$ ,  $\widehat{XH}$  is a unit vector parallel to the XH bond vector, and  $\widehat{\mathfrak{D}}_i$  is one of the unit vectors defining the diffusion frame. The three diffusion frame unit vectors can be expressed using the Euler angles  $\alpha$ ,  $\beta$ , and  $\gamma$  as

$$\widehat{\mathfrak{D}}_x = \begin{pmatrix} -\sin \alpha \sin \gamma + \cos \alpha \cos \beta \cos \gamma \\ -\sin \alpha \cos \gamma - \cos \alpha \cos \beta \sin \gamma \\ \cos \alpha \sin \beta \end{pmatrix}, \quad (13.166a)$$

$$\widehat{\mathfrak{D}}_y = \begin{pmatrix} \cos \alpha \sin \gamma + \sin \alpha \cos \beta \cos \gamma \\ \cos \alpha \cos \gamma - \sin \alpha \cos \beta \sin \gamma \\ \sin \alpha \sin \beta \end{pmatrix}, \quad (13.166b)$$

$$\widehat{\mathfrak{D}}_z = \begin{pmatrix} -\sin \beta \cos \gamma \\ \sin \beta \sin \gamma \\ \cos \beta \end{pmatrix}. \quad (13.166c)$$

### 13.12.2 The dot product gradient of the ellipsoid

The partial derivative of the dot product  $\delta_i$  with respect to the orientational parameter  $\mathfrak{D}_j$  is

$$\frac{\partial \delta_i}{\partial \mathfrak{D}_j} = \frac{\partial}{\partial \mathfrak{D}_j} (\widehat{XH} \cdot \widehat{\mathfrak{D}}_i) = \widehat{XH} \frac{\partial \widehat{\mathfrak{D}}_i}{\partial \mathfrak{D}_j} + \frac{\partial \widehat{XH}}{\partial \mathfrak{D}_j} \cdot \widehat{\mathfrak{D}}_i. \quad (13.167)$$

Because  $\widehat{XH}$  is constant and not dependent on the Euler angles its derivative is zero. Therefore

$$\frac{\partial \delta_i}{\partial \mathfrak{D}_j} = \widehat{XH} \frac{\partial \widehat{\mathfrak{D}}_i}{\partial \mathfrak{D}_j}. \quad (13.168)$$

#### The $\mathfrak{D}_x$ gradient

The partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_x$  with respect to the Euler angles are

$$\frac{\partial \widehat{\mathfrak{D}}_x}{\partial \alpha} = \begin{pmatrix} -\cos \alpha \sin \gamma - \sin \alpha \cos \beta \cos \gamma \\ -\cos \alpha \cos \gamma + \sin \alpha \cos \beta \sin \gamma \\ -\sin \alpha \sin \beta \end{pmatrix}, \quad (13.169a)$$

$$\frac{\partial \widehat{\mathfrak{D}}_x}{\partial \beta} = \begin{pmatrix} -\cos \alpha \sin \beta \cos \gamma \\ \cos \alpha \sin \beta \sin \gamma \\ \cos \alpha \cos \beta \end{pmatrix}, \quad (13.169b)$$

$$\frac{\partial \widehat{\mathfrak{D}}_x}{\partial \gamma} = \begin{pmatrix} -\sin \alpha \cos \gamma - \cos \alpha \cos \beta \sin \gamma \\ \sin \alpha \sin \gamma - \cos \alpha \cos \beta \cos \gamma \\ 0 \end{pmatrix}. \quad (13.169c)$$

**The  $\mathfrak{D}_y$  gradient**

The partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_y$  with respect to the Euler angles are

$$\frac{\partial \widehat{\mathfrak{D}}_y}{\partial \alpha} = \begin{pmatrix} -\sin \alpha \sin \gamma + \cos \alpha \cos \beta \cos \gamma \\ -\sin \alpha \cos \gamma - \cos \alpha \cos \beta \sin \gamma \\ \cos \alpha \sin \beta \end{pmatrix}, \quad (13.170a)$$

$$\frac{\partial \widehat{\mathfrak{D}}_y}{\partial \beta} = \begin{pmatrix} -\sin \alpha \sin \beta \cos \gamma \\ \sin \alpha \sin \beta \sin \gamma \\ \sin \alpha \cos \beta \end{pmatrix}, \quad (13.170b)$$

$$\frac{\partial \widehat{\mathfrak{D}}_y}{\partial \gamma} = \begin{pmatrix} \cos \alpha \cos \gamma - \sin \alpha \cos \beta \sin \gamma \\ -\cos \alpha \sin \gamma - \sin \alpha \cos \beta \cos \gamma \\ 0 \end{pmatrix}. \quad (13.170c)$$

**The  $\mathfrak{D}_z$  gradient**

The partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_z$  with respect to the Euler angles are

$$\frac{\partial \widehat{\mathfrak{D}}_z}{\partial \alpha} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \quad (13.171a)$$

$$\frac{\partial \widehat{\mathfrak{D}}_z}{\partial \beta} = \begin{pmatrix} -\cos \beta \cos \gamma \\ \cos \beta \sin \gamma \\ -\sin \beta \end{pmatrix}, \quad (13.171b)$$

$$\frac{\partial \widehat{\mathfrak{D}}_z}{\partial \gamma} = \begin{pmatrix} \sin \beta \sin \gamma \\ \sin \beta \cos \gamma \\ 0 \end{pmatrix}. \quad (13.171c)$$

### 13.12.3 The dot product Hessian of the ellipsoid

The second partial derivative of the dot product  $\delta_i$  with respect to the orientational parameters  $\mathfrak{D}_j$  and  $\mathfrak{D}_k$  is

$$\frac{\partial^2 \delta_i}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k} = \frac{\partial^2}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k} \left( \widehat{XH} \cdot \widehat{\mathfrak{D}}_i \right) = \widehat{XH} \frac{\partial^2 \widehat{\mathfrak{D}}_i}{\partial \mathfrak{D}_j \cdot \partial \mathfrak{D}_k}. \quad (13.172)$$

#### The $\mathfrak{D}_x$ Hessian

The second partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_x$  with respect to the Euler angles are

$$\frac{\partial^2 \widehat{\mathfrak{D}}_x}{\partial \alpha^2} = \begin{pmatrix} \sin \alpha \sin \gamma - \cos \alpha \cos \beta \cos \gamma \\ \sin \alpha \cos \gamma + \cos \alpha \cos \beta \sin \gamma \\ -\cos \alpha \sin \beta \end{pmatrix}, \quad (13.173a)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_x}{\partial \alpha \cdot \partial \beta} = \begin{pmatrix} \sin \alpha \sin \beta \cos \gamma \\ -\sin \alpha \sin \beta \sin \gamma \\ -\sin \alpha \cos \beta \end{pmatrix}, \quad (13.173b)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_x}{\partial \alpha \cdot \partial \gamma} = \begin{pmatrix} -\cos \alpha \cos \gamma + \sin \alpha \cos \beta \sin \gamma \\ \cos \alpha \sin \gamma + \sin \alpha \cos \beta \cos \gamma \\ 0 \end{pmatrix}, \quad (13.173c)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_x}{\partial \beta^2} = \begin{pmatrix} -\cos \alpha \cos \beta \cos \gamma \\ \cos \alpha \cos \beta \sin \gamma \\ -\cos \alpha \sin \beta \end{pmatrix}, \quad (13.173d)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_x}{\partial \beta \cdot \partial \gamma} = \begin{pmatrix} \cos \alpha \sin \beta \sin \gamma \\ \cos \alpha \sin \beta \cos \gamma \\ 0 \end{pmatrix}, \quad (13.173e)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_x}{\partial \gamma^2} = \begin{pmatrix} \sin \alpha \sin \gamma - \cos \alpha \cos \beta \cos \gamma \\ \sin \alpha \cos \gamma + \cos \alpha \cos \beta \sin \gamma \\ 0 \end{pmatrix}. \quad (13.173f)$$

#### The $\mathfrak{D}_y$ Hessian

The second partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_y$  with respect to the Euler angles are

$$\frac{\partial^2 \widehat{\mathfrak{D}}_y}{\partial \alpha^2} = \begin{pmatrix} -\cos \alpha \sin \gamma - \sin \alpha \cos \beta \cos \gamma \\ -\cos \alpha \cos \gamma + \sin \alpha \cos \beta \sin \gamma \\ -\sin \alpha \sin \beta \end{pmatrix}, \quad (13.174a)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_y}{\partial \alpha \cdot \partial \beta} = \begin{pmatrix} -\cos \alpha \sin \beta \cos \gamma \\ \cos \alpha \sin \beta \sin \gamma \\ \cos \alpha \cos \beta \end{pmatrix}, \quad (13.174b)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_y}{\partial \alpha \cdot \partial \gamma} = \begin{pmatrix} -\sin \alpha \cos \gamma - \cos \alpha \cos \beta \sin \gamma \\ \sin \alpha \sin \gamma - \cos \alpha \cos \beta \cos \gamma \\ 0 \end{pmatrix}, \quad (13.174c)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_y}{\partial \beta^2} = \begin{pmatrix} -\sin \alpha \cos \beta \cos \gamma \\ \sin \alpha \cos \beta \sin \gamma \\ -\sin \alpha \sin \beta \end{pmatrix}, \quad (13.174d)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_y}{\partial \beta \cdot \partial \gamma} = \begin{pmatrix} \sin \alpha \sin \beta \sin \gamma \\ \sin \alpha \sin \beta \cos \gamma \\ 0 \end{pmatrix}, \quad (13.174e)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_y}{\partial \gamma^2} = \begin{pmatrix} -\cos \alpha \sin \gamma - \sin \alpha \cos \beta \cos \gamma \\ -\cos \alpha \cos \gamma + \sin \alpha \cos \beta \sin \gamma \\ 0 \end{pmatrix}. \quad (13.174f)$$

### The $\mathfrak{D}_z$ Hessian

The second partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_z$  with respect to the Euler angles are

$$\frac{\partial^2 \widehat{\mathfrak{D}}_z}{\partial \alpha^2} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \quad (13.175a)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_z}{\partial \alpha \cdot \partial \beta} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \quad (13.175b)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_z}{\partial \alpha \cdot \partial \gamma} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \quad (13.175c)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_z}{\partial \beta^2} = \begin{pmatrix} \sin \beta \cos \gamma \\ -\sin \beta \sin \gamma \\ -\cos \beta \end{pmatrix}, \quad (13.175d)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_z}{\partial \beta \cdot \partial \gamma} = \begin{pmatrix} \cos \beta \sin \gamma \\ \cos \beta \cos \gamma \\ 0 \end{pmatrix}, \quad (13.175e)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_z}{\partial \gamma^2} = \begin{pmatrix} \sin \beta \cos \gamma \\ -\sin \beta \sin \gamma \\ 0 \end{pmatrix}. \quad (13.175f)$$

### 13.13 Spheroidal dot product derivatives

#### 13.13.1 The dot product of the spheroid

The single dot product of the spheroid is defined as

$$\delta_z = \widehat{XH} \cdot \widehat{\mathfrak{D}}_{\parallel}, \quad (13.176)$$

where  $\widehat{XH}$  is a unit vector parallel to the XH vector.  $\widehat{\mathfrak{D}}_{\parallel}$  is a unit vector parallel to the unique axis of the diffusion tensor and can be expressed using the spherical angles where  $\theta$  is the polar angle and  $\phi$  is the azimuthal angle as

$$\widehat{\mathfrak{D}}_{\parallel} = \begin{pmatrix} \sin \theta \cos \phi \\ \sin \theta \sin \phi \\ \cos \theta \end{pmatrix}. \quad (13.177)$$

#### 13.13.2 The dot product gradient of the spheroid

The partial derivative of the dot product with respect to the orientational parameter  $\mathfrak{D}_i$  is

$$\frac{\partial \delta_z}{\partial \mathfrak{D}_i} = \frac{\partial}{\partial \mathfrak{D}_i} (\widehat{XH} \cdot \widehat{\mathfrak{D}}_{\parallel}) = \widehat{XH} \frac{\partial \widehat{\mathfrak{D}}_{\parallel}}{\partial \mathfrak{D}_i} + \frac{\partial \widehat{XH}}{\partial \mathfrak{D}_i} \widehat{\mathfrak{D}}_{\parallel}. \quad (13.178)$$

Because the XH bond vector is constant and not dependent on the spherical angles its derivative is zero. Therefore

$$\frac{\partial \delta_z}{\partial \mathfrak{D}_i} = \widehat{XH} \frac{\partial \widehat{\mathfrak{D}}_{\parallel}}{\partial \mathfrak{D}_i}. \quad (13.179)$$

#### The $\mathfrak{D}_{\parallel}$ gradient

The partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_{\parallel}$  with respect to the spherical angles are

$$\frac{\partial \widehat{\mathfrak{D}}_{\parallel}}{\partial \theta} = \begin{pmatrix} \cos \theta \cos \phi \\ \cos \theta \sin \phi \\ -\sin \theta \end{pmatrix}, \quad (13.180a)$$

$$\frac{\partial \widehat{\mathfrak{D}}_{\parallel}}{\partial \phi} = \begin{pmatrix} -\sin \theta \sin \phi \\ \sin \theta \cos \phi \\ 0 \end{pmatrix}. \quad (13.180b)$$

#### 13.13.3 The dot product Hessian of the spheroid

The second partial derivative of the single spheroidal dot product  $\delta_z$  with respect to the orientational parameters  $\mathfrak{D}_i$  and  $\mathfrak{D}_j$  is

$$\frac{\partial^2 \delta_z}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} = \frac{\partial^2}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j} (\widehat{XH} \cdot \widehat{\mathfrak{D}}_{\parallel}) = \widehat{XH} \frac{\partial^2 \widehat{\mathfrak{D}}_{\parallel}}{\partial \mathfrak{D}_i \cdot \partial \mathfrak{D}_j}. \quad (13.181)$$

**The  $\mathfrak{D}_{\parallel}$  Hessian**

The second partial derivatives of the unit vector  $\widehat{\mathfrak{D}}_{\parallel}$  with respect to the spherical angles are

$$\frac{\partial^2 \widehat{\mathfrak{D}}_{\parallel}}{\partial \theta^2} = \begin{pmatrix} -\sin \theta \cos \phi \\ -\sin \theta \sin \phi \\ -\cos \theta \end{pmatrix}, \quad (13.182a)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_{\parallel}}{\partial \theta \cdot \partial \phi} = \begin{pmatrix} -\cos \theta \sin \phi \\ \cos \theta \cos \phi \\ 0 \end{pmatrix}, \quad (13.182b)$$

$$\frac{\partial^2 \widehat{\mathfrak{D}}_{\parallel}}{\partial \phi^2} = \begin{pmatrix} -\sin \theta \cos \phi \\ -\sin \theta \sin \phi \\ 0 \end{pmatrix}. \quad (13.182c)$$





## Part V

# Reference



## Chapter 14

# Alphabetical listing of user functions

The following is a listing with descriptions of all the user functions available within the relax prompt and scripting environments. These are simply an alphabetical list of the docstrings which can normally be viewed in prompt mode by typing `help(function)`.

### 14.1 A warning about the formatting

The following documentation of the user functions has been automatically generated by a script which extracts and formats the docstring associated with each function. There may therefore be instances where the formatting has failed or where there are inconsistencies.

### 14.2 The list of functions

Each user function is presented within it's own subsection with the documentation broken into multiple parts: the synopsis, the default arguments, and the sections from the function's docstring.

#### 14.2.1 The synopsis

The synopsis presents a brief description of the function. It is taken as the first line of the docstring when browsing the help system.

#### 14.2.2 Defaults

This section lists all the arguments taken by the function and their default values. To invoke the function type the function name then in brackets type a comma separated list of arguments.

The first argument printed is always ‘self’ but you can safely ignore it. ‘self’ is part of the object oriented programming within Python and is automatically prefixed to the list of arguments you supply. Therefore you can’t provide ‘self’ as the first argument even if you do try.

### 14.2.3 Docstring sectioning

All other sections are created from the sectioning of the user function docstring.

## 14.2.4 align\_tensor.copy



### Synopsis

Copy alignment tensor data.

### Defaults

`align_tensor.copy(tensor_from=None, pipe_from=None, tensor_to=None, pipe_to=None)`

### Keyword arguments

**tensor\_from:** The identification string of the alignment tensor to copy the data from.

**pipe\_from:** The name of the data pipe to copy the alignment tensor data from.

**tensor\_to:** The identification string of the alignment tensor to copy the data to.

**pipe\_to:** The name of the data pipe to copy the alignment tensor data to.

### Description

This will copy the alignment tensor data to a new tensor or a new data pipe. The destination data pipe must not contain any alignment tensor data corresponding to the `tensor_to` label. If the source or destination data pipes are not supplied, then both will default to the current data pipe. Both the source and destination tensor IDs must be supplied.

### Prompt examples

To copy the alignment tensor data corresponding to 'Pf1' from the data pipe 'old' to the current data pipe, type one of:

```
relax> align_tensor.copy('Pf1', 'old')
```

```
relax> align_tensor.copy(tensor_from='Pf1',
    pipe_from='old')
```

To copy the alignment tensor data corresponding to 'Otting' from the current data pipe to the data pipe new, type one of:

```
relax> align_tensor.copy('Otting', pipe_to='
    new')
```

```
relax> align_tensor.copy(tensor_from='Otting
    ', pipe_to='new')
```

To copy the alignment tensor data of 'Otting' to that of 'Otting new', type one of:

```
relax> align_tensor.copy('Otting', tensor_to
    ='Otting new')
```

```
relax> align_tensor.copy(tensor_from='Pf1',
    tensor_to='Otting new')
```

---

### 14.2.5 `align_tensor.delete`



#### Synopsis

Delete alignment tensor data from the relax data store.

#### Defaults

`align_tensor.delete(tensor=None)`

#### Keyword arguments

**tensor:** The alignment tensor identification string.

#### Description

This will delete the specified alignment tensor data from the current data pipe. If no tensor is specified, all tensors will be deleted.

### 14.2.6 `align_tensor.display`



#### Synopsis

Display the alignment tensor information in full detail.

#### Defaults

`align_tensor.display(tensor=None)`

#### Keyword arguments

**tensor:** The alignment tensor identification string.

#### Description

This will show all information relating to the alignment tensor, including the different tensor forms:

Probability tensor.

Saupe order matrix.

Alignment tensor.

Magnetic susceptibility tensor.

All possible tensor parameters and information will also be shown (Eigensystem, GDO, Aa, Ar,  $\mathfrak{R}$ , eta, `chi_ax`, `chi_rh`, etc). The printout will be extensive.

If no tensor is specified, all tensors will be displayed.

---

### 14.2.7 align\_tensor.fix



#### Synopsis

Fix all alignment tensors so that they do not change during optimisation.

#### Defaults

**align\_tensor.fix**(id=None, fixed=True)

#### Keyword arguments

**id**: The alignment tensor identification string.

**fixed**: The flag specifying if the tensors should be fixed or variable.

#### Description

If the ID string is left unset, then all alignment tensors will be fixed.

### 14.2.8 align\_tensor.init



#### Synopsis

Initialise an alignment tensor.

#### Defaults

**align\_tensor.init**(tensor=None, align\_id=None, domain=None, params=None, scale=1.0, angle\_units='deg', param\_types=2, errors=False)

#### Keyword arguments

**tensor**: The optional alignment tensor ID string, required if multiple tensors exist per alignment.

**align\_id**: The alignment ID string that the tensor corresponds to.

**domain**: The optional domain ID string that the tensor corresponds to.

**params**: The alignment tensor data.

**scale**: The alignment tensor eigenvalue scaling value.

**angle\_units**: The units for the angle parameters.

**param\_types**: A flag to select different parameter combinations.

**errors**: A flag which determines if the alignment tensor data or its errors are being input.

#### Description

The tensor ID is only required if there are multiple unique tensors per alignment. An example is if internal domain motions cause multiple parts of the molecule to align differently. The tensor ID is optional and in the case of only a single tensor per alignment, the tensor can be identified using the alignment ID instead.

The alignment tensor parameters should be a tuple of floating point numbers (a list surrounded by round brackets). These correspond to the parameters of the tensor which can be specified by the parameter types whereby the values correspond to:

- 0** – {Sxx, Syy, Sxy, Sxz, Syz} (unitless),
- 1** – {Szz, Sxx-yy, Sxy, Sxz, Syz} (Pales default format),
- 2** – {Axx, Ayy, Axy, Axz, Ayz} (unitless),

- 3 – {Azz, Axx-yy, Axy, Axz, Ayz} (unitless),  
 4 – {Axx, Ayy, Axy, Axz, Ayz} (units of Hertz),  
 5 – {Azz, Axx-yy, Axy, Axz, Ayz} (units of Hertz),  
 6 – {Pxx, Pyy, Pxy, Pxz, Pyz} (unitless),  
 7 – {Pzz, Pxx-yy, Pxy, Pxz, Pyz} (unitless).

Other formats may be added later. The relationship between the Saupe order matrix S and the alignment tensor A is

$$S = 3/2 A.$$

The probability matrix P is related to the alignment tensor A by

$$A = P - 1/3 I,$$

where I is the identity matrix. For the alignment tensor to be supplied in Hertz, the bond vectors must all be of equal length.

## Prompt examples

To set a rhombic tensor for the domain labelled 'domain 1' with the alignment named 'super media', type one of:

```
relax> align_tensor.init('domain 1', 'super
media', (-8.6322e-05, -5.5786e-04, -3
.1732e-05, 2.2927e-05, 2.8599e-04),
param_types=1)

relax> align_tensor.init(tensor='domain 1',
align_id='super media', params=(-8
.6322e-05, -5.5786e-04, -3.1732e-05, 2
.2927e-05, 2.8599e-04), param_types=1)
```

## 14.2.9 align\_tensor.matrix\_angles



### Synopsis

Calculate the 5D angles between all alignment tensors.

### Defaults

**align\_tensor.matrix\_angles**(basis\_set=0, tensors=None)

### Keyword arguments

**basis\_set**: The basis set to operate with.

**tensors**: A list of the tensors to apply the calculation to. If None, all tensors are used.

### Description

This will calculate the angles between all loaded alignment tensors for the current data pipe. The matrices are first converted to a 5D vector form and then the angles are calculated. The angles are dependent on the basis set. If the basis set is set to the default of 0, the vectors {Sxx, Syy, Sxy, Sxz, Syz} are used. If the basis set is set to 1, the vectors {Szz, Sxxxy, Sxy, Sxz, Syz} are used instead.



---

**14.2.10 align\_tensor.reduction****Synopsis**

Specify that one tensor is a reduction of another.

**Defaults**

**align\_tensor.reduction**(full\_tensor=None, red\_tensor=None)

**Keyword arguments**

**full\_tensor**: The full alignment tensor.

**red\_tensor**: The reduced alignment tensor.

**Description**

Prior to optimisation of the N-state model and Frame Order theories using alignment tensors, which tensor is a reduction of which other tensor must be specified through this user function.

**Prompt examples**

To state that the alignment tensor loaded as 'chi3 C-dom' is a reduction of 'chi3 N-dom', type:

```
relax> align_tensor.reduction(full_tensor='
    chi3 N-dom', red_tensor='chi3 C-dom')
```

---

**14.2.11 align\_tensor.set\_domain****Synopsis**

Set the domain label for the alignment tensor.

**Defaults**

**align\_tensor.set\_domain**(tensor=None, domain=None)

**Keyword arguments**

**tensor**: The alignment tensor to assign the domain label to.

**domain**: The domain label.

**Description**

Prior to optimisation of the N-state model or Frame Order theories, the domain to which each alignment tensor belongs must be specified.

**Prompt examples**

To link the alignment tensor loaded as 'chi3 C-dom' to the C-terminal domain 'C', type:

```
relax> align_tensor.set_domain(tensor='chi3
    C-dom', domain='C')
```

### 14.2.12 align\_tensor.svd



The relationships between the geometric and unitary basis sets are:

$$\begin{aligned} S_{zz} &= -S_{xx} - S_{yy}, \\ S_{xxyy} &= S_{xx} - S_{yy}, \end{aligned}$$

#### Synopsis

Calculate the singular values and condition number for all alignment tensors.

The SVD values and condition number are dependent upon the basis set chosen.

#### Defaults

`align_tensor.svd(basis_set=0, tensors=None)`

#### Keyword arguments

**basis\_set:** The basis set to operate with.

**tensors:** A list of the tensors to apply the calculation to. If None, all tensors are used.

#### Description

This will perform a singular value decomposition of all tensors loaded for the current data pipe. If the basis set is set to the default of 0, the matrix on which SVD will be performed is composed of the unitary basis set {Sxx, Syy, Sxy, Sxz, Syz} layed out as:

|  |      |      |      |      |      |  |
|--|------|------|------|------|------|--|
|  | Sxx1 | Syy1 | Sxy1 | Sxz1 | Syz1 |  |
|  | Sxx2 | Syy2 | Sxy2 | Sxz2 | Syz2 |  |
|  | Sxx3 | Syy3 | Sxy3 | Sxz3 | Syz3 |  |
|  | .    | .    | .    | .    | .    |  |
|  | .    | .    | .    | .    | .    |  |
|  | .    | .    | .    | .    | .    |  |
|  | SxxN | SyyN | SxyN | SxzN | SyzN |  |

If **basis\_set** is set to 1, the geometric basis set consisting of the stretching and skewing parameters Szz and Sxxyy respectively {Szz, Sxxyy, Sxy, Sxz, Syz} will be used instead. The matrix is:

|  |      |        |      |      |      |  |
|--|------|--------|------|------|------|--|
|  | Szz1 | Sxxyy1 | Sxy1 | Sxz1 | Syz1 |  |
|  | Szz2 | Sxxyy2 | Sxy2 | Sxz2 | Syz2 |  |
|  | Szz3 | Sxxyy3 | Sxy3 | Sxz3 | Syz3 |  |
|  | .    | .      | .    | .    | .    |  |
|  | .    | .      | .    | .    | .    |  |
|  | .    | .      | .    | .    | .    |  |
|  | SzzN | SxxyyN | SxyN | SxzN | SyzN |  |

14.2.13 `angles.diff_frame`

## Synopsis

Calculate the angles defining the XH bond vector within the diffusion frame.

## Defaults

`angles.diff_frame()`

## Description

If the diffusion tensor is isotropic, then nothing will be done.

If the diffusion tensor is axially symmetric, then the angle  $\alpha$  will be calculated for each XH bond vector.

If the diffusion tensor is asymmetric, then the three angles will be calculated.

14.2.14 `bmr.b.citation`

## Synopsis

Specify a citation to be added the BMRB data file.

## Defaults

`bmr.b.citation(cite_id=None, authors=None, doi=None, pubmed_id=None, full_citation=None, title=None, status='published', type='journal', journal_abbrev=None, journal_full=None, volume=None, issue=None, page_first=None, page_last=None, year=None)`

## Keyword arguments

`cite_id`: The citation ID string.

`authors`: The list of authors. Each author element is a list of four elements (the first name, last name, first initial, and middle initials).

`doi`: The DOI number, e.g. '10.1000/182'.

`pubmed_id`: The identification code assigned to the publication by PubMed.

`full_citation`: The full citation as given in a reference list.

`title`: The title of the publication.

`status`: The status of the publication. This can be a value such as 'published', 'submitted', etc.

`type`: The type of publication, for example 'journal'.

`journal_abbrev`: The standard journal abbreviation.

`journal_full`: The full journal name.

`volume`: The volume number.

`issue`: The issue number.

`page_first`: The first page number.

`page_last`: The last page number.

`year`: The publication year.

## Description

The `full_citation` should be in a format similar to that used in a journal article by either cutting and pasting from another document or by typing. Please include author names, title, journal, page numbers, and year or equivalent information for the type of publication given.

The journal status can only be one of:

```
'preparation',
'in press',
'published',
'retracted',
'submitted'.
```

The citation type can only be one of:

```
'abstract',
'BMRB only',
'book',
'book chapter',
'internet',
'journal',
'personal communication',
'thesis'.
```

The standard journal abbreviation is that defined by the Chemical Abstract Services for the journal where the data are or will be published. If the data in the deposition are related to a J. Biomol. NMR paper, the value must be 'J. Biomol. NMR' to alert the BMRB annotators so that the deposition is properly processed. If the depositor truly does not know the journal, a value of 'not known' or 'na' is acceptable.

## Prompt examples

To add the citation "d'Auvergne E. J., Gooley P. R. (2007). Set theory formulation of the model-free problem and the diffusion seeded model-free paradigm. Mol. Biosyst., 3(7), 483-494.", type:

```
relax> bmrbcitation(authors=["Edward", "d'
    Auvergne", "E.", "J."], ["Paul", "
    Gooley", "P.", "R."], doi="10.1039/
    b702202f", pubmed_id="17579774",
    full_citation="d'Auvergne E. J., Gooley
    P. R. (2007). Set theory formulation
    of the model-free problem and the
    diffusion seeded model-free paradigm.
    Mol. Biosyst., 3(7), 483-494.", title="
```

```
Set theory formulation of the model-
free problem and the diffusion seeded
model-free paradigm.", status="
published", type="journal",
journal_abbrev="Mol. Biosyst.",
journal_full="Molecular Biosystems",
volume=3, issue=7, page_first=483,
page_last=498, year=2007)
```

---

### 14.2.15 `bmr.display`



#### Synopsis

Display the BMRB data in NMR-STAR format.

#### Defaults

`bmr.display(version='3.1')`

#### Keyword arguments

**version:** The version of the BMRB NMR-STAR format to display.

#### Description

This will print the BMRB NMR-STAR formatted data to STDOUT.

### 14.2.16 `bmr.read`



#### Synopsis

Read BMRB files in the NMR-STAR format.

#### Defaults

`bmr.read(file=None, dir=None, version=None, sample_conditions=None)`

#### Keyword arguments

**file:** The name of the BMRB NMR-STAR formatted file to read.

**dir:** The directory where the file is located.

**version:** The version of the BMRB NMR-STAR format to read. This is not necessary as the version is normally auto-detected.

**sample\_conditions:** The sample conditions label in the NMR-STAR file to restrict loading to.

#### Description

This will allow most of the data from a BMRB NMR-STAR formatted file to be loaded into the relax data store. Note that an empty data pipe should be created for storing the data, and that currently only model-free data pipes can be used. Also, only one sample condition can be read per relax data pipe. Therefore if one of the sample conditions is not specified and multiple conditions exist in the NMR-STAR file, an error will be raised.

### 14.2.17 bmr.script



#### Synopsis

Specify the scripts used in the analysis.

#### Defaults

**bmr.script**(file=None, dir=None, analysis\_type=None, model\_selection=None, engine='relax', model\_elim=False, universal\_solution=False)

#### Keyword arguments

**file**: The name of the script file.

**dir**: The directory where the file is located.

**analysis\_type**: The type of analysis performed.

**model\_selection**: The model selection technique used, if relevant. For example 'AIC' model selection.

**engine**: The software engine used in the analysis.

**model\_elim**: A model-free specific flag specifying if model elimination was performed.

**universal\_solution**: A model-free specific flag specifying if the universal solution was sought after.

#### Description

This user function allows scripts used in the analysis to be included in the BMRB deposition. The following addition information may need to be specified with the script.

The analysis type must be set. Allowable values include all the data pipe types used in relax, ie:

'**frame\_order**' – The Frame Order theories,

'**jw**' – Reduced spectral density mapping,

'**mf**' – Model-free analysis,

'**N-state**' – N-state model of domain motions,

'**noe**' – Steady state NOE calculation,

'**relax\_fit**' – Relaxation curve fitting,

The model selection technique only needs to be set if the script selects between different mathematical models. This can be anything, but the following are recommended:

'**AIC**' – Akaike's Information Criteria.

'**AICc**' – Small sample size corrected AIC.

'**BIC**' – Bayesian or Schwarz Information Criteria.

'**Bootstrap**' – Bootstrap model selection.

'**CV**' – Single-item-out cross-validation.

'**Expect**' – The expected overall discrepancy (the true values of the parameters are required).

'**Farrow**' – Old model-free method by Farrow et al., 1994.

'**Palmer**' – Old model-free method by Mandel et al., 1995.

'**Overall**' – The realised overall discrepancy (the true values of the parameters are required).

The engine is the software used in the calculation, optimisation, etc. This can be anything, but those recognised by relax (automatic program info, citations, etc. added) include:

'**relax**' – hence relax was used for the full analysis.

'**modelfree4**' – Art Palmer's Modelfree4 program was used for optimising the model-free parameter values.

'**dasha**' – The Dasha program was used for optimising the model-free parameter values.

'**curvefit**' – Art Palmer's curvefit program was used to determine the  $R_1$  or  $R_2$  values.

The model\_elim flag is model-free specific and should be set if the methods from "d'Auvergne, E. J. and Gooley, P. R. (2006). Model-free model elimination: A new step in the model-free dynamic analysis of NMR relaxation data. *J. Biomol. NMR*, 35(2), 117-135." were used. This should be set to True for the full\_analysis.py script.

The universal\_solution flag is model-free specific and should be set if the methods from "d'Auvergne E. J., Gooley P. R. (2007). Set theory formulation of the model-free problem and the diffusion seeded model-free paradigm. *Mol. Biosyst.*, 3(7), 483-494." were used. This should be set to True for the full\_analysis.py script.

## Prompt examples

For BMRB deposition, to specify that the `full_analysis.py` script was used, type one of:

```
relax> bmr.script('full_analysis.py', '
    model-free', 'AIC', 'relax', True, True
)
```

```
relax> bmr.script(file='full_analysis.py',
    dir=None, analysis_type='model-free',
    model_selection='AIC', engine='relax',
    model_elim=True, universal_solution=
    True)
```

## 14.2.18 bmr.script



### Synopsis

Specify the software used in the analysis.

### Defaults

`bmr.script(name=None, version=None, url=None, vendor_name=None, cite_ids=None, tasks=None)`

### Keyword arguments

`name`: The name of the software program utilised.

`version`: The version of the software, if applicable.

`url`: The web address of the software.

`vendor_name`: The name of the company or person behind the program.

`cite_ids`: A list of the BMRB citation ID numbers.

`tasks`: A list of all the tasks performed by the software.

### Description

This user function allows the software used in the analysis to be specified in full detail.

For the tasks list, this should be a python list of strings (eg. `['spectral processing']`). Although not restricted to these, the values suggested by the BMRB are:

```
'chemical shift assignment',
'chemical shift calculation',
'collection',
'data analysis',
'geometry optimization',
'peak picking',
'processing',
'refinement',
'structure solution'
```

## Prompt examples

For BMRB deposition, to say that Sparky was used in the analysis, type:

```
relax> cite_id = bmr.b.citation(authors=["
    Tom", "Goddard", "T.", "D."], ["D", "
    Kneller", "D.", "G."], title="Goddard,
    T. D. and Kneller, D. G., SPARKY 3,
    University of California, San
    Francisco.")

relax> bmr.b.software("Sparky", version="3
    .110", url="http://www.cgl.ucsf.edu/
    home/sparky/", vendor_name="Goddard, T.
    D.", cite_ids=[cite_id], tasks=["
    spectral analysis"])
```

### 14.2.19 bmr.b.software\_select



## Synopsis

Select the software used in the analysis.

## Defaults

**bmr.b.software\_select**(name=None, version=None)

## Keyword arguments

**name**: The name of the software program utilised.

**version**: The version of the software, if applicable.

## Description

Rather than specifying all the information directly, this user function allows the software packaged used in the analysis to be selected by name. The programs currently supported are:

‘NMRPipe’ – <http://spin.niddk.nih.gov/NMRPipe/>

‘Sparky’ – <http://www.cgl.ucsf.edu/home/sparky/>

More can be added if all relevant information (program name, description, website, original citation, purpose, etc.) is emailed to [relax-users@gna.org](mailto:relax-users@gna.org).

Note that relax is automatically added to the BMRB file.

## Prompt examples

For BMRB deposition, to say that both NMRPipe and Sparky were used prior to relax, type:

```
relax> bmr.b.software_select('NMRPipe')

relax> bmr.b.software_select('Sparky',
    version='3.113')
```



---

### 14.2.20 bmrbl.thiol\_state



#### Synopsis

Select the thiol state of the system.

#### Defaults

**bmrbl.thiol\_state**(state=None)

#### Keyword arguments

**state**: The thiol state.

#### Description

The thiol state can be any text, though the BMRB suggests the following:

```
'all disulfide bound',
'all free',
'all other bound',
'disulfide and other bound',
'free and disulfide bound',
'free and other bound',
'free disulfide and other bound',
'not available',
'not present',
'not reported',
'unknown'.
```

Alternatively the pure states **reduced** or **oxidised** could be specified.

#### Prompt examples

For BMRB deposition, to say that the protein studied is in the oxidised state, type one of:

```
relax> bmrbl.thiol_state('oxidised')
```

```
relax> bmrbl.thiol_state(state='oxidised')
```

### 14.2.21 bmrbl.write



#### Synopsis

Write the results to a BMRB NMR-STAR formatted file.

#### Defaults

**bmrbl.write**(file=None, dir='pipe\_name', version='3.1', force=False)

#### Keyword arguments

**file**: The name of the BMRB file to output results to. Optionally this can be a file object, or any object with a write() method.

**dir**: The directory name.

**version**: The NMR-STAR dictionary format version to create.

**force**: A flag which if True will cause the any pre-existing file to be overwritten.

#### Description

This will create a NMR-STAR formatted file of the data in the current data pipe for BMRB deposition.

In the prompt/script UI modes, to place the BMRB file in the current working directory, set dir to None. If dir is set to the special name **pipe\_name**, then the results file will be placed into a directory with the same name as the current data pipe.

---

### 14.2.22 `bruker.read`



### 14.2.23 `calc`



#### Synopsis

Read a Bruker Dynamics Center (DC) relaxation data file.

#### Synopsis

Calculate the function value.

#### Defaults

`bruker.read(ri_id=None, file=None, dir=None)`

#### Defaults

`calc(verbosity=1)`

#### Keyword arguments

`ri_id`: The relaxation data ID string. This must be a unique identifier.

`file`: The name of the Bruker Dynamics Center file containing the relaxation data.

`dir`: The directory where the file is located.

#### Keyword arguments

`verbosity`: The amount of information to print to screen. Zero corresponds to minimal output while higher values increase the amount of output. The default value is 1.

#### Description

This user function is used to load all of the data out of a Bruker Dynamics Center (DC) relaxation data file for subsequent analysis within relax. Currently the  $R_1$  and  $R_2$  relaxation rates and steady-state NOE data is supported.

#### Description

This will call the target function for the analysis type associated with the current data pipe using the current parameter values. This can be used to find, for example, the chi-squared value for different parameter values.

### 14.2.24 chemical\_shift.read

 $\delta$ 

#### Synopsis

Read chemical shifts from a file.

#### Defaults

**chemical\_shift.read**(file=None, dir=None, spin\_id\_col=None, mol\_name\_col=None, res\_num\_col=None, res\_name\_col=None, spin\_num\_col=None, spin\_name\_col=None, sep=None, spin\_id=None)

#### Keyword arguments

**file**: The name of the peak list of generic formatted file containing the chemical shifts.

**dir**: The directory where the file is located.

**spin\_id\_col**: The spin ID string column used by the generic file format (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col**: The molecule name column used by the generic file format (alternative to the spin ID column).

**res\_num\_col**: The residue number column used by the generic file format (alternative to the spin ID column).

**res\_name\_col**: The residue name column used by the generic file format (alternative to the spin ID column).

**spin\_num\_col**: The spin number column used by the generic file format (alternative to the spin ID column).

**spin\_name\_col**: The spin name column used by the generic file format (alternative to the spin ID column).

**sep**: The column separator used by the generic format (the default is white space).

**spin\_id**: The spin ID string used to restrict the loading of data to certain spin subsets.

#### Description

This will read chemical shifts from a peak list or a generic column formatted file.

#### Prompt examples

The following commands will read the chemical shifts out of the Sparky peak list `'10ms.list'`:

```
relax> chemical_shift.read('10ms.list')
```

### 14.2.25 consistency\_tests.set\_freq

 $\omega$ 

#### Synopsis

Select which relaxation data to use in the consistency tests by NMR spectrometer frequency.

#### Defaults

**consistency\_tests.set\_freq**(freq=None)

#### Keyword arguments

**freq**: The spectrometer frequency in Hz. This must match the currently loaded data to the last decimal point. See the `'sfrq'` parameter in the Varian procpa file or the `'SF01'` parameter in the Bruker acqu file.

#### Description

This will select the relaxation data to use in the consistency tests corresponding to the given frequencies. The data is selected by the spectrometer frequency in Hertz, which should be set to the exact value (see the `'sfrq'` parameter in the Varian procpa file or the `'SF01'` parameter in the Bruker acqu file). Note though that the  $R_1$ ,  $R_2$  and NOE are all expected to have the exact same frequency in the  $J(\omega)$  mapping analysis (to the last decimal point).

#### Prompt examples

```
relax> consistency_tests.set_freq(600.0 * 1e6)
```

```
relax> consistency_tests.set_freq(freq=600.0 * 1e6)
```

---

### 14.2.26 `dasha.create`



#### Synopsis

Create the Dasha script.

#### Defaults

`dasha.create`(algor='LM', dir=None, force=False)

#### Keyword arguments

**algor**: The minimisation algorithm.

**dir**: The directory to place the files.

**force**: A flag which if set to True will cause the results file to be overwritten if it already exists.

#### Description

The script file created is called '`dir/dasha_script`'.

#### Optimisation algorithms

The two minimisation algorithms within Dasha are accessible through the algorithm which can be set to:

'LM' – The Levenberg-Marquardt algorithm,

'NR' – Newton-Raphson algorithm.

For Levenberg-Marquardt minimisation, the function '`lmin`' will be called, while for Newton-Raphson, the function '`min`' will be executed.

### 14.2.27 `dasha.execute`



#### Synopsis

Perform a model-free optimisation using Dasha.

#### Defaults

`dasha.execute`(dir=None, force=False, binary='dasha')

#### Keyword arguments

**dir**: The directory to place the files.

**force**: A flag which if set to True will cause the results file to be overwritten if it already exists.

**binary**: The name of the executable Dasha program file.

#### Description

Dasha will be executed as

```
$ dasha < dasha_script | tee dasha_results
```

If you would like to use a different Dasha executable file, change the binary name to the appropriate file name. If the file is not located within the environment's path, include the full path in front of the binary file name.

---

**14.2.28** `dasha.extract`**Synopsis**

Extract data from the Dasha results file.

**Defaults**

`dasha.extract(dir=None)`

**Keyword arguments**

`dir`: The directory where the file `'dasha_results'` is found.

**Description**

The model-free results will be extracted from the Dasha results file `'dasha_results'` located in the given directory.

**14.2.29** `deselect.all`**Synopsis**

Deselect all spins in the current data pipe.

**Defaults**

`deselect.all()`

**Description**

This will deselect all spins, irregardless of their current state.

**Prompt examples**

To deselect all spins, simply type:

```
relax> deselect.all()
```

### 14.2.30 `deselect.interatom`



#### Synopsis

Deselect specific interatomic data containers.

#### Defaults

`deselect.interatom`(spin\_id1=None, spin\_id2=None, boolean='AND', change\_all=False)

#### Keyword arguments

**spin\_id1**: The spin ID string of the first spin of the interatomic data container.

**spin\_id2**: The spin ID string of the second spin of the interatomic data container.

**boolean**: The boolean operator specifying how interatomic data containers should be selected.

**change\_all**: A flag specifying if all other interatomic data containers should be changed.

#### Description

This is used to deselect specific interatomic data containers which store information about spin pairs such as RDCs, NOEs, dipole-dipole pairs involved in relaxation, etc. The 'change\_all' flag default is False meaning that all interatomic data containers currently either selected or deselected will remain that way. Setting this to True will cause all interatomic data containers not specified by the spin ID strings to be deselected.

#### Boolean operators

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

#### Prompt examples

To deselect all N-H backbone bond vectors of a protein, assuming these interatomic data containers have been already set up, type one of:

```
relax> deselect.interatom('@N', '@H')
```

```
relax> deselect.interatom(spin_id1='@N',
                          spin_id2='@H')
```

To deselect all H-H interatomic vectors of a small organic molecule, type one of:

```
relax> deselect.interatom('@H*', '@H*')
```

```
relax> deselect.interatom(spin_id1='@H*',
                          spin_id2='@H*')
```

Table 14.1: Boolean operators and their effects on selections

| Spin system or interatomic data container | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|---|---|---|---|---|---|---|---|---|
| Original selection                        | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 |
| New selection                             | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| OR  | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 |
| NOR                                       | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| AND                                       | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| NAND                                      | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| XOR                                       | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 |
| XNOR                                      | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 0 |

### 14.2.31 deselect.read



**spin\_id:** The spin ID string to restrict the loading of data to certain spin subsets.

**boolean:** The boolean operator specifying how spins should be selected.

**change\_all:** A flag specifying if all other spins should be changed.

#### Synopsis

Deselect the spins contained in a file.

#### Defaults

**deselect.read**(file=None, dir=None, spin\_id\_col=None, mol\_name\_col=None, res\_num\_col=None, res\_name\_col=None, spin\_num\_col=None, spin\_name\_col=None, sep=None, spin\_id=None, boolean='AND', change\_all=False)

#### Keyword arguments

**file:** The name of the file containing the list of spins to deselect.

**dir:** The directory where the file is located.

**spin\_id\_col:** The spin ID string column (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col:** The molecule name column (alternative to the spin\_id\_col).

**res\_num\_col:** The residue number column (alternative to the spin\_id\_col).

**res\_name\_col:** The residue name column (alternative to the spin\_id\_col).

**spin\_num\_col:** The spin number column (alternative to the spin\_id\_col).

**spin\_name\_col:** The spin name column (alternative to the spin\_id\_col).

**sep:** The column separator (the default is white space).

#### Description

The spin system can be identified in the file using two different formats. The first is the spin ID string column which can include the molecule name, the residue name and number, and the spin name and number. Alternatively the molecule name, residue number, residue name, spin number and/or spin name columns can be supplied allowing this information to be in separate columns. Note that the numbering of columns starts at one. The spin ID string can be used to restrict the reading to certain spin types, for example only <sup>15</sup>N spins when only residue information is in the file.

Empty lines and lines beginning with a hash are ignored.

The 'change all' flag default is False meaning that all spins currently either selected or deselected will remain that way. Setting this to True will cause all spins not specified in the file to be selected.

#### Boolean operators

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

#### Prompt examples

To deselect all overlapped residues listed with residue numbers in the first column of the file 'unresolved', type one of:

```
relax> deselect.read('unresolved',  
    res_num_col=1)
```

```
relax> deselect.read(file='unresolved',  
    res_num_col=1)
```

To deselect the spins in the second column of the relaxation data file 'r1.600' while selecting all other spins, for example type:

```
relax> deselect.read('r1.600', spin_num_col  
    =2, change_all=True)
```

```
relax> deselect.read(file='r1.600',  
    spin_num_col=2, change_all=True)
```

---

## 14.2.32 deselect.reverse



### Synopsis

Reversal of the spin selection for the given spins.

### Defaults

`deselect.reverse(spin_id=None)`

### Keyword arguments

`spin_id`: The spin ID string.

### Description

By supplying the spin ID string, a subset of spins can have their selection status reversed.

### Description

To deselect all currently selected spins and select those which are deselected type:

```
relax> deselect.reverse()
```



### 14.2.33 `deselect.spin`



#### Synopsis

Deselect specific spins.

#### Defaults

**deselect.spin**(spin\_id=None, boolean='AND', change\_all=False)

#### Keyword arguments

**spin\_id**: The spin ID string.

**boolean**: The boolean operator specifying how spins should be deselected.

**change\_all**: A flag specifying if all other spins should be changed.

#### Description

The 'change all' flag default is False meaning that all spins currently either selected or deselected will remain that way. Setting this to True will cause all spins not specified by the spin ID string to be deselected.

#### Boolean operators

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

#### Prompt examples

To deselect all glycines and alanines, type:

```
relax> deselect.spin(spin_id=':GLY|:ALA')
```

To deselect residue 12 MET type:

```
relax> deselect.spin(':12')
```

```
relax> deselect.spin(spin_id=':12')
```

```
relax> deselect.spin(spin_id=':12&:MET')
```

### 14.2.34 `diffusion_tensor.copy`



#### Synopsis

Copy diffusion tensor data from one data pipe to another.

#### Defaults

**diffusion\_tensor.copy**(pipe\_from=None, pipe\_to=None)

#### Keyword arguments

**pipe\_from**: The name of the data pipe to copy the diffusion tensor data from.

**pipe\_to**: The name of the data pipe to copy the diffusion tensor data to.

#### Description

This will copy the diffusion tensor data between data pipes. The destination data pipe must not contain any diffusion tensor data. If the source or destination data pipes are not supplied, then both will default to the current data pipe (hence specifying at least one is essential).

#### Prompt examples

To copy the diffusion tensor from the data pipe 'm1' to the current data pipe, type:

```
relax> diffusion_tensor.copy('m1')
```

```
relax> diffusion_tensor.copy(pipe_from='m1')
```

To copy the diffusion tensor from the current data pipe to the data pipe 'm9', type:

```
relax> diffusion_tensor.copy(pipe_to='m9')
```

To copy the diffusion tensor from the data pipe 'm1' to 'm2', type:

```
relax> diffusion_tensor.copy('m1', 'm2')
```

```
relax> diffusion_tensor.copy(pipe_from='m1',
                             pipe_to='m2')
```

---

**14.2.35 diffusion\_tensor.delete****Synopsis**

Delete the diffusion tensor data from the relax data store.

**Defaults**

`diffusion_tensor.delete()`

**Description**

This will delete all diffusion tensor data from the current data pipe.

**14.2.36 diffusion\_tensor.display****Synopsis**

Display the diffusion tensor information.

**Defaults**

`diffusion_tensor.display()`

**Description**

This will display all of the diffusion tensor information of the current data pipe.

### 14.2.37 diffusion\_tensor.init



#### Synopsis

Initialise the diffusion tensor.

#### Defaults

`diffusion_tensor.init(params=None, time_scale=1.0, d_scale=1.0, angle_units='deg', param_types=0, spheroid_type=None, fixed=True)`

#### Keyword arguments

`params`: The diffusion tensor data.

`time_scale`: The correlation time scaling value.

`d_scale`: The diffusion tensor eigenvalue scaling value.

`angle_units`: The units for the angle parameters.

`param_types`: A flag to select different parameter combinations.

`spheroid_type`: A string which, if supplied together with spheroid parameters, will restrict the tensor to either being 'oblate' or 'prolate'.

`fixed`: A flag specifying whether the diffusion tensor is fixed or can be optimised.

#### The sphere (isotropic diffusion)

When the molecule diffuses as a sphere, all three eigenvalues of the diffusion tensor are equal,  $\mathfrak{D}_x = \mathfrak{D}_y = \mathfrak{D}_z$ . In this case, the orientation of the XH bond vector within the diffusion frame is inconsequential to relaxation, hence, the spherical or Euler angles are undefined. Therefore solely a single geometric parameter, either  $\tau_m$  or  $\mathfrak{D}_{iso}$ , can fully and sufficiently parameterise the diffusion tensor. The correlation function for the global rotational diffusion is

$$C(\tau) = \frac{1}{5} e^{-\tau / \tau_m},$$

To select isotropic diffusion, the parameter should be a single floating point number. The number is the value of the isotropic global correlation time,  $\tau_m$ , in seconds. To specify the time in nanoseconds, set the time scale to 1e-9. Alternative parameters can be used by changing the 'param\_types' flag to the following integers

0 – {tm} (Default),

1 – {Diso},

where

$$1 / \tau_m = 6\mathfrak{D}_{iso}.$$

#### The spheroid (axially symmetric diffusion)

When two of the three eigenvalues of the diffusion tensor are equal, the molecule diffuses as a spheroid. Four pieces of information are required to specify this tensor, the two geometric parameters,  $\mathfrak{D}_{iso}$  and  $\mathfrak{D}_a$ , and the two orientational parameters, the polar angle  $\theta$  and the azimuthal angle  $\phi$  describing the orientation of the axis of symmetry. The correlation function of the global diffusion is

$$C(\tau) = \frac{1}{5} \sum_{i=-1}^1 \langle c_i \rangle e^{-\tau / \tau_i},$$

where

$$c_{-1} = 1/4 (3 \delta_z^2 - 1)^2,$$

$$c_0 = 3 \delta_z^2 (1 - \delta_z^2),$$

$$c_1 = 3/4 (\delta_z^2 - 1)^2,$$

and

$$1 / \tau_{-1} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a,$$

$$1 / \tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a,$$

$$1 / \tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a.$$

The direction cosine  $\delta_z$  is defined as the cosine of the angle  $\alpha$  between the XH bond vector and the unique axis of the diffusion tensor.

To select axially symmetric anisotropic diffusion, the parameters should be a tuple of floating point numbers of length four. A tuple is a type of data structure enclosed in round brackets, the elements of which are separated by commas. Alternative sets of parameters, 'param\_types', are

0 –  $\{\tau_m, \mathfrak{D}_a, \theta, \phi\}$  (Default),

1 –  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \theta, \phi\}$ ,

2 –  $\{\tau_m, \mathfrak{D}_{ratio}, \theta, \phi\}$ ,

3 –  $\{\mathfrak{D}_{\parallel}, \mathfrak{D}_{\perp}, \theta, \phi\}$ ,

4 –  $\{\mathfrak{D}_{iso}, \mathfrak{D}_{ratio}, \theta, \phi\}$ ,

$$C(\tau) = \frac{1}{5} \frac{\tau^{-2}}{\tau_i} \exp\left(-\frac{\tau}{\tau_i}\right),$$

where

$$\tau_m = 1 / 6\mathfrak{D}_{iso},$$

$$\mathfrak{D}_{iso} = 1/3 (\mathfrak{D}_{\parallel} + 2\mathfrak{D}_{\perp}),$$

$$\mathfrak{D}_a = \mathfrak{D}_{\parallel} - \mathfrak{D}_{\perp},$$

$$\mathfrak{D}_{ratio} = \mathfrak{D}_{\parallel} / \mathfrak{D}_{\perp}.$$

The spherical angles  $\{\theta, \phi\}$  orienting the unique axis of the diffusion tensor within the PDB frame are defined between

$$0 \leq \theta \leq \pi,$$

$$0 \leq \phi \leq 2\pi,$$

while the angle  $\alpha$  which is the angle between this axis and the given XH bond vector is defined between

$$0 \leq \alpha \leq 2\pi.$$

The spheroid type should be ‘oblate’, ‘prolate’, or None. This will be ignored if the diffusion tensor is not axially symmetric. If ‘oblate’ is given, then the constraint  $\mathfrak{D}_a \leq 0$  is used while if ‘prolate’ is given, then the constraint  $\mathfrak{D}_a \geq 0$  is used. If nothing is supplied, then  $\mathfrak{D}_a$  will be allowed to have any values. To prevent minimisation of diffusion tensor parameters in a space with two minima, it is recommended to specify which tensor is to be minimised, thereby partitioning the two minima into the two subspaces along the boundary  $\mathfrak{D}_a = 0$ .

## The ellipsoid (rhombic diffusion)

When all three eigenvalues of the diffusion tensor are different, the molecule diffuses as an ellipsoid. This diffusion is also known as fully anisotropic, asymmetric, or rhombic. The full tensor is specified by six pieces of information, the three geometric parameters  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_a$ , and  $\mathfrak{D}_r$  representing the isotropic, anisotropic, and rhombic components of the tensor, and the three Euler angles  $\alpha$ ,  $\beta$ , and  $\gamma$  orienting the tensor within the PDB frame. The correlation function is

where the weights on the exponentials are

$$c_2 = 1/4 (d + e),$$

$$c_1 = 3 \delta_y^2 \delta_z^2,$$

$$c_0 = 3 \delta_x^2 \delta_z^2,$$

$$c_1 = 3 \delta_x^2 \delta_y^2,$$

$$c_2 = 1/4 (d + e).$$

Let

$$\mathfrak{R} = \sqrt{1 + 3\mathfrak{D}_r},$$

then

$$d = 3 (\delta_x^4 + \delta_y^4 + \delta_z^4) - 1,$$

$$e = -1 / \mathfrak{R} ((1 + 3\mathfrak{D}_r)(\delta_x^4 + 2\delta_y^2 \delta_z^2) + (1 - 3\mathfrak{D}_r)(\delta_y^4 + 2\delta_x^2 \delta_z^2) - 2(\delta_z^4 + 2\delta_x^2 \delta_y^2)).$$

The correlation times are

$$1 / \tau_2 = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a \cdot \mathfrak{R},$$

$$1 / \tau_1 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a (1 + 3\mathfrak{D}_r),$$

$$1 / \tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a (1 - 3\mathfrak{D}_r),$$

$$1 / \tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a,$$

$$1 / \tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a \cdot \mathfrak{R}.$$

The three direction cosines  $\delta_x$ ,  $\delta_y$ , and  $\delta_z$  are the coordinates of a unit vector parallel to the XH bond vector. Hence the unit vector is  $[\delta_x, \delta_y, \delta_z]$ .

To select fully anisotropic diffusion, the parameters should be a tuple of length six. A tuple is a type of data structure enclosed in round brackets, the elements of which are separated by commas. Alternative sets of parameters, ‘param\_types’, are

0 –  $\{\tau_m, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$  (Default),

1 –  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$ ,

2 –  $\{\mathfrak{D}_x, \mathfrak{D}_y, \mathfrak{D}_z, \alpha, \beta, \gamma\}$ ,

**3** – {Dxx, Dyy, Dzz, Dxy, Dxz, Dyz},

where

$$\tau_m = 1 / 6\mathfrak{D}_{iso},$$

$$\mathfrak{D}_{iso} = 1/3 (\mathfrak{D}_x + \mathfrak{D}_y + \mathfrak{D}_z),$$

$$\mathfrak{D}_a = \mathfrak{D}_z - (\mathfrak{D}_x + \mathfrak{D}_y)/2,$$

$$\mathfrak{D}_r = (\mathfrak{D}_y - \mathfrak{D}_x)/2\mathfrak{D}_a.$$

The angles  $\alpha$ ,  $\beta$ , and  $\gamma$  are the Euler angles describing the diffusion tensor within the PDB frame. These angles are defined using the z-y-z axis rotation notation where  $\alpha$  is the initial rotation angle around the z-axis,  $\beta$  is the rotation angle around the y-axis, and  $\gamma$  is the final rotation around the z-axis again. The angles are defined between

$$0 \leq \alpha \leq 2\pi,$$

$$0 \leq \beta \leq \pi,$$

$$0 \leq \gamma \leq 2\pi.$$

Within the PDB frame, the XH bond vector is described using the spherical angles  $\theta$  and  $\phi$  where  $\theta$  is the polar angle and  $\phi$  is the azimuthal angle defined between

$$0 \leq \theta \leq \pi,$$

$$0 \leq \phi \leq 2\pi.$$

When param\_types is set to 3, then the elements of the diffusion tensor matrix defined within the PDB frame can be supplied.

## Units

The correlation time scaling value should be a floating point number. The only parameter affected by this value is  $\tau_m$ .

The diffusion tensor eigenvalue scaling value should also be a floating point number. Parameters affected by this value are  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_{\parallel}$ ,  $\mathfrak{D}_{\perp}$ ,  $\mathfrak{D}_a$ ,  $\mathfrak{D}_x$ ,  $\mathfrak{D}_y$ , and  $\mathfrak{D}_z$ . Significantly,  $\mathfrak{D}_r$  is not affected.

The units for the angle parameters should be either 'deg' or 'rad'. Parameters affected are  $\theta$ ,  $\phi$ ,  $\alpha$ ,  $\beta$ , and  $\gamma$ .

## Prompt examples

To set an isotropic diffusion tensor with a correlation time of 10 ns, type:

```
relax> diffusion_tensor.init(10e-9)
```

```
relax> diffusion_tensor.init(params=10e-9)
```

```
relax> diffusion_tensor.init(10.0, 1e-9)
```

```
relax> diffusion_tensor.init(params=10.0,
                             time_scale=1e-9, fixed=True)
```

To select axially symmetric diffusion with a  $\tau_m$  value of 8.5 ns,  $\mathfrak{D}_{ratio}$  of 1.1,  $\theta$  value of 20 degrees, and  $\phi$  value of 20 degrees, type:

```
relax> diffusion_tensor.init((8.5e-9, 1.1,
                             20.0, 20.0), param_types=2)
```

To select a spheroid diffusion tensor with a  $\mathfrak{D}_{\parallel}$  value of 1.698e7,  $\mathfrak{D}_{\perp}$  value of 1.417e7,  $\theta$  value of 67.174 degrees, and  $\phi$  value of -83.718 degrees, type one of:

```
relax> diffusion_tensor.init((1.698e7, 1
                             .417e7, 67.174, -83.718), param_types
                             =3)
```

```
relax> diffusion_tensor.init(params=(1.698e7
                                     , 1.417e7, 67.174, -83.718),
                             param_types=3)
```

```
relax> diffusion_tensor.init((1.698e-1, 1
                             .417e-1, 67.174, -83.718), param_types
                             =3, d_scale=1e8)
```

```
relax> diffusion_tensor.init(params=(1.698e
                                     -1, 1.417e-1, 67.174, -83.718),
                             param_types=3, d_scale=1e8)
```

```
relax> diffusion_tensor.init((1.698e-1, 1
                             .417e-1, 1.1724, -1.4612), param_types
                             =3, d_scale=1e8, angle_units='rad')
```

```
relax> diffusion_tensor.init(params=(1.698e
                                     -1, 1.417e-1, 1.1724, -1.4612),
                             param_types=3, d_scale=1e8, angle_units
                             ='rad', fixed=True)
```

To select ellipsoidal diffusion, type:

```
relax> diffusion_tensor.init((1.340e7, 1
                             .516e7, 1.691e7, -82.027, -80.573, 65
                             .568), param_types=2)
```

---

### 14.2.38 domain

#### Synopsis

Definition of structural domains.

#### Defaults

`domain(id=None, spin_id=None)`

#### Keyword arguments

`id`: The ID string used to identify molecular domains.

`spin_id`: The spin ID string of all atomic members of the domain.

#### Description

This is used to define structural domains. Multiple domains can be defined, and these can overlap. Rather than labelling the currently loaded spins with the ID string, the spin ID string is stored for later use. This allows new spins to be loaded later and still be included within the same domain.

### 14.2.39 dx.execute



#### Synopsis

Execute an OpenDX program.

#### Defaults

`dx.execute(file_prefix='map', dir='dx', dx_exe='dx', vp_exec=True)`

#### Keyword arguments

`file_prefix`: The file name prefix. For example if file is set to `'temp'`, then the OpenDX program `temp.net` will be loaded.

`dir`: The directory to change to for running OpenDX. If this is set to `None`, OpenDX will be run in the current directory.

`dx_exe`: The OpenDX executable file.

`vp_exec`: A flag specifying whether to execute the visual program automatically at start-up. The default of `True` causes the program to be executed.

#### Description

This will execute OpenDX to display the space maps created previously by the `dx.map` user function. This will work for any type of OpenDX map.

## 14.2.40 dx.map



### Synopsis

Create a map of the given space in OpenDX format.

### Defaults

**dx.map**(params=None, map\_type='Iso3D', spin\_id=None, inc=20, lower=None, upper=None, axis\_incs=5, file\_prefix='map', dir='dx', point=None, point\_file='point', remap=None)

### Keyword arguments

**params**: The parameters to be mapped. This should be an array of strings, the meanings of which are described below.

**map\_type**: The type of map to create. For example the default, a 3D isosurface, the type is 'Iso3D'. See below for more details.

**spin\_id**: The spin ID string.

**inc**: The number of increments to map in each dimension. This value controls the resolution of the map.

**lower**: The lower bounds of the space. If you wish to change the lower bounds of the map then supply an array of length equal to the number of parameters in the model. A lower bound for each parameter must be supplied. If nothing is supplied then the defaults will be used.

**upper**: The upper bounds of the space. If you wish to change the upper bounds of the map then supply an array of length equal to the number of parameters in the model. An upper bound for each parameter must be supplied. If nothing is supplied then the defaults will be used.

**axis\_incs**: The number of increments or ticks displaying parameter values along the axes of the OpenDX plot.

**file\_prefix**: The file name. All the output files are prefixed with this name. The main file containing the data points will be called the value of 'file'. The OpenDX program will be called 'file.net' and the OpenDX import file will be called 'file.general'.

**dir**: The directory to output files to. Set this to 'None' if you do not want the files to be placed in subdirectory. If the directory does not exist, it will be created.

**point**: An array of parameter values where a point in the map, shown as a red sphere, will be placed. The length must be equal to the number of parameters.

**point\_file**: The name of that the point output files will be prefixed with.

**remap**: A user supplied remapping function. This function will receive the parameter array and must return an array of equal length.

### Description

This will map the space corresponding to the spin identifier and create the OpenDX files. The map type can be changed to one of the following supported map types:

Please see Table 14.2 on page 312.

### Regular expression

The python function 'match', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'[]' – A sequence or set of characters to match to a single character. For example, '[sS]2' will match both 'S2' and 's2'.

'^' – Match the start of the string.

'\$' – Match the end of the string. For example, '^ [Ss]2\$' will match 's2' but not 'S2f' or 's2s'.

'.' – Match any character.

'x\*' – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.

'.\*' – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

### Diffusion tensor parameter string matching patterns

Please see Table 14.3 on page 312.

### Model-free data type string matching patterns

Please see Table 14.4 on page 312.

Table 14.2: OpenDx mapping types.

| Surface type  | Name    |
|---------------|---------|
| 3D isosurface | 'Iso3D' |

Table 14.3: Diffusion tensor parameter string matching patterns.

| Data type   | Object name | Patterns          |
|---|-------------|-------------------|
| Global correlation time - $\tau_m$  | 'tm'        | '^tm\$'           |
| Isotropic component of the diffusion tensor - $\mathfrak{D}_{iso}$  | 'Diso'      | '[Dd]iso'         |
| Anisotropic component of the diffusion tensor - $\mathfrak{D}_a$  | 'Da'        | '[Dd]a'           |
| Rhombic component of the diffusion tensor - $\mathfrak{D}_r$  | 'Dr'        | '[Dd]r\$'         |
| Eigenvalue associated with the x-axis of the diffusion tensor - $\mathfrak{D}_x$                                | 'Dx'        | '[Dd]x'           |
| Eigenvalue associated with the y-axis of the diffusion tensor - $\mathfrak{D}_y$                                | 'Dy'        | '[Dd]y'           |
| Eigenvalue associated with the z-axis of the diffusion tensor - $\mathfrak{D}_z$                                | 'Dz'        | '[Dd]z'           |
| Diffusion coefficient parallel to the major axis of the spheroid diffusion tensor - $\mathfrak{D}_{\parallel}$  | 'Dpar'      | '[Dd]par'         |
| Diffusion coefficient perpendicular to the major axis of the spheroid diffusion tensor - $\mathfrak{D}_{\perp}$ | 'Dper'      | '[Dd]per'         |
| Ratio of the parallel and perpendicular components of the spheroid diffusion tensor - $\mathfrak{D}_{ratio}$    | 'Dratio'    | '[Dd]ratio'       |
| The first Euler angle of the ellipsoid diffusion tensor - $\alpha$  | 'alpha'     | '^a\$' or 'alpha' |
| The second Euler angle of the ellipsoid diffusion tensor - $\beta$  | 'beta'      | '^b\$' or 'beta'  |
| The third Euler angle of the ellipsoid diffusion tensor - $\gamma$  | 'gamma'     | '^g\$' or 'gamma' |
| The polar angle defining the major axis of the spheroid diffusion tensor - $\theta$                             | 'theta'     | 'theta'           |
| The azimuthal angle defining the major axis of the spheroid diffusion tensor - $\phi$                           | 'phi'       | 'phi'             |

Table 14.4: Model-free data type string matching patterns.

| Data type                 | Object name |
|---------------------------|-------------|
| Local $\tau_m$            | 'local_tm'  |
| Order parameter $S^2$     | 's2'        |
| Order parameter $S_f^2$   | 's2f'       |
| Order parameter $S_s^2$   | 's2s'       |
| Correlation time $\tau_e$ | 'te'        |
| Correlation time $\tau_f$ | 'tf'        |
| Correlation time $\tau_s$ | 'ts'        |
| Chemical exchange         | 'rex'       |
| CSA                       | 'csa'       |



## Prompt examples

The following commands will generate a map of the extended model-free space for model 'm5' consisting of the parameters  $\{S^2, S_f^2, \tau_s\}$ . Files will be output into the directory 'dx' and will be prefixed by 'map'. In this case, the system is a protein and residue number 6 will be mapped.

```
relax> dx.map(['s2', 's2f', 'ts'], spin_id=':6')
```

```
relax> dx.map(['s2', 's2f', 'ts'], spin_id=':6', file_prefix='map', dir='dx')
```

```
relax> dx.map(params=['s2', 's2f', 'ts'],
             spin_id=':6', inc=20, file_prefix='map',
             dir='dx')
```

```
relax> dx.map(params=['s2', 's2f', 'ts'],
             spin_id=':6', map_type='Iso3D', inc=20,
             file_prefix='map', dir='dx')
```

To map the model-free space 'm4' for residue 2, spin N6 defined by the parameters  $\{S^2, \tau_e, R_{ex}\}$ , name the results 'test', and to place the files in the current directory, use one of the following commands:

```
relax> dx.map(['s2', 'te', 'rex'], spin_id=':2@N6', file_prefix='test', dir=None)
```

```
relax> dx.map(params=['s2', 'te', 'rex'],
             spin_id=':2@N6', inc=100, file_prefix='test',
             dir=None)
```

### 14.2.41 eliminate



#### Synopsis

Elimination or rejection of models.

#### Defaults

**eliminate**(function=None, args=None)

#### Keyword arguments

**function**: An optional user supplied function for model elimination.

**args**: A tuple of arguments used by the optional function for model elimination.

#### Description

This is used for model validation to eliminate or reject models prior to model selection. Model validation is a part of mathematical modelling whereby models are either accepted or rejected.

Empirical rules are used for model rejection and are listed below. However these can be overridden by supplying a function in the prompt and scripting modes. The function should accept five arguments, a string defining a certain parameter, the value of the parameter, the minimisation instance (ie the residue index if the model is residue specific), and the function arguments. If the model is rejected, the function should return True, otherwise it should return False. The function will be executed multiple times, once for each parameter of the model.

The function arguments should be a tuple, a list enclosed in round brackets, and will be passed to the user supplied function or the inbuilt function. For a description of the arguments accepted by the inbuilt functions, see below.

Once a model is rejected, the select flag corresponding to that model will be set to False so that model selection, or any other function, will then skip the model.

#### Local $\tau_m$ model elimination rule

The local  $\tau_m$ , in some cases, may exceed the value expected for a global correlation time. Generally the  $\tau_m$  value will be stuck at the upper limit defined for the parameter. These models are eliminated using the rule:

$$\tau_m \geq c$$

The default value of  $c$  is 50 ns, although this can be overridden by supplying the value (in seconds) as the first element of the `args` tuple.

## Internal correlation times $\tau_e$ , $\tau_f$ , $\tau_s$ model elimination rules

These parameters may experience the same problem as the local  $\tau_m$  in that the model fails and the parameter value is stuck at the upper limit. These parameters are constrained using the formula  $(\tau_e, \tau_f, \tau_s \leq 2\tau_m)$ . These failed models are eliminated using the rule:

`te, tf, ts >= c . tm.`

The default value of  $c$  is 1.5. Because of round-off errors and the constraint algorithm, setting  $c$  to 2 will result in no models being eliminated as the minimised parameters will always be less than  $2\tau_m$ . The value can be changed by supplying the value as the second element of the tuple.

## Arguments

The `'args'` argument must be a tuple of length 2, the elements of which must be numbers. For example, to eliminate models which have a local  $\tau_m$  value greater than 25 ns and models with internal correlation times greater than 1.5 times  $\tau_m$ , set `'args'` to `(25 * 1e-9, 1.5)`.

## 14.2.42 fix



## Synopsis

Fix or allow parameter values to change during optimisation.

## Defaults

`fix(element=None, fixed=True)`

## Keyword arguments

`element`: Which element to fix.

`fixed`: A flag specifying if the parameters should be fixed or allowed to change.

## Description

The element can be any of the following:

`'diff'` – The diffusion tensor parameters. This will allow all diffusion tensor parameters to be toggled.

`'all_spins'` – Using this keyword, all parameters from all spins will be toggled.

`'all'` – All parameters will be toggled. This is equivalent to combining both `'diff'` and `'all_spins'`.

The flag `'fixed'`, if set to `True`, will fix parameters during optimisation whereas a value of `False` will allow parameters to vary.

### 14.2.43 `frame_order.average_position`



#### Synopsis

Define the mechanics of the average domain position.

#### Defaults

`frame_order.average_position(pivot='com', translation=False)`

#### Keyword arguments

**pivot:** The type of pivot to use for the rotation to the average domain position. This can be one of 'com' or 'motional'.

**translation:** A flag specifying if the average domain position should be allowed to translate during optimisation. If False, then translation can be disabled.

#### Description

Prior to optimisation, the mechanics of the average moving domain position must be specified. Having the domain shifted to the correct average position is essential for understanding the dynamics as this information is the major contributor to the RDC and PCS. The motional eigenframe (spherical or Euler angles) and ordering (via order parameters, cone angles or torsion angles) come second, and are therefore severely distorted by an incorrect average domain position.

There are two pieces of information affecting this average position - a rotation and translation. For the rotation, a pivot point is required. Note that this pivot is not related to the pivot of the motions. However if you believe that your starting structure lies within the uniform distribution of positions of the domain motions, then the two pivots can be linked by setting the average position pivot to the motional pivot. The default however is to set the pivot to the centre of mass (CoM) of the moving domain.

The second option allows the average domain position to translate during optimisation. By default, only a rotation of the initial structure of the domain is rotated to the average position. But if the rotation is not sufficient to shift the domain to the average position, then a translation will be required. This option will be ignored if no PDC data is present, as RDCs do not contain information about the translation of the domain.

#### Prompt examples

To use the centre of mass as the rotational pivot and to allow translation of the average domain position during optimisation, type one of:

```
relax> frame_order.translate('com', True)
```

```
relax> frame_order.translate(translation=
    True)
```

```
relax> frame_order.translate(pivot='com',
    translation=True)
```

To use the motional pivot as the average domain rotational pivot while disallowing translation of, type one of:

```
relax> frame_order.translate('motional')
```

```
relax> frame_order.translate('motional',
    False)
```

```
relax> frame_order.translate(pivot='motional',
    translation=False)
```

---

14.2.44 `frame_order.num_int_pts`

## Synopsis

Set the number of integration points used in the quasi-random Sobol' sequence during optimisation.

## Defaults

`frame_order.num_int_pts(num=200000)`

## Keyword arguments

**num:** The number of integration points to use in the Sobol' sequence during optimisation.

## Description

This allows the number of integration points used during the Frame Order target function optimisation to be changed from the default. This is used in the quasi-random Sobol' sequence for the numerical integration.

---

14.2.45 `frame_order.pdb_model`

## Synopsis

Create a PDB file representation of the frame order dynamics.

## Defaults

`frame_order.pdb_model(ave_pos_file='ave_pos.pdb', rep_file='frame_order.pdb', dist_file='domain_distribution.pdb', dir=None, size=30.0, inc=36, force=False)`

## Keyword arguments

**ave\_pos\_file:** The name of the 3D structure PDB file for the molecular structure with the moving domains shifted to the average position.

**rep\_file:** The name of the PDB file for the geometric object representation of the frame order dynamics.

**dist\_file:** The name of the file which will contain multiple models spanning the full dynamics distribution of the frame order model.

**dir:** The directory where the file is to be located.

**size:** The size of the geometric object in Å.

**inc:** The number of increments used to create the geometric object.

**force:** A flag which, if set to True, will overwrite the any pre-existing files.

## Description

This function creates a PDB file containing an artificial geometric structure representing the Frame Order cone models.

There are four different types of residue within the PDB. The pivot point is represented as a single carbon atom of the residue 'PIV'. The cone consists of numerous H atoms of the residue 'CON'. The cone axis vector is presented as the residue 'AXE' with one carbon atom positioned at the pivot and the other  $x$  Å away on the cone axis (set by the geometric object size). Finally, if Monte Carlo have been performed, there will be multiple 'MCC' residues representing the cone for each simulation, and multiple 'MCA' residues representing the multiple cone axes.

To create the diffusion in a cone PDB representation, a uniform distribution of vectors on a sphere is generated

using spherical coordinates with the polar angle defined by the cone axis. By incrementing the polar angle using an arccos distribution, a radial array of vectors representing latitude are created while incrementing the azimuthal angle evenly creates the longitudinal vectors. These are all placed into the PDB file as H atoms and are all connected using PDB CONECT records. Each H atom is connected to its two neighbours on the both the longitude and latitude. This creates a geometric PDB object with longitudinal and latitudinal lines representing the filled cone.

---

### 14.2.46 `frame_order.pivot`



#### Synopsis

Set the pivot point for the two body motion in the structural coordinate system.

#### Defaults

`frame_order.pivot(pivot=None, fix=None)`

#### Keyword arguments

**pivot:** The pivot point for the motion (e.g. the position between the 2 domains in PDB coordinates).

**fix:** A flag specifying if the pivot point should be fixed during optimisation.

#### Description

This will set the pivot point for the two domain system within the PDB coordinate system. This is required for interpreting PCS data as well as for the generation of cone or other PDB representations of the domain motions.

#### Prompt examples

To set the pivot point, type one of:

```
relax> frame_order.pivot([12.067, 14.313, -3  
                          .2675])
```

```
relax> frame_order.pivot(pivot=[12.067, 14  
                              .313, -3.2675])
```

**14.2.47 frame\_order.quad\_int****Synopsis**

Turn the high precision quadratic integration on or off.

**Defaults**

```
frame_order.quad_int(flag=False)
```

**Keyword arguments**

**flag:** The flag with if True will perform high precision numerical integration via the `scipy.integrate.quad()`, `dblquad()` and `tplquad()` integration methods rather than the rough quasi-random numerical integration.

**Description**

This allows the high precision numerical integration of the Scipy `quad()` and related functions to be used instead of the lower precision quasi-random Sobol' sequence integration. This is for the optimisation of the Frame Order target functions. The quadratic integration is orders of magnitude slower than the Sobol' sequence integration, but the precision is much higher.

**14.2.48 frame\_order.ref\_domain****Synopsis**

Set the reference domain for the '2-domain' Frame Order theories.

**Defaults**

```
frame_order.ref_domain(ref=None)
```

**Keyword arguments**

**ref:** The domain which will act as the frame of reference. This is only valid for the '2-domain' Frame Order theories.

**Description**

Prior to optimisation of the '2-domain' Frame Order theories, which of the two domains will act as the frame of reference must be specified. This is important for the attachment of cones to domains, etc.

**Prompt examples**

To set up the isotropic cone frame order model with 'centre' domain being the frame of reference, type:

```
relax> frame_order.ref_domain(ref='centre')
```

## 14.2.49 `frame_order.select_model`



### Synopsis

Select and set up the Frame Order model.

### Defaults

`frame_order.select_model(model=None)`

### Keyword arguments

`model`: The name of the preset Frame Order model.

### Description

Prior to optimisation, the Frame Order model should be selected. These models consist of three parameter categories:

The average domain position. This includes the parameters `ave_pos_alpha`, `ave_pos_beta`, and `ave_pos_gamma`. These Euler angles rotate the tensors from the arbitrary PDB frame of the moving domain to the average domain position.

The frame order eigenframe. This includes the parameters `eigen_alpha`, `eigen_beta`, and `eigen_gamma`. These Euler angles define the major modes of motion. The cone central axis is defined as the z-axis. The pseudo-elliptic cone  $x$  and  $y$ -axes are defined as the  $x$  and  $y$ -axes of the eigenframe.

The cone parameters. These are defined as the tilt-torsion angles `cone_theta_x`, `cone_theta_y`, and `cone_sigma_max`. The `cone_theta_x` and `cone_theta_y` parameters define the two cone opening angles of the pseudo-ellipse. The amount of domain torsion is defined as the average domain position, plus and minus `cone_sigma_max`. The isotropic cones are defined by setting `cone_theta_x = cone_theta_y` and converting the single parameter into a 2<sup>nd</sup> rank order parameter.

The list of available models are:

**‘pseudo-ellipse’** – The pseudo-elliptic cone model. This is the full model consisting of the parameters `ave_pos_alpha`, `ave_pos_beta`, `ave_pos_gamma`, `eigen_alpha`, `eigen_beta`, `eigen_gamma`, `cone_theta_x`, `cone_theta_y`, and `cone_sigma_max`.

**‘pseudo-ellipse, torsionless’** – The pseudo-elliptic cone with the torsion angle `cone_sigma_max` set to zero.

**‘pseudo-ellipse, free rotor’** – The pseudo-elliptic cone with no torsion angle restriction.

**‘iso cone’** – The isotropic cone model. The cone is defined by a single order parameter `s1` which is related to the single cone opening angle `cone_theta_x = cone_theta_y`. Due to rotational symmetry about the cone axis, the average position  $\alpha$  Euler angle `ave_pos.alpha` is dropped from the model. The symmetry also collapses the eigenframe to a single z-axis defined by the parameters `axis.theta` and `axis.phi`.

**‘iso cone, torsionless’** – The isotropic cone model with the torsion angle `cone_sigma_max` set to zero.

**‘iso cone, free rotor’** – The isotropic cone model with no torsion angle restriction.

**‘line’** – The line cone model. This is the pseudo-elliptic cone with one of the cone angles, `cone_theta_y`, assumed to be statistically negligible. I.e. the cone angle is so small that it cannot be distinguished from noise.

**‘line, torsionless’** – The line cone model with the torsion angle `cone_sigma_max` set to zero.

**‘line, free rotor’** – The line cone model with no torsion angle restriction.

**‘rotor’** – The only motion is a rotation about the cone axis restricted by the torsion angle `cone_sigma_max`.

**‘rigid’** – No domain motions.

**‘free rotor’** – The only motion is free rotation about the cone axis.

### Prompt examples

To select the isotropic cone model, type:

```
relax> frame_order.select_model(model='iso
cone')
```

---

### 14.2.50 `grace.view`

*Grace*

#### Synopsis

Visualise the file within Grace.

#### Defaults

`grace.view(file=None, dir='grace', grace_exe='xmgrace')`

#### Keyword arguments

`file`: The name of the file.

`dir`: The directory name.

`grace_exe`: The Grace executable file.

#### Description

This can be used to view the specified Grace `*.agr` file by opening it with the Grace program.

#### Prompt examples

To view the file `'s2.agr'` in the directory `'grace'`, type:

```
relax> grace.view(file='s2.agr')
```

```
relax> grace.view(file='s2.agr', dir='grace'
)
```

### 14.2.51 `grace.write`

*Grace Grace*

#### Synopsis

Create a grace `'*.agr'` file to visualise the 2D data.

#### Defaults

`grace.write(x_data_type='res_num', y_data_type=None, spin_id=None, plot_data='value', file=None, dir='grace', force=False, norm=False)`

#### Keyword arguments

`x_data_type`: The data type for the X-axis (no regular expression is allowed).

`y_data_type`: The data type for the Y-axis (no regular expression is allowed).

`spin_id`: The spin ID string.

`plot_data`: The data to use for the plot.

`file`: The name of the file.

`dir`: The directory name.

`force`: A flag which, if set to True, will cause the file to be overwritten.

`norm`: A flag which, if set to True, will cause all graphs to be normalised to a starting value of 1. This is for the normalisation of series type data.

#### Description

This is designed to be as flexible as possible so that any combination of data can be plotted. The output is in the format of a Grace plot (also known as ACE/gr, Xmgr, and xmgrace) which only supports two dimensional plots. Three types of information can be used to create various types of plot. These include the x-axis and y-axis data types, the spin ID string, and the type of data plot.

The x-axis and y-axis data types should be plain strings, regular expression is not allowed. The two axes of the Grace plot can be any of the data types listed in the tables below. The only limitation is that the data must belong to the same data pipe.

If the x-axis data type is not given, the plot will default to having the residue numbering along the x-axis. Two special data types for the axes are:



**‘res\_num’** – The axis will consist of the residue numbering.

**‘spin\_num’** – The axis will consist of the spin numbering.

The spin ID string can be used to limit which spins are used in the plot. The default is that all spins will be used, however, the ID string can be used to select a subset of all spins, or a single spin for plots of Monte Carlo simulations, etc.

The property which is actually plotted can be controlled by the plot data setting. This can be one of the following:

**‘value’** – Plot values (with errors if they exist).

**‘error’** – Plot errors.

**‘sims’** – Plot the simulation values.

Normalisation is only allowed for series type data, for example the  $R_2$  exponential curves, and will be ignored for all other data types. If the norm flag is set to True then the y-value of the first point of the series will be set to 1. This normalisation is useful for highlighting errors in the data sets.

## Regular expression

The python function **‘match’**, which uses regular expression, is used to determine which data type to set values to, therefore various **data\_type** strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

**‘[]’** – A sequence or set of characters to match to a single character. For example, **‘[sS]2’** will match both **‘S2’** and **‘s2’**.

**‘^’** – Match the start of the string.

**‘\$’** – Match the end of the string. For example, **‘^[sS]2\$’** will match **‘s2’** but not **‘S2f’** or **‘s2s’**.

**‘.’** – Match any character.

**‘x\*’** – Match the character **‘x’** any number of times, for example **‘x’** will match, as will **‘xxxxx’**.

**‘.\*’** – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

## Minimisation statistic data type string matching patterns

Please see Table 14.5 on page 322.

## NOE calculation data type string matching patterns

Please see Table 14.6 on page 322.

## Relaxation dispersion curve fitting data type string matching patterns

Please see Table 14.7 on page 322.

## Relaxation curve fitting data type string matching patterns

Please see Table 14.8 on page 323.

## Reduced spectral density mapping data type string matching patterns

Please see Table 14.9 on page 323.

## Consistency testing data type string matching patterns

Please see Table 14.10 on page 323.

## Model-free data type string matching patterns

Please see Table 14.4 on page 312.

## Prompt examples

To write the NOE values for all spins to the Grace file **‘noe.agr’**, type one of:

```
relax> grace.write('res_num', 'noe', file='noe.agr')
```

```
relax> grace.write(y_data_type='noe', file='noe.agr')
```

```
relax> grace.write(x_data_type='res_num', y_data_type='noe', file='noe.agr')
```

```
relax> grace.write(y_data_type='noe', file='noe.agr', force=True)
```

Table 14.5: Minimisation statistic data type string matching patterns.

| Data type             | Object name | Patterns                               |
|-----------------------|-------------|--|
| Chi-squared statistic | 'chi2'      | '^[Cc]hi2\$' or '^[Cc]hi[-_][Ss]quare' |
| Iteration count       | 'iter'      | '^[Ii]ter'                             |
| Function call count   | 'f_count'   | '^[Ff].*[ -][Cc]ount'                  |
| Gradient call count   | 'g_count'   | '^[Gg].*[ -][Cc]ount'                  |
| Hessian call count    | 'h_count'   | '^[Hh].*[ -][Cc]ount'                  |

Table 14.6: NOE data type string matching patterns.

| Data type           | Object name |
|---------------------|-------------|
| Reference intensity | 'ref'       |
| Saturated intensity | 'sat'       |
| NOE                 | 'noe'       |

Table 14.7: Relaxation dispersion curve fitting data type string matching patterns.

| Data type   | Object name   |
|---|---------------|
| Transversal relaxation rate (rad/s)   | 'r2'          |
| Transversal relaxation rate for state A (rad/s)                                   | 'r2a'         |
| Transversal relaxation rate for state B (rad/s)                                   | 'r2b'         |
| Population of state A   | 'pA'          |
| Population of state B   | 'pB'          |
| Population of state C   | 'pC'          |
| The pA.pB.dw**2 parameter (ppm <sup>2</sup> )                                     | 'phi_ex'      |
| The pA.dw**2 parameter (ppm <sup>2</sup> )  | 'padw2'       |
| Chemical shift difference between states A and B (ppm)                            | 'dw'          |
| Chemical shift difference between states A and B for 3-site exchange (ppm)        | 'dw_AB'       |
| Chemical shift difference between states A and C for 3-site exchange (ppm)        | 'dw_AC'       |
| Chemical shift difference between states B and C for 3-site exchange (ppm)        | 'dw_BC'       |
| Proton chemical shift difference between states A and B (ppm)                     | 'dwH'         |
| Proton chemical shift difference between states A and B for 3-site exchange (ppm) | 'dwH_AB'      |
| Proton chemical shift difference between states A and C for 3-site exchange (ppm) | 'dwH_AC'      |
| Proton chemical shift difference between states B and C for 3-site exchange (ppm) | 'dwH_BC'      |
| Exchange rate (rad/s)   | 'kex'         |
| Exchange rate between sites A and B for 3-site exchange (rad/s)                   | 'kex_AB'      |
| Exchange rate between sites A and C for 3-site exchange (rad/s)                   | 'kex_AC'      |
| Exchange rate between sites B and C for 3-site exchange (rad/s)                   | 'kex_BC'      |
| Exchange rate from state A to state B (rad/s)                                     | 'k_AB'        |
| Exchange rate from state B to state A (rad/s)                                     | 'k_BA'        |
| Time of exchange (s/rad)  | 'tex'         |
| Peak intensities (series)   | 'intensities' |
| CPMG pulse train frequency (series, Hz)   | 'cpmg_frqs'   |

Table 14.8: Relaxation curve fitting data type string matching patterns.

| Data type                        | Object name   |
|----------------------------------|---------------|
| Relaxation rate                  | 'rx'          |
| Peak intensities (series)        | 'intensities' |
| Initial intensity                | 'i0'          |
| Intensity at infinity            | 'iinf'        |
| Relaxation period times (series) | 'relax_times' |

Table 14.9: Reduced spectral density mapping data type string matching patterns.

| Data type     | Object name |
|---------------|-------------|
| $J(0)$        | 'j0'        |
| $J(\omega_X)$ | 'jwx'       |
| $J(\omega_H)$ | 'jwh'       |
| CSA           | 'csa'       |

Table 14.10: Consistency testing data type string matching patterns.

| Data type          | Object name      |
|--------------------|------------------|
| $J(0)$             | 'j0'             |
| F_eta              | 'f_eta'          |
| F_R2               | 'f_r2'           |
| Bond length        | 'r'              |
| CSA                | 'csa'            |
| Heteronucleus type | 'heteronuc_type' |
| Proton type        | 'proton_type'    |
| Angle $\theta$     | 'orientation'    |
| Correlation time   | 'tc'             |

To create a Grace file of 's2' vs. 'te' for all spins, type one of:

```
relax> grace.write('s2', 'te', file='
    s2_te.agr')

relax> grace.write(x_data_type='s2',
    y_data_type='te', file='s2_te.agr')

relax> grace.write(x_data_type='s2',
    y_data_type='te', file='s2_te.agr',
    force=True)
```

To create a Grace file of the Monte Carlo simulation values of 'rex' vs. 'te' for residue 123, type one of:

```
relax> grace.write('rex', 'te', spin_id='
    :123', plot_data='sims', file='
    s2_te.agr')

relax> grace.write(x_data_type='rex',
    y_data_type='te', spin_id=':123',
    plot_data='sims', file='s2_te.agr')
```

By plotting the peak intensities, the integrity of exponential relaxation curves can be checked and anomalies searched for prior to model-free analysis or reduced spectral density mapping. For example the normalised average peak intensities can be plotted verses the relaxation time periods for the relaxation curves of all residues of a protein. The normalisation, whereby the initial peak intensity of each residue  $I(0)$  is set to 1, emphasises any problems. To produce this Grace file, type:

```
relax> grace.write(x_data_type='relax_times'
    , y_data_type='ave_int', file='
    intensities_norm.agr', force=True, norm
    =True)
```

## 14.2.52 grid\_search



### Synopsis

Perform a grid search.

### Defaults

**grid\_search**(lower=None, upper=None, inc=21, constraints=True, verbosity=1)

### Keyword arguments

**lower**: An array of the lower bound parameter values for the grid search. The length of the array should be equal to the number of parameters in the model.

**upper**: An array of the upper bound parameter values for the grid search. The length of the array should be equal to the number of parameters in the model.

**inc**: The number of increments to search over. If a single integer is given then the number of increments will be equal in all dimensions. Different numbers of increments in each direction can be set if 'inc' is set to an array of integers of length equal to the number of parameters.

**constraints**: A boolean flag specifying whether the parameters should be constrained. The default is to turn constraints on (constraints=True).

**verbosity**: The amount of information to print to screen. Zero corresponds to minimal output while higher values increase the amount of output. The default value is 1.

### Description

This will perform a grid search across the parameter space.

14.2.53 `interatom.copy`

## Synopsis

Copy all data associated with a interatomic data container.

## Defaults

`interatom.copy(pipe_from=None, pipe_to=None, spin_id1=None, spin_id2=None)`

## Keyword arguments

**pipe\_from:** The data pipe containing the interatomic data container from which the data will be copied. This defaults to the current data pipe.

**pipe\_to:** The data pipe to copy the interatomic data container to. This defaults to the current data pipe.

**spin\_id1:** The spin ID of the first spin.

**spin\_id2:** The spin ID of the first spin.

## Description

This will copy all the data associated with the identified interatomic data container to a different data pipe. The new interatomic data container must not already exist.

## Prompt examples

To copy the interatomic data container between `:20C` and `:20H`, from the `'orig'` data pipe to the current data pipe, type one of:

```
relax> interatom.copy('orig', spin_id1=':20C', spin_id2=':20H')
```

```
relax> interatom.copy(pipe_from='orig', spin_id1=':20C', spin_id2=':20H')
```

14.2.54 `interatom.define`

## Synopsis

Define interatomic interactions between pairs of spins.

## Defaults

`interatom.define(spin_id1='@N', spin_id2='@H', direct_bond=True, pipe=None)`

## Keyword arguments

**spin\_id1:** The spin ID string for the first spin of the interatomic interaction.

**spin\_id2:** The spin ID string for the second spin of the interatomic interaction.

**direct\_bond:** This is a flag which if True means that the two spins are directly bonded. This flag is useful to simplify the set up of the main heteronuclear relaxation mechanism or one-bond residual dipolar couplings.

**pipe:** The data pipe to create the interatomic data container for. This defaults to the current data pipe if not supplied.

## Description

To analyse relaxation or residual dipolar coupling (RDC) data, for example, pairs of spins which are coupled need to be defined. This can be via the magnetic dipole-dipole interaction or scalar coupling interaction. This function will create an interatomic data object connecting two existing spins. This data container will be used to store all information about the interatomic interaction including interatomic vectors and distances.

For analyses which use relaxation data, simply defining the interatomic interaction will indicate that there is a dipolar relaxation mechanism operating between the two spins. Note that for model-free analyses or reduced spectral density mapping, only a single relaxation mechanism can be handled. For RDC dependent analyses, the presence of the interatomic interaction indicates that dipolar coupling is expected between the two spins.

## Prompt examples

To connect the spins `:10N` to `:10H`, type one of:

```
relax> interatom.define(':10N', ':10H')
```

```
relax> interatom.define(spin_id1=':1@N',
    spin_id2=':1@H')
```

To define the protein  $^{15}\text{N}$  heteronuclear relaxation mechanism for a model-free analysis, type one of the following:

```
relax> interatom.define('@N', '@H', True)
```

```
relax> interatom.define(spin_id1='@N',
    spin_id2='@H', direct_bond=True)
```

---

### 14.2.55 interatom.read\_dist



#### Synopsis

Read inter-spin distances from a file.

#### Defaults

**interatom.read\_dist**(file=None, dir=None, unit='meter', spin\_id1\_col=1, spin\_id2\_col=2, data\_col=3, sep=None)

#### Keyword arguments

**file**: The name of the file containing the averaged distance data.

**dir**: The directory where the file is located.

**unit**: The unit of distance. The default is meter, but Å can also be specified.

**spin\_id1\_col**: The spin ID string column for the first spin.

**spin\_id2\_col**: The spin ID string column for the second spin.

**data\_col**: The distance data column.

**sep**: The column separator (the default is white space).

#### Description

This allows interatomic distances to be read from a file. This is useful in the case when the distances vary, avoiding having to tediously use the `interatom.set_dist` user function for each spin-pair separately. The format of the file should be columnar, with the two spin ID strings in two separate columns and the distances in any other. The default measurement unit is meter but this can be changed to Å.

For RDC and relaxation based analyses, as the magnetic dipole-dipole interaction is averaged in NMR over the interatomic distance to the inverse third power, the interatomic distances within a 3D structural file are of no use for defining the interaction. Therefore these  $r^{-3}$  average distances must be explicitly defined.

## Prompt examples

To load the distances in meters from the fifth column of the 'distances' file, and where the spin IDs are in the first and second columns, type one of the following:

```
relax> interatom.read_dist('distances', 1,
                           2, 5)
```

```
relax> interatom.read_dist(file='distances',
                           unit='meter', spin_id1_col=1,
                           spin_id2_col=2, data_col=5)
```

## 14.2.56 interatom.set\_dist



### Synopsis

Set the inter-spin distances.

### Defaults

```
interatom.set_dist(spin_id1='@N', spin_id2='@H',
ave_dist=1.0200000000000001e-10, unit='meter')
```

### Keyword arguments

**spin\_id1:** The spin identification string for the first spin of the dipole pair.

**spin\_id2:** The spin identification string for the second spin of the dipole pair.

**ave\_dist:** The  $r^{-3}$  averaged distance between the two spins to be used in the magnetic dipole constant, defaulting to meters.

**unit:** The unit of distance (the default is 'meter').

### Description

For many NMR interactions, the distance between the spin of interest and another spin or atom must be defined. This information can be extracted from a 3D structure but, in many cases, these distances are not of interest. For example the empirical or fixed distance calculation of proton positions in X-ray crystallographic structures will often not correspond to the real interatomic distances.

Another example is the magnetic dipole-dipole interaction which is averaged over the interatomic distance to the inverse third power. In this case, the interatomic distances from any 3D structural file can be of no use for defining the interaction. The average distances must be explicitly supplied. This user function allows these distances to be set up. The default measurement unit is meter but this can be changed to Å. Alternatively the distances can be read from a file using other user functions in this class.

## Prompt examples

To set the N-H distance for protein the <sup>15</sup>N heteronuclear relaxation mechanism to 1.02 Å, type one of the following:

```
relax> interatom.set_dist('@N', '@H', 1.02 *
                           1e-10)
```

```
relax> interatom.set_dist(spin_id1='@N',
    spin_id2='@H', ave_dist=1.02 * 1e-10,
    unit='meter')
```

```
relax> interatom.set_dist(spin_id1='@N',
    spin_id2='@H', ave_dist=1.02, unit='
    Angstrom')
```

---

## 14.2.57 interatom.unit\_vectors



### Synopsis

Calculate the unit vectors for all interatomic interactions.

### Defaults

**interatom.unit\_vectors**(ave=True)

### Keyword arguments

**ave**: A flag which if True will cause the bond vectors from all models to be averaged. If vectors from only one model is extracted, this will have no effect.

### Description

For an orientational dependent analysis, such as model-free analysis with the spheroidal and ellipsoidal global diffusion tensors or any analysis using RDCs, the unit vectors between the two dipoles must be calculated prior to starting the analysis. For the unit vector extraction, the two interacting spins should already possess positional information and the dipole-dipole interaction should already be defined via the `interatom.define` user function. This information will be used to calculate unit vectors between the two spins. Without positional information, no vectors can be calculated and an orientational dependent analysis will not be possible.

The number of unit vectors per interaction will be defined by the number of positions each spin possesses together with the averaging flag. If both spins have N and M positions loaded, the number of positions for both must match (N=M). In this case, as well as when one spin has N positions and the other a single position, then N unit vectors will be calculated. This is unless the averaging flag is set in which case an averaged vector of unit length will be calculated.

### Prompt examples

To calculate the unit vectors prior to a model-free analysis, type one of the following:

```
relax> interatom.unit_vectors(True)
```

```
relax> interatom.unit_vectors(ave=True)
```



---

14.2.58 `j_coupling.copy`**Synopsis**

Copy J coupling data from one data pipe to another.

**Defaults**

`j_coupling.copy(pipe_from=None, pipe_to=None)`

**Keyword arguments**

**pipe\_from:** The name of the pipe to copy the J coupling data from.

**pipe\_to:** The name of the pipe to copy the J coupling data to.

**Description**

This function will copy J coupling data from one pipe to another.

**Prompt examples**

To copy all J coupling data from pipe 'DMSO' to pipe 'CDC13', type one of:

```
relax> j_coupling.copy('DMSO', 'CDC13')
```

```
relax> j_coupling.copy(pipe_from='DMSO',  
    pipe_to='CDC13')
```

14.2.59 `j_coupling.delete`**Synopsis**

Delete the J coupling values.

**Defaults**

`j_coupling.delete()`

**Description**

This will delete all J coupling data in the current data pipe.

**Prompt examples**

To delete all J coupling data, type:

```
relax> j_coupling.delete()
```

---

### 14.2.60 j\_coupling.display



#### Synopsis

Display the J coupling data in the current data pipe.

#### Defaults

`j_coupling.display()`

#### Description

This will display all of the J coupling data in the current data pipe.

#### Prompt examples

To display all J coupling data, type:

```
relax> j_coupling.display()
```

---

### 14.2.61 j\_coupling.read



#### Synopsis

Read the J coupling data from file.

#### Defaults

`j_coupling.read(file=None, dir=None, spin_id1_col=1, spin_id2_col=2, data_col=None, error_col=None, sign_col=None, sep=None)`

#### Keyword arguments

**file:** The name of the file containing the J coupling data.

**dir:** The directory where the file is located.

**spin\_id1\_col:** The spin ID string column for the first spin.

**spin\_id2\_col:** The spin ID string column for the second spin.

**data\_col:** The J coupling data column.

**error\_col:** The experimental error column.

**sign\_col:** A special column holding the sign of the J coupling, being either 1 or -1, in case this data is obtained separately.

**sep:** The column separator (the default is white space).

#### Description

This will read J coupling data from a file. If the sign of the J coupling has been determined by a different experiment, this information can be present in a different column having either the value of 1 or -1.

#### Prompt examples

The following commands will read the J coupling data out of the file 'J.txt' where the columns are separated by the symbol ',':

```
relax> j_coupling.read('J.txt', sep=',')
```

If the individual spin J coupling errors are located in the file 'j\_err.txt' in column number 5 then, to read these values into relax, type one of:

```
relax> j_coupling.read('j_err.txt',  
    error_col=5)  
  
relax> j_coupling.read(file='j_err.txt',  
    error_col=5)
```

---

## 14.2.62 j\_coupling.write



### Synopsis

Write the J coupling data to file.

### Defaults

`j_coupling.write(file=None, dir=None, force=False)`

### Keyword arguments

`file`: The name of the file.

`dir`: The directory name.

`force`: A flag which if True will cause the file to be overwritten.

### Description

This will write the J coupling values to file. If no directory name is given, the file will be placed in the current working directory.

### 14.2.63 jw\_mapping.set\_freq

 $J(\omega)$ 
 $\omega$ 

#### Synopsis

Select which relaxation data to use in the  $J(\omega)$  mapping by NMR spectrometer frequency.

#### Defaults

`jw_mapping.set_freq(freq=None)`

#### Keyword arguments

**freq:** The spectrometer frequency in Hz. This must match the currently loaded data to the last decimal point. See the 'sfrq' parameter in the Varian procar file or the 'SF01' parameter in the Bruker acquis file.

#### Description

This will select the relaxation data to use in the reduced spectral density mapping corresponding to the given frequency. The data is selected by the spectrometer frequency in Hertz, which should be set to the exact value (see the 'sfrq' parameter in the Varian procar file or the 'SF01' parameter in the Bruker acquis file). Note though that the  $R_1$ ,  $R_2$  and NOE are all expected to have the exact same frequency in the  $J(\omega)$  mapping analysis (to the last decimal point).

#### Prompt examples

```
relax> jw_mapping.set_freq(600.0 * 1e6)
```

```
relax> jw_mapping.set_freq(freq=600.0 * 1e6)
```

### 14.2.64 minimise



#### Synopsis

Perform an optimisation.

#### Defaults

`minimise(min_algor='newton', line_search=None, hessian_mod=None, hessian_type=None, func_tol=1e-25, grad_tol=None, max_iter=10000000, constraints=True, scaling=True, verbosity=1)`

#### Keyword arguments

**min\_algor:** The optimisation algorithm to use.

**line\_search:** The line search algorithm which will only be used in combination with the line search and conjugate gradient methods. This will default to the More and Thiente line search.

**hessian\_mod:** The Hessian modification. This will only be used in the algorithms which use the Hessian, and defaults to Gill, Murray, and Wright modified Cholesky algorithm.

**hessian\_type:** The Hessian type. This will only be used in a few trust region algorithms, and defaults to BFGS.

**func\_tol:** The function tolerance. This is used to terminate minimisation once the function value between iterations is less than the tolerance. The default value is 1e-25.

**grad\_tol:** The gradient tolerance. Minimisation is terminated if the current gradient value is less than the tolerance. The default value is None.

**max\_iter:** The maximum number of iterations. The default value is 1e7.

**constraints:** A boolean flag specifying whether the parameters should be constrained. The default is to turn constraints on (constraints=True).

**scaling:** The diagonal scaling boolean flag. The default that scaling is on (scaling=True).

**verbosity:** The amount of information to print to screen. Zero corresponds to minimal output while higher values increase the amount of output. The default value is 1.

## Description

This will perform an optimisation starting from the current parameter values. This is only suitable for data pipe types which have target functions and hence support optimisation.

## Diagonal scaling

Diagonal scaling is the transformation of parameter values such that each value has a similar order of magnitude. Certain minimisation techniques, for example the trust region methods, perform extremely poorly with badly scaled problems. In addition, methods which are insensitive to scaling such as Newton minimisation may still benefit due to the minimisation of round off errors.

In Model-free analysis for example, if  $S^2 = 0.5$ ,  $\tau_e = 200$  ps, and  $R_{ex} = 15$  1/s at 600 MHz, the unscaled parameter vector would be [0.5, 2.0e-10, 1.055e-18].  $R_{ex}$  is divided by  $(2 * \pi * 600,000,000)**2$  to make it field strength independent. The scaling vector for this model may be something like [1.0, 1e-9, 1/(2 \*  $\pi$  \* 6e8)\*\*2]. By dividing the unscaled parameter vector by the scaling vector the scaled parameter vector is [0.5, 0.2, 15.0]. To revert to the original unscaled parameter vector, the scaled parameter vector and scaling vector are multiplied.

## Minimisation algorithms

A minimisation function is selected if the minimisation algorithm matches a certain pattern. Because the python regular expression 'match' statement is used, various strings can be supplied to select the same minimisation algorithm. Below is a list of the minimisation algorithms available together with the corresponding patterns.

This is a short description of python regular expression, for more information, see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

- '[]' – A sequence or set of characters to match to a single character. For example, '[Nn]ewton' will match both 'Newton' and 'newton'.
- '^' – Match the start of the string.
- '\$' – Match the end of the string. For example, '^ [Ll] [Mm] \$' will match 'lm' and 'LM' but will not match if characters are placed either before or after these strings.

To select a minimisation algorithm, use a string which matches one of the following patterns given in the tables.

Unconstrained line search methods:

Please see Table 14.11 on page 334.

Unconstrained trust-region methods:

Please see Table 14.12 on page 334.

Unconstrained conjugate gradient methods:

Please see Table 14.13 on page 334.

Miscellaneous unconstrained methods:

Please see Table 14.14 on page 334.

Global minimisation methods:

Please see Table 14.15 on page 334.

## Minimisation options

The minimisation options can be given in any order.

Line search algorithms. These are used in the line search methods and the conjugate gradient methods. The default is the Backtracking line search. The algorithms are:

Please see Table 14.16 on page 335.

Hessian modifications. These are used in the Newton, Dogleg, and Exact trust region algorithms:

Please see Table 14.17 on page 335.

Hessian type, these are used in a few of the trust region methods including the Dogleg and Exact trust region algorithms. In these cases, when the Hessian type is set to Newton, a Hessian modification can also be supplied as above. The default Hessian type is Newton, and the default Hessian modification when Newton is selected is the GMW algorithm:

Please see Table 14.18 on page 335.

For Newton minimisation, the default line search algorithm is the More and Thuente line search, while the default Hessian modification is the GMW algorithm.

## Prompt examples

To apply Newton minimisation together with the GMW81 Hessian modification algorithm, the More and Thuente line search algorithm, a function tolerance of 1e-25, no gradient tolerance, a maximum of 10,000,000 iterations, constraints turned on to limit parameter values, and have normal printout, type any combination of:

```
relax> minimise('newton')
relax> minimise('Newton')
relax> minimise('newton', 'gmw')
relax> minimise('newton', 'mt')
relax> minimise('newton', 'gmw', 'mt')
relax> minimise('newton', 'mt', 'gmw')
relax> minimise('newton', func_tol=1e-25)
```

Table 14.11: Minimisation algorithms – unconstrained line search methods.

| Minimisation algorithm            | Patterns   |
|-----------------------------------|--|
| Back-and-forth coordinate descent | <code>'^[Cc][Dd]'</code> or <code>'^[Cc]oordinate[-][Dd]escent\$'</code> |
| Steepest descent                  | <code>'^[Ss][Dd]'</code> or <code>'^[Ss]teepest[-][Dd]escent\$'</code>   |
| Quasi-Newton BFGS                 | <code>'^[Bb][Ff][Gg][Ss]'</code>   |
| Newton                            | <code>'^[Nn]ewton\$'</code>  |
| Newton-CG                         | <code>'^[Nn]ewton[-][Cc][Gg]'</code> or <code>'^[Nn][Cc][Gg]'</code>     |

Table 14.12: Minimisation algorithms – unconstrained trust-region methods.

| Minimisation algorithm | Patterns  |
|------------------------|---|
| Cauchy point           | <code>'^[Cc]auchy'</code>   |
| Dogleg                 | <code>'^[Dd]ogleg'</code>   |
| CG-Steihaug            | <code>'^[Cc][Gg][-][Ss]teihaug'</code> or <code>'^[Ss]teihaug'</code> |
| Exact trust region     | <code>'^[Ee]xact'</code>  |

Table 14.13: Minimisation algorithms – unconstrained conjugate gradient methods.

| Minimisation algorithm | Patterns  |
|------------------------|---|
| Fletcher-Reeves        | <code>'^[Ff][Rr]'</code> or <code>'^[Ff]letcher[-][Rr]eeves\$'</code>     |
| Polak-Ribiere          | <code>'^[Pp][Rr]'</code> or <code>'^[Pp]olak[-][Rr]ibiere\$'</code>       |
| Polak-Ribière +        | <code>'^[Pp][Rr]\+\$'</code> or <code>'^[Pp]olak[-][Rr]ibiere\+\$'</code> |
| Hestenes-Stiefel       | <code>'^[Hh][Ss]'</code> or <code>'^[Hh]estenes[-][Ss]tiefel\$'</code>    |

Table 14.14: Minimisation algorithms – miscellaneous unconstrained methods.

| Minimisation algorithm | Patterns  |
|------------------------|---|
| Simplex                | <code>'^[Ss]implex\$'</code>  |
| Levenberg-Marquardt    | <code>'^[Ll][Mm]'</code> or <code>'^[Ll]evenburg-[Mm]arquardt\$'</code> |

Table 14.15: Minimisation algorithms – global minimisation methods.

| Minimisation algorithm | Patterns  |
|------------------------|---|
| Simulated Annealing    | <code>'^[Ss][Aa]'</code> or <code>'^[Ss]imulated [Aa]nnealing\$'</code> |

Table 14.16: Minimisation sub-algorithms – line search algorithms.

| Line search algorithm                                   | Patterns  |
|---|---|
| Backtracking line search                                | <code>^[Bb]ack'</code>  |
| Nocedal and Wright interpolation based line search      | <code>^[Nn][Ww][Ii]' or '^[Nn]ocedal[ _][Ww]right[ _][Ii]nt'</code>   |
| Nocedal and Wright line search for the Wolfe conditions | <code>^[Nn][Ww][Ww]' or '^[Nn]ocedal[ _][Ww]right[ _][Ww]olfe'</code> |
| More and Thuente line search                            | <code>^[Mm][Tt]' or '^[Mm]ore[ _][Tt]huyente\$'</code>                |
| No line search  | <code>^[Nn]o [Ll]ine [Ss]earch\$'</code>                              |

Table 14.17: Minimisation sub-algorithms – Hessian modifications.

| Hessian modification                                     | Patterns                               |
|--|--|
| Unmodified Hessian                                       | <code>^[Nn]o [Hh]essian [Mm]od'</code> |
| Eigenvalue modification                                  | <code>^[Ee]igen'</code>                |
| Cholesky with added multiple of the identity             | <code>^[Cc]hol'</code>                 |
| The Gill, Murray, and Wright modified Cholesky algorithm | <code>^[Gg][Mm][Ww]\$'</code>          |
| The Schnabel and Eskow 1999 algorithm                    | <code>^[Ss][Ee]99'</code>              |

Table 14.18: Minimisation sub-algorithms – Hessian type.

| Hessian type      | Patterns                          |
|-------------------|-----------------------------------|
| Quasi-Newton BFGS | <code>^[Bb][Ff][Gg][Ss]\$'</code> |
| Newton            | <code>^[Nn]ewton\$'</code>        |

```
relax> minimise('newton', func_tol=1e-25,
               grad_tol=None)
```

```
relax> minimise('newton', max_iter=1e7)
```

```
relax> minimise('newton', constraints=True,
               max_iter=1e7)
```

```
relax> minimise('newton', verbosity=1)
```

To use constrained Simplex minimisation with a maximum of 5000 iterations, type:

```
relax> minimise('simplex', constraints=True,
               max_iter=5000)
```

---

## 14.2.65 model\_free.create\_model

 $S_e^2, \tau_e$ 


### Synopsis

Create a model-free model.

### Defaults

**model\_free.create\_model**(model=None, equation=None, params=None, spin\_id=None)

### Keyword arguments

**model**: The new name of the model-free model.

**equation**: The model-free equation.

**params**: The array of parameter names of the model.

**spin\_id**: The spin identification string.

### Description

This user function should almost never be used. It is provided for academic reasons for the study of old analyses and published results. If you are looking for a normal model-free model, use the `model_free.select_model` user function instead.

### Model-free equation

The model-free equation can be one of the following:

**'mf\_orig'** selects the original model-free equations with parameters  $\{S^2, \tau_e\}$ .

**'mf\_ext'** selects the extended model-free equations with parameters  $\{S_f^2, \tau_f, S^2, \tau_s\}$ .

**'mf\_ext2'** selects the extended model-free equations with parameters  $\{S_f^2, \tau_f, S_s^2, \tau_s\}$ .

### Model-free parameters

The following parameters are accepted for the original model-free equation:

**'s2'** – The square of the generalised order parameter.



‘te’ – The effective correlation time.

The following parameters are accepted for the extended model-free equation:

‘s2f’ – The square of the generalised order parameter of the faster motion.

‘tf’ – The effective correlation time of the faster motion.

‘s2’ – The square of the generalised order parameter  $S^2 = S_f^2 * S_s^2$ .

‘ts’ – The effective correlation time of the slower motion.

The following parameters are accepted for the extended 2 model-free equation:

‘s2f’ – The square of the generalised order parameter of the faster motion.

‘tf’ – The effective correlation time of the faster motion.

‘s2s’ – The square of the generalised order parameter of the slower motion.

‘ts’ – The effective correlation time of the slower motion.

The following parameters are accepted for all equations:

‘rex’ – The chemical exchange relaxation.

‘r’ – The average bond length  $\langle r \rangle$ .

‘csa’ – The chemical shift anisotropy.

The following commands will create the model-free model ‘large\_model’ which is based on the extended model-free equation and contains the seven parameters ‘s2f’, ‘tf’, ‘s2’, ‘ts’, ‘rex’, ‘csa’, ‘r’.

```
relax> model_free.create_model('large_model'
    , 'mf_ext', ['s2f', 'tf', 's2', 'ts', '
    rex', 'csa', 'r'])
```

```
relax> model_free.create_model(model='
    large_model', params=['s2f', 'tf', 's2'
    , 'ts', 'rex', 'csa', 'r'], equation='
    mf_ext')
```

## Spin identification string

If ‘spin\_id’ is supplied then the model will only be created for the corresponding spins. Otherwise the model will be created for all spins.

## Prompt examples

The following commands will create the model-free model ‘m1’ which is based on the original model-free equation and contains the single parameter ‘s2’.

```
relax> model_free.create_model('m1', '
    mf_orig', ['s2'])
```

```
relax> model_free.create_model(model='m1',
    params=['s2'], equation='mf_orig')
```

---

**14.2.66    `model_free.delete`** $S^2\tau_e$ **Synopsis**

Delete all model-free data from the current data pipe.

**Defaults**

`model_free.delete()`

**Description**

This will delete all of the model-free data - parameters, model, etc. - from the current data pipe.

**Prompt examples**

To delete all model-free data, type:

```
relax> model_free.delete()
```

---

**14.2.67    `model_free.remove_tm`** $S^2\tau_e$ **Synopsis**

Remove the local  $\tau_m$  parameter from a model.

**Defaults**

`model_free.remove_tm(spin_id=None)`

**Keyword arguments**

`spin_id`: The spin identification string.

**Description**

This function will remove the local  $\tau_m$  parameter from the model-free parameter set. If there is no local  $\tau_m$  parameter within the set nothing will happen.

If no spin identification string is given, then the function will apply to all spins.

**Prompt examples**

The following command will remove the parameter 'tm':

```
relax> model_free.remove_tm()
```

## 14.2.68 `model_free.select_model`

 $S_e^2, \tau_e$ 


### Synopsis

Select a preset model-free model.

### Defaults

`model_free.select_model(model=None, spin_id=None)`

'm11' – {CSA,  $S^2$ },

'm12' – {CSA,  $S^2$ ,  $\tau_e$ },

'm13' – {CSA,  $S^2$ ,  $R_{ex}$ },

'm14' – {CSA,  $S^2$ ,  $\tau_e$ ,  $R_{ex}$ },

'm15' – {CSA,  $S_f^2$ ,  $S^2$ ,  $\tau_s$ },

'm16' – {CSA,  $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ },

'm17' – {CSA,  $S_f^2$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm18' – {CSA,  $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm19' – {CSA,  $R_{ex}$ }.

### Keyword arguments

`model`: The name of the preset model.

`spin_id`: The spin identification string.

### Description

This allows a standard model-free model to be selected from a long list of models.

### The preset models

The standard preset model-free models are

'm0' – {},

'm1' – {S2},

'm2' – { $S^2$ ,  $\tau_e$ },

'm3' – { $S^2$ ,  $R_{ex}$ },

'm4' – { $S^2$ ,  $\tau_e$ ,  $R_{ex}$ },

'm5' – { $S_f^2$ ,  $S^2$ ,  $\tau_s$ },

'm6' – { $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ },

'm7' – { $S_f^2$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm8' – { $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm9' – {Rex}.

'm20' – {r},

'm21' – {r,  $S^2$ },

'm22' – {r,  $S^2$ ,  $\tau_e$ },

'm23' – {r,  $S^2$ ,  $R_{ex}$ },

'm24' – {r,  $S^2$ ,  $\tau_e$ ,  $R_{ex}$ },

'm25' – {r,  $S_f^2$ ,  $S^2$ ,  $\tau_s$ },

'm26' – {r,  $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ },

'm27' – {r,  $S_f^2$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm28' – {r,  $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm29' – {r, CSA,  $R_{ex}$ }.

The preset model-free models with both optimisation of the bond length and CSA are

'm30' – {r, CSA},

'm31' – {r, CSA,  $S^2$ },

'm32' – {r, CSA,  $S^2$ ,  $\tau_e$ },

'm33' – {r, CSA,  $S^2$ ,  $R_{ex}$ },

'm34' – {r, CSA,  $S^2$ ,  $\tau_e$ ,  $R_{ex}$ },

'm35' – {r, CSA,  $S_f^2$ ,  $S^2$ ,  $\tau_s$ },

'm36' – {r, CSA,  $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ },

'm37' – {r, CSA,  $S_f^2$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm38' – {r, CSA,  $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ },

'm39' – {r, CSA,  $R_{ex}$ }.

The preset model-free models with optimisation of the CSA value are

'm10' – {CSA},

Warning: The models in the thirties range fail when using standard R<sub>1</sub>, R<sub>2</sub>, and NOE relaxation data. This is due to the extreme flexibility of these models where a change in the parameter 'r' is compensated by a corresponding change in the parameter 'csa' and vice versa.

## The preset local tm models

Additional preset model-free models, which are simply extensions of the above models with the addition of a local  $\tau_m$  parameter are:

‘tm0’ –  $\{\tau_m\}$ ,  
 ‘tm1’ –  $\{\tau_m, S^2\}$ ,  
 ‘tm2’ –  $\{\tau_m, S^2, \tau_e\}$ ,  
 ‘tm3’ –  $\{\tau_m, S^2, R_{ex}\}$ ,  
 ‘tm4’ –  $\{\tau_m, S^2, \tau_e, R_{ex}\}$ ,  
 ‘tm5’ –  $\{\tau_m, S_f^2, S^2, \tau_s\}$ ,  
 ‘tm6’ –  $\{\tau_m, S_f^2, \tau_f, S^2, \tau_s\}$ ,  
 ‘tm7’ –  $\{\tau_m, S_f^2, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm8’ –  $\{\tau_m, S_f^2, \tau_f, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm9’ –  $\{\tau_m, R_{ex}\}$ .

The preset model-free models with optimisation of the CSA value are

‘tm10’ –  $\{\tau_m, CSA\}$ ,  
 ‘tm11’ –  $\{\tau_m, CSA, S^2\}$ ,  
 ‘tm12’ –  $\{\tau_m, CSA, S^2, \tau_e\}$ ,  
 ‘tm13’ –  $\{\tau_m, CSA, S^2, R_{ex}\}$ ,  
 ‘tm14’ –  $\{\tau_m, CSA, S^2, \tau_e, R_{ex}\}$ ,  
 ‘tm15’ –  $\{\tau_m, CSA, S_f^2, S^2, \tau_s\}$ ,  
 ‘tm16’ –  $\{\tau_m, CSA, S_f^2, \tau_f, S^2, \tau_s\}$ ,  
 ‘tm17’ –  $\{\tau_m, CSA, S_f^2, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm18’ –  $\{\tau_m, CSA, S_f^2, \tau_f, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm19’ –  $\{\tau_m, CSA, R_{ex}\}$ .

The preset model-free models with optimisation of the bond length are

‘tm20’ –  $\{\tau_m, r\}$ ,  
 ‘tm21’ –  $\{\tau_m, r, S^2\}$ ,  
 ‘tm22’ –  $\{\tau_m, r, S^2, \tau_e\}$ ,  
 ‘tm23’ –  $\{\tau_m, r, S^2, R_{ex}\}$ ,  
 ‘tm24’ –  $\{\tau_m, r, S^2, \tau_e, R_{ex}\}$ ,  
 ‘tm25’ –  $\{\tau_m, r, S_f^2, S^2, \tau_s\}$ ,

‘tm26’ –  $\{\tau_m, r, S_f^2, \tau_f, S^2, \tau_s\}$ ,  
 ‘tm27’ –  $\{\tau_m, r, S_f^2, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm28’ –  $\{\tau_m, r, S_f^2, \tau_f, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm29’ –  $\{\tau_m, r, CSA, R_{ex}\}$ .

The preset model-free models with both optimisation of the bond length and CSA are

‘tm30’ –  $\{\tau_m, r, CSA\}$ ,  
 ‘tm31’ –  $\{\tau_m, r, CSA, S^2\}$ ,  
 ‘tm32’ –  $\{\tau_m, r, CSA, S^2, \tau_e\}$ ,  
 ‘tm33’ –  $\{\tau_m, r, CSA, S^2, R_{ex}\}$ ,  
 ‘tm34’ –  $\{\tau_m, r, CSA, S^2, \tau_e, R_{ex}\}$ ,  
 ‘tm35’ –  $\{\tau_m, r, CSA, S_f^2, S^2, \tau_s\}$ ,  
 ‘tm36’ –  $\{\tau_m, r, CSA, S_f^2, \tau_f, S^2, \tau_s\}$ ,  
 ‘tm37’ –  $\{\tau_m, r, CSA, S_f^2, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm38’ –  $\{\tau_m, r, CSA, S_f^2, \tau_f, S^2, \tau_s, R_{ex}\}$ ,  
 ‘tm39’ –  $\{\tau_m, r, CSA, R_{ex}\}$ .

## Spin identification string

If ‘spin\_id’ is supplied then the model will only be selected for the corresponding spins. Otherwise the model will be selected for all spins.

## Prompt examples

To pick model ‘m1’ for all selected spins, type:

```
relax> model_free.select_model('m1')

relax> model_free.select_model(model='m1')
```

### 14.2.69 model\_selection



## Synopsis

Select the best model from a set of optimised models.

## Defaults

```
model_selection(method='AIC', model_pipe=None,  
bundle=None, pipes=None)
```

## Keyword arguments

method: The model selection technique (see below).

**model\_pipe:** The name of the new data pipe which will be created by this user function by the copying of the selected data pipe.

**bundle:** The optional pipe bundle is a special grouping or clustering of data pipes. If this is specified, the newly created data pipe will be added to this bundle.

**pipes:** An array containing the names of all data pipes to include in model selection.

## Description

The following model selection methods are supported:

**AIC** – Akaike’s Information Criteria.

**AICc** – Small sample size corrected AIC.

**BIC** – Bayesian or Schwarz Information Criteria.

**Bootstrap** – Bootstrap model selection.

**CV** – Single-item-out cross-validation.

**Expect** – The expected overall discrepancy (the true values of the parameters are required).

**Farrow** – Old model-free method by Farrow et al., 1994.

**Palmer** – Old model-free method by Mandel et al., 1995.

**Overall** – The realised overall discrepancy (the true values of the parameters are required).

For the methods ‘**Bootstrap**’, ‘**Expect**’, and ‘**Overall**’, the Monte Carlo simulations should have previously been executed with the `monte_carlo.create_data` method set to `Bootstrapping` to modify its behaviour.

If the data pipes have not been specified, then all data pipes will be used for model selection.

## Prompt examples

For model-free analysis, if the preset models 1 to 5 are minimised and loaded into the program, the following commands will carry out AIC model selection and to place the selected results into the 'mixed' data pipe, type one of:

```
relax> model_selection('AIC', 'mixed')
```

```
relax> model_selection(method='AIC',
  modsel_pipe='mixed')
```

```
relax> model_selection('AIC', 'mixed', ['m1'
    , 'm2', 'm3', 'm4', 'm5'])
```

```
relax> model_selection(method='AIC',
  modsel_pipe='mixed', pipes=['m1', 'm2',
    'm3', 'm4', 'm5'])
```

### 14.2.70 molecule.copy



#### Synopsis

Copy all data associated with a molecule.

#### Defaults

```
molecule.copy(pipe_from=None, mol_from=None,
               pipe_to=None, mol_to=None)
```

#### Keyword arguments

**pipe\_from:** The data pipe containing the molecule from which the data will be copied. This defaults to the current data pipe.

**mol\_from:** The name of the molecule from which to copy data from.

**pipe\_to:** The data pipe to copy the data to. This defaults to the current data pipe.

**mol\_to:** The name of the new molecule. If left blank, the new molecule will have the same name as the old. This needs to be a molecule ID string, starting with '#'.

#### Description

This will copy all the data associated with a molecule to a second molecule. This includes all residue and spin system information. The new molecule name must be unique in the destination data pipe.

#### Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is '**#<mol\_name> :<res\_id>[, <res\_id>[, <res\_id>, ...]] @<atom\_id>[, <atom\_id>[, <atom\_id>, ...]]'**', where the token elements are '**<mol\_name>**', the name of the molecule, '**<res\_id>**', the residue identifier which can be a number, name, or range of numbers, '**<atom\_id>**', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

#### Prompt examples

To copy the molecule data from the molecule 'GST' to the new molecule 'wt-GST', type:

```
relax> molecule.copy('#GST', '#wt-GST')
```

```
relax> molecule.copy(mol_from='#GST', mol_to=
                    '#wt-GST')
```

To copy the molecule data of the molecule 'Ap4Aase' from the data pipe 'm1' to 'm2', assuming the current data pipe is 'm1', type:

```
relax> molecule.copy(mol_from='#ApAase',
                    pipe_to='m2')
```

```
relax> molecule.copy(pipe_from='m1',
                    mol_from='#ApAase', pipe_to='m2',
                    mol_to='#ApAase')
```

---

14.2.71 molecule.create

## Synopsis

Create a new molecule.

## Defaults

`molecule.create(mol_name=None, mol_type=None)`

## Keyword arguments

`mol_name`: The name of the new molecule.

`mol_type`: The type of molecule.

## Description

This adds a new molecule data container to the relax data storage object. The same molecule name cannot be used more than once. The molecule type need not be specified. However, if given, it should be one of 'protein', 'DNA', 'RNA', 'organic molecule', or 'inorganic molecule'.

## Prompt examples

To create the molecules 'Ap4Aase', 'ATP', and 'MgF4', type:

```
relax> molecule.create('Ap4Aase')
```

```
relax> molecule.create('ATP')
```

```
relax> molecule.create('MgF4')
```

---

14.2.72 molecule.delete

## Synopsis

Deleting molecules from the relax data store.

## Defaults

`molecule.delete(mol_id=None)`

## Keyword arguments

`mol_id`: The molecule ID string.

## Description

This can be used to delete a single or sets of molecules from the relax data store. The molecule will be deleted from the current data pipe.

## Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is '#<mol\_name> :<res\_id>[, <res\_id>[, <res\_id>, ...]] @<atom\_id>[, <atom\_id>[, <atom\_id>, ...]]', where the token elements are '<mol\_name>', the name of the molecule, '<res\_id>', the residue identifier which can be a number, name, or range of numbers, '<atom\_id>', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

## 14.2.73 molecule.display



## Synopsis

Display the molecule information.

## Defaults

`molecule.display(mol_id=None)`

## Keyword arguments

`mol_id`: The molecule ID string.

## Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

## 14.2.74 molecule.name



## Synopsis

Name a molecule.

## Defaults

`molecule.name(mol_id=None, name=None, force=False)`

## Keyword arguments

`mol_id`: The molecule ID string corresponding to one or more molecules.

`name`: The new molecule name.

`force`: A flag which if True will cause the molecule to be renamed.

## Description

This simply allows molecules to be named (or renamed).

## Prompt examples

To rename the molecule 'Ap4Aase' to 'Inhib Ap4Aase', type one of:

```
relax> molecule.name('#Ap4Aase', 'Inhib
Ap4Aase', True)
```

```
relax> molecule.name(mol_id='#Ap4Aase', name
='Inhib Ap4Aase', force=True)
```

This assumes the molecule 'Ap4Aase' already exists.

## Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`.



...]] @<atom\_id>[, <atom\_id>[, <atom\_id>, ...]]', where the token elements are '<mol\_name>', the name of the molecule, '<res\_id>', the residue identifier which can be a number, name, or range of numbers, '<atom\_id>', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

---

## 14.2.75 molecule.type



### Synopsis

Set the molecule type.

### Defaults

**molecule.type**(mol\_id=None, type=None, force=False)

### Keyword arguments

**mol\_id**: The molecule ID string corresponding to one or more molecules.

**type**: The molecule type.

**force**: A flag which if True will cause the molecule to type to be overwritten.

### Description

This allows the type of the molecule to be specified. It can be one of:

```
'protein',  
'DNA',  
'RNA',  
'organic molecule',  
'inorganic molecule'.
```

### Prompt examples

To set the molecule 'Ap4Aase' to the 'protein' type, type one of:

```
relax> molecule.type('#Ap4Aase', 'protein',  
                      True)
```

```
relax> molecule.type(mol_id='#Ap4Aase', type  
                      ='protein', force=True)
```

## Spin ID string documentation

---

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

### 14.2.76 molmol.clear\_history



#### Synopsis

Clear the Molmol command history.

#### Defaults

`molmol.clear_history()`

#### Description

This will clear the Molmol history from memory.

---

**14.2.77 molmol.command****Synopsis**

Execute a user supplied Molmol command.

**Defaults**

**molmol.command**(command=None)

**Keyword arguments**

**command**: The Molmol command to execute.

**Description**

This allows Molmol commands to be passed to the program. This can be useful for automation or scripting.

**Prompt examples**

To reinitialise the Molmol instance, type:

```
relax> molmol.command("InitAll yes")
```

---

**14.2.78 molmol.macro\_apply****Synopsis**

Execute Molmol macros.

**Defaults**

**molmol.macro\_apply**(data\_type=None, style='classic', colour\_start\_name=None, colour\_start\_rgb=None, colour\_end\_name=None, colour\_end\_rgb=None, colour\_list=None)

**Keyword arguments**

**data\_type**: The data type to map to the structure.

**style**: The style of the macro.

**colour\_start\_name**: The name of the starting colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the starting colour RGB colour array cannot be given.

**colour\_start\_rgb**: The starting colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the starting colour name cannot be given.

**colour\_end\_name**: The name of the ending colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the ending colour RGB colour array cannot be given.

**colour\_end\_rgb**: The ending colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the ending colour name cannot be given.

**colour\_list**: The colour list to search for the colour names. This can be either 'molmol' or 'x11'.

**Description**

This allows spin specific values to be mapped to a structure through Molmol macros. Currently only the 'classic' style, which is described below, is available.

## Colour

The values are coloured based on a linear colour gradient which is specified through starting and ending colours. These can either be a string to identify one of the RGB (red, green, blue) colour arrays listed in the tables below, or you can give the RGB vector itself. For example, `'white'` and `[1.0, 1.0, 1.0]` both select the same colour. Leaving both colours unset will select the default colour gradient which for each type of analysis is described below.

When supplying the colours as strings, two lists of colours can be selected from which to match the strings. These are the default Molmol colour list and the X11 colour list, both of which are described in the tables below. The default behaviour is to first search the Molmol list and then the X11 colour list, raising an error if neither contain the name. To explicitly select these lists, set the colour list to either `'molmol'` or `'x11'`.

## Model-free classic style

Creator: Edward d'Auvergne

Argument string: `"classic"`

Description: The classic style draws the backbone of a protein in a cylindrical bond style. Rather than colouring the amino acids to which the NH bond belongs, the three covalent bonds of the peptide bond from Ca to Ca in which the NH bond is located are coloured. Deselected residues are shown as black lines.

Supported data types:

Please see Table [14.19](#) on page [349](#).

## Molmol RGB colour arrays

The following table is a list of colours used in Molmol and their corresponding RGB colour values ranging from 0 to 1.

Please see Table [14.20](#) on page [350](#).

## X11 RGB colour arrays

The following table is the list of X11 colour names and their corresponding RGB colour values ranging from 0 to 255.

Please see Table [14.21](#) on page [351](#).

Table 14.19: The model-free classic style for mapping model spin specific data onto 3D molecular structures using either PyMOL or Molmol.

| Data type                  | String      | Description   |
|----------------------------|-------------|---|
| $S^2$ .                    | 's2'        | The standard model-free order parameter, equal to $S_f^2$ .S2s for the two timescale models. The default colour gradient starts at 'yellow' and ends at 'red'.  |
| $S_f^2$ .                  | 's2f'       | The order parameter of the faster of two internal motions. Residues which are described by model-free models m1 to m4, the single timescale models, are illustrated as white neon bonds. The default colour gradient is the same as that for the $S^2$ data type.   |
| $S_s^2$ .                  | 's2s'       | The order parameter of the slower of two internal motions. This functions exactly as $S_f^2$ except that $S_s^2$ is plotted instead.  |
| Amplitude of fast motions. | 'amp_fast'  | Model independent display of the amplitde of fast motions. For residues described by model-free models m5 to m8, the value plotted is that of $S_f^2$ . However, for residues described by models m1 to m4, what is shown is dependent on the timescale of the motions. This is because these single timescale models can, at times, be perfect approximations to the more complex two timescale models. Hence if $\tau_e$ is less than 200 ps, $S^2$ is plotted. Otherwise the peptide bond is coloured white. The default colour gradient is the same as that for $S^2$ . |
| Amplitude of slow motions. | 'amp_slow'  | Model independent display of the amplitde of slow motions, arbitrarily defined as motions slower than 200 ps. For residues described by model-free models m5 to m8, the order parameter $S^2$ is plotted if $\tau_s > 200$ ps. For models m1 to m4, $S^2$ is plotted if $\tau_e > 200$ ps. The default colour gradient is the same as that for $S^2$ .  |
| $\tau_e$ .                 | 'te'        | The correlation time, $\tau_e$ . The default colour gradient starts at 'turquoise' and ends at 'blue'.  |
| $\tau_f$ .                 | 'tf'        | The correlation time, $\tau_f$ . The default colour gradient is the same as that of $\tau_e$ .  |
| $\tau_s$ .                 | 'ts'        | The correlation time, $\tau_s$ . The default colour gradient starts at 'blue' and ends at 'black'.  |
| Timescale of fast motions  | 'time_fast' | Model independent display of the timescale of fast motions. For models m5 to m8, only the parameter $\tau_f$ is plotted. For models m2 and m4, the parameter $\tau_e$ is plotted only if it is less than 200 ps. All other residues are assumed to have a correlation time of zero. The default colour gradient is the same as that of $\tau_e$ .   |
| Timescale of slow motions  | 'time_slow' | Model independent display of the timescale of slow motions. For models m5 to m8, only the parameter $\tau_s$ is plotted. For models m2 and m4, the parameter $\tau_e$ is plotted only if it is greater than 200 ps. All other residues are coloured white. The default colour gradient is the same as that of $\tau_s$ .  |
| Chemical exchange          | 'rex'       | The chemical exchange, $R_{ex}$ . Residues which experience no chemical exchange are coloured white. The default colour gradient starts at 'yellow' and finishes at 'red'.  |

Table 14.20: Molmol colour names and corresponding RGB colour values (from 0 to 1)

| Name           | Red   | Green | Blue  |
|----------------|-------|-------|-------|
| 'black'        | 0.000 | 0.000 | 0.000 |
| 'navy'         | 0.000 | 0.000 | 0.502 |
| 'blue'         | 0.000 | 0.000 | 1.000 |
| 'dark green'   | 0.000 | 0.392 | 0.000 |
| 'green'        | 0.000 | 1.000 | 0.000 |
| 'cyan'         | 0.000 | 1.000 | 1.000 |
| 'turquoise'    | 0.251 | 0.878 | 0.816 |
| 'royal blue'   | 0.255 | 0.412 | 0.882 |
| 'aquamarine'   | 0.498 | 1.000 | 0.831 |
| 'sky green'    | 0.529 | 0.808 | 0.922 |
| 'dark violet'  | 0.580 | 0.000 | 0.827 |
| 'pale green'   | 0.596 | 0.984 | 0.596 |
| 'purple'       | 0.627 | 0.125 | 0.941 |
| 'brown'        | 0.647 | 0.165 | 0.165 |
| 'light blue'   | 0.678 | 0.847 | 0.902 |
| 'grey'         | 0.745 | 0.745 | 0.745 |
| 'light grey'   | 0.827 | 0.827 | 0.827 |
| 'violet'       | 0.933 | 0.510 | 0.933 |
| 'light coral'  | 0.941 | 0.502 | 0.502 |
| 'khaki'        | 0.941 | 0.902 | 0.549 |
| 'beige'        | 0.961 | 0.961 | 0.863 |
| 'red'          | 1.000 | 0.000 | 0.000 |
| 'magenta'      | 1.000 | 0.000 | 1.000 |
| 'deep pink'    | 1.000 | 0.078 | 0.576 |
| 'orange red'   | 1.000 | 0.271 | 0.000 |
| 'hot pink'     | 1.000 | 0.412 | 0.706 |
| 'coral'        | 1.000 | 0.498 | 0.314 |
| 'dark orange'  | 1.000 | 0.549 | 0.000 |
| 'orange'       | 1.000 | 0.647 | 0.000 |
| 'pink'         | 1.000 | 0.753 | 0.796 |
| 'gold'         | 1.000 | 0.843 | 0.000 |
| 'yellow'       | 1.000 | 1.000 | 0.000 |
| 'light yellow' | 1.000 | 1.000 | 0.878 |
| 'ivory'        | 1.000 | 1.000 | 0.941 |
| 'white'        | 1.000 | 1.000 | 1.000 |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name              | Red | Green | Blue |
|-------------------|-----|-------|------|
| snow              | 255 | 250   | 250  |
| ghost white       | 248 | 248   | 255  |
| white smoke       | 245 | 245   | 245  |
| gainsboro         | 220 | 220   | 220  |
| floral white      | 255 | 250   | 240  |
| old lace          | 253 | 245   | 230  |
| linen             | 250 | 240   | 230  |
| antique white     | 250 | 235   | 215  |
| papaya whip       | 255 | 239   | 213  |
| blanched almond   | 255 | 235   | 205  |
| bisque            | 255 | 228   | 196  |
| peach puff        | 255 | 218   | 185  |
| navajo white      | 255 | 222   | 173  |
| moccasin          | 255 | 228   | 181  |
| cornsilk          | 255 | 248   | 220  |
| ivory             | 255 | 255   | 240  |
| lemon chiffon     | 255 | 250   | 205  |
| seashell          | 255 | 245   | 238  |
| honeydew          | 240 | 255   | 240  |
| mint cream        | 245 | 255   | 250  |
| azure             | 240 | 255   | 255  |
| alice blue        | 240 | 248   | 255  |
| lavender          | 230 | 230   | 250  |
| lavender blush    | 255 | 240   | 245  |
| misty rose        | 255 | 228   | 225  |
| white             | 255 | 255   | 255  |
| black             | 0   | 0     | 0    |
| dark slate grey   | 47  | 79    | 79   |
| dim grey          | 105 | 105   | 105  |
| slate grey        | 112 | 128   | 144  |
| light slate grey  | 119 | 136   | 153  |
| grey              | 190 | 190   | 190  |
| light grey        | 211 | 211   | 211  |
| midnight blue     | 25  | 25    | 112  |
| navy              | 0   | 0     | 128  |
| cornflower blue   | 100 | 149   | 237  |
| dark slate blue   | 72  | 61    | 139  |
| slate blue        | 106 | 90    | 205  |
| medium slate blue | 123 | 104   | 238  |
| light slate blue  | 132 | 112   | 255  |
| medium blue       | 0   | 0     | 205  |
| royal blue        | 65  | 105   | 225  |
| blue              | 0   | 0     | 255  |
| dodger blue       | 30  | 144   | 255  |
| deep sky blue     | 0   | 191   | 255  |
| sky blue          | 135 | 206   | 235  |
| light sky blue    | 135 | 206   | 250  |
| steel blue        | 70  | 130   | 180  |
| light steel blue  | 176 | 196   | 222  |
| light blue        | 173 | 216   | 230  |
| powder blue       | 176 | 224   | 230  |
| pale turquoise    | 175 | 238   | 238  |
| dark turquoise    | 0   | 206   | 209  |
| medium turquoise  | 72  | 209   | 204  |
| turquoise         | 64  | 224   | 208  |
| cyan              | 0   | 255   | 255  |
| light cyan        | 224 | 255   | 255  |
| cadet blue        | 95  | 158   | 160  |
| medium aquamarine | 102 | 205   | 170  |
| aquamarine        | 127 | 255   | 212  |
| dark green        | 0   | 100   | 0    |
| dark olive green  | 85  | 107   | 47   |
| dark sea green    | 143 | 188   | 143  |
| sea green         | 46  | 139   | 87   |
| medium sea green  | 60  | 179   | 113  |
| light sea green   | 32  | 178   | 170  |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name                   | Red | Green | Blue |
|------------------------|-----|-------|------|
| pale green             | 152 | 251   | 152  |
| spring green           | 0   | 255   | 127  |
| lawn green             | 124 | 252   | 0    |
| green                  | 0   | 255   | 0    |
| chartreuse             | 127 | 255   | 0    |
| medium spring green    | 0   | 250   | 154  |
| green yellow           | 173 | 255   | 47   |
| lime green             | 50  | 205   | 50   |
| yellow green           | 154 | 205   | 50   |
| forest green           | 34  | 139   | 34   |
| olive drab             | 107 | 142   | 35   |
| dark khaki             | 189 | 183   | 107  |
| khaki                  | 240 | 230   | 140  |
| pale goldenrod         | 238 | 232   | 170  |
| light goldenrod yellow | 250 | 250   | 210  |
| light yellow           | 255 | 255   | 224  |
| yellow                 | 255 | 255   | 0    |
| gold                   | 255 | 215   | 0    |
| light goldenrod        | 238 | 221   | 130  |
| goldenrod              | 218 | 165   | 32   |
| dark goldenrod         | 184 | 134   | 11   |
| rosy brown             | 188 | 143   | 143  |
| indian red             | 205 | 92    | 92   |
| saddle brown           | 139 | 69    | 19   |
| sienna                 | 160 | 82    | 45   |
| peru                   | 205 | 133   | 63   |
| burlywood              | 222 | 184   | 135  |
| beige                  | 245 | 245   | 220  |
| wheat                  | 245 | 222   | 179  |
| sandy brown            | 244 | 164   | 96   |
| tan                    | 210 | 180   | 140  |
| chocolate              | 210 | 105   | 30   |
| firebrick              | 178 | 34    | 34   |
| brown                  | 165 | 42    | 42   |
| dark salmon            | 233 | 150   | 122  |
| salmon                 | 250 | 128   | 114  |
| light salmon           | 255 | 160   | 122  |
| orange                 | 255 | 165   | 0    |
| dark orange            | 255 | 140   | 0    |
| coral                  | 255 | 127   | 80   |
| light coral            | 240 | 128   | 128  |
| tomato                 | 255 | 99    | 71   |
| orange red             | 255 | 69    | 0    |
| red                    | 255 | 0     | 0    |
| hot pink               | 255 | 105   | 180  |
| deep pink              | 255 | 20    | 147  |
| pink                   | 255 | 192   | 203  |
| light pink             | 255 | 182   | 193  |
| pale violet red        | 219 | 112   | 147  |
| maroon                 | 176 | 48    | 96   |
| medium violet red      | 199 | 21    | 133  |
| violet red             | 208 | 32    | 144  |
| magenta                | 255 | 0     | 255  |
| violet                 | 238 | 130   | 238  |
| plum                   | 221 | 160   | 221  |
| orchid                 | 218 | 112   | 214  |
| medium orchid          | 186 | 85    | 211  |
| dark orchid            | 153 | 50    | 204  |
| dark violet            | 148 | 0     | 211  |
| blue violet            | 138 | 43    | 226  |
| purple                 | 160 | 32    | 240  |
| medium purple          | 147 | 112   | 219  |
| thistle                | 216 | 191   | 216  |
| snow 1                 | 255 | 250   | 250  |
| snow 2                 | 238 | 233   | 233  |
| snow 3                 | 205 | 201   | 201  |



Table 14.21: X11 colour names and corresponding RGB colour values

| Name             | Red | Green | Blue |
|------------------|-----|-------|------|
| snow 4           | 139 | 137   | 137  |
| seashell 1       | 255 | 245   | 238  |
| seashell 2       | 238 | 229   | 222  |
| seashell 3       | 205 | 197   | 191  |
| seashell 4       | 139 | 134   | 130  |
| antique white 1  | 255 | 239   | 219  |
| antique white 2  | 238 | 223   | 204  |
| antique white 3  | 205 | 192   | 176  |
| antique white 4  | 139 | 131   | 120  |
| bisque 1         | 255 | 228   | 196  |
| bisque 2         | 238 | 213   | 183  |
| bisque 3         | 205 | 183   | 158  |
| bisque 4         | 139 | 125   | 107  |
| peach puff 1     | 255 | 218   | 185  |
| peach puff 2     | 238 | 203   | 173  |
| peach puff 3     | 205 | 175   | 149  |
| peach puff 4     | 139 | 119   | 101  |
| navajo white 1   | 255 | 222   | 173  |
| navajo white 2   | 238 | 207   | 161  |
| navajo white 3   | 205 | 179   | 139  |
| navajo white 4   | 139 | 121   | 94   |
| lemon chiffon 1  | 255 | 250   | 205  |
| lemon chiffon 2  | 238 | 233   | 191  |
| lemon chiffon 3  | 205 | 201   | 165  |
| lemon chiffon 4  | 139 | 137   | 112  |
| cornsilk 1       | 255 | 248   | 220  |
| cornsilk 2       | 238 | 232   | 205  |
| cornsilk 3       | 205 | 200   | 177  |
| cornsilk 4       | 139 | 136   | 120  |
| ivory 1          | 255 | 255   | 240  |
| ivory 2          | 238 | 238   | 224  |
| ivory 3          | 205 | 205   | 193  |
| ivory 4          | 139 | 139   | 131  |
| honeydew 1       | 240 | 255   | 240  |
| honeydew 2       | 224 | 238   | 224  |
| honeydew 3       | 193 | 205   | 193  |
| honeydew 4       | 131 | 139   | 131  |
| lavender blush 1 | 255 | 240   | 245  |
| lavender blush 2 | 238 | 224   | 229  |
| lavender blush 3 | 205 | 193   | 197  |
| lavender blush 4 | 139 | 131   | 134  |
| misty rose 1     | 255 | 228   | 225  |
| misty rose 2     | 238 | 213   | 210  |
| misty rose 3     | 205 | 183   | 181  |
| misty rose 4     | 139 | 125   | 123  |
| azure 1          | 240 | 255   | 255  |
| azure 2          | 224 | 238   | 238  |
| azure 3          | 193 | 205   | 205  |
| azure 4          | 131 | 139   | 139  |
| slate blue 1     | 131 | 111   | 255  |
| slate blue 2     | 122 | 103   | 238  |
| slate blue 3     | 105 | 89    | 205  |
| slate blue 4     | 71  | 60    | 139  |
| royal blue 1     | 72  | 118   | 255  |
| royal blue 2     | 67  | 110   | 238  |
| royal blue 3     | 58  | 95    | 205  |
| royal blue 4     | 39  | 64    | 139  |
| blue 1           | 0   | 0     | 255  |
| blue 2           | 0   | 0     | 238  |
| blue 3           | 0   | 0     | 205  |
| blue 4           | 0   | 0     | 139  |
| dodger blue 1    | 30  | 144   | 255  |
| dodger blue 2    | 28  | 134   | 238  |
| dodger blue 3    | 24  | 116   | 205  |
| dodger blue 4    | 16  | 78    | 139  |
| steel blue 1     | 99  | 184   | 255  |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name               | Red | Green | Blue |
|--------------------|-----|-------|------|
| steel blue 2       | 92  | 172   | 238  |
| steel blue 3       | 79  | 148   | 205  |
| steel blue 4       | 54  | 100   | 139  |
| deep sky blue 1    | 0   | 191   | 255  |
| deep sky blue 2    | 0   | 178   | 238  |
| deep sky blue 3    | 0   | 154   | 205  |
| deep sky blue 4    | 0   | 104   | 139  |
| sky blue 1         | 135 | 206   | 255  |
| sky blue 2         | 126 | 192   | 238  |
| sky blue 3         | 108 | 166   | 205  |
| sky blue 4         | 74  | 112   | 139  |
| light sky blue 1   | 176 | 226   | 255  |
| light sky blue 2   | 164 | 211   | 238  |
| light sky blue 3   | 141 | 182   | 205  |
| light sky blue 4   | 96  | 123   | 139  |
| slate grey 1       | 198 | 226   | 255  |
| slate grey 2       | 185 | 211   | 238  |
| slate grey 3       | 159 | 182   | 205  |
| slate grey 4       | 108 | 123   | 139  |
| light steel blue 1 | 202 | 225   | 255  |
| light steel blue 2 | 188 | 210   | 238  |
| light steel blue 3 | 162 | 181   | 205  |
| light steel blue 4 | 110 | 123   | 139  |
| light blue 1       | 191 | 239   | 255  |
| light blue 2       | 178 | 223   | 238  |
| light blue 3       | 154 | 192   | 205  |
| light blue 4       | 104 | 131   | 139  |
| light cyan 1       | 224 | 255   | 255  |
| light cyan 2       | 209 | 238   | 238  |
| light cyan 3       | 180 | 205   | 205  |
| light cyan 4       | 122 | 139   | 139  |
| pale turquoise 1   | 187 | 255   | 255  |
| pale turquoise 2   | 174 | 238   | 238  |
| pale turquoise 3   | 150 | 205   | 205  |
| pale turquoise 4   | 102 | 139   | 139  |
| cadet blue 1       | 152 | 245   | 255  |
| cadet blue 2       | 142 | 229   | 238  |
| cadet blue 3       | 122 | 197   | 205  |
| cadet blue 4       | 83  | 134   | 139  |
| turquoise 1        | 0   | 245   | 255  |
| turquoise 2        | 0   | 229   | 238  |
| turquoise 3        | 0   | 197   | 205  |
| turquoise 4        | 0   | 134   | 139  |
| cyan 1             | 0   | 255   | 255  |
| cyan 2             | 0   | 238   | 238  |
| cyan 3             | 0   | 205   | 205  |
| cyan 4             | 0   | 139   | 139  |
| dark slate grey 1  | 151 | 255   | 255  |
| dark slate grey 2  | 141 | 238   | 238  |
| dark slate grey 3  | 121 | 205   | 205  |
| dark slate grey 4  | 82  | 139   | 139  |
| aquamarine 1       | 127 | 255   | 212  |
| aquamarine 2       | 118 | 238   | 198  |
| aquamarine 3       | 102 | 205   | 170  |
| aquamarine 4       | 69  | 139   | 116  |
| dark sea green 1   | 193 | 255   | 193  |
| dark sea green 2   | 180 | 238   | 180  |
| dark sea green 3   | 155 | 205   | 155  |
| dark sea green 4   | 105 | 139   | 105  |
| sea green 1        | 84  | 255   | 159  |
| sea green 2        | 78  | 238   | 148  |
| sea green 3        | 67  | 205   | 128  |
| sea green 4        | 46  | 139   | 87   |
| pale green 1       | 154 | 255   | 154  |
| pale green 2       | 144 | 238   | 144  |
| pale green 3       | 124 | 205   | 124  |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name               | Red | Green | Blue |
|--------------------|-----|-------|------|
| pale green 4       | 84  | 139   | 84   |
| spring green 1     | 0   | 255   | 127  |
| spring green 2     | 0   | 238   | 118  |
| spring green 3     | 0   | 205   | 102  |
| spring green 4     | 0   | 139   | 69   |
| green 1            | 0   | 255   | 0    |
| green 2            | 0   | 238   | 0    |
| green 3            | 0   | 205   | 0    |
| green 4            | 0   | 139   | 0    |
| chartreuse 1       | 127 | 255   | 0    |
| chartreuse 2       | 118 | 238   | 0    |
| chartreuse 3       | 102 | 205   | 0    |
| chartreuse 4       | 69  | 139   | 0    |
| olive drab 1       | 192 | 255   | 62   |
| olive drab 2       | 179 | 238   | 58   |
| olive drab 3       | 154 | 205   | 50   |
| olive drab 4       | 105 | 139   | 34   |
| dark olive green 1 | 202 | 255   | 112  |
| dark olive green 2 | 188 | 238   | 104  |
| dark olive green 3 | 162 | 205   | 90   |
| dark olive green 4 | 110 | 139   | 61   |
| khaki 1            | 255 | 246   | 143  |
| khaki 2            | 238 | 230   | 133  |
| khaki 3            | 205 | 198   | 115  |
| khaki 4            | 139 | 134   | 78   |
| light goldenrod 1  | 255 | 236   | 139  |
| light goldenrod 2  | 238 | 220   | 130  |
| light goldenrod 3  | 205 | 190   | 112  |
| light goldenrod 4  | 139 | 129   | 76   |
| light yellow 1     | 255 | 255   | 224  |
| light yellow 2     | 238 | 238   | 209  |
| light yellow 3     | 205 | 205   | 180  |
| light yellow 4     | 139 | 139   | 122  |
| yellow 1           | 255 | 255   | 0    |
| yellow 2           | 238 | 238   | 0    |
| yellow 3           | 205 | 205   | 0    |
| yellow 4           | 139 | 139   | 0    |
| gold 1             | 255 | 215   | 0    |
| gold 2             | 238 | 201   | 0    |
| gold 3             | 205 | 173   | 0    |
| gold 4             | 139 | 117   | 0    |
| goldenrod 1        | 255 | 193   | 37   |
| goldenrod 2        | 238 | 180   | 34   |
| goldenrod 3        | 205 | 155   | 29   |
| goldenrod 4        | 139 | 105   | 20   |
| dark goldenrod 1   | 255 | 185   | 15   |
| dark goldenrod 2   | 238 | 173   | 14   |
| dark goldenrod 3   | 205 | 149   | 12   |
| dark goldenrod 4   | 139 | 101   | 8    |
| rosy brown 1       | 255 | 193   | 193  |
| rosy brown 2       | 238 | 180   | 180  |
| rosy brown 3       | 205 | 155   | 155  |
| rosy brown 4       | 139 | 105   | 105  |
| indian red 1       | 255 | 106   | 106  |
| indian red 2       | 238 | 99    | 99   |
| indian red 3       | 205 | 85    | 85   |
| indian red 4       | 139 | 58    | 58   |
| sienna 1           | 255 | 130   | 71   |
| sienna 2           | 238 | 121   | 66   |
| sienna 3           | 205 | 104   | 57   |
| sienna 4           | 139 | 71    | 38   |
| burlywood 1        | 255 | 211   | 155  |
| burlywood 2        | 238 | 197   | 145  |
| burlywood 3        | 205 | 170   | 125  |
| burlywood 4        | 139 | 115   | 85   |
| wheat 1            | 255 | 231   | 186  |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name           | Red | Green | Blue |
|----------------|-----|-------|------|
| wheat 2        | 238 | 216   | 174  |
| wheat 3        | 205 | 186   | 150  |
| wheat 4        | 139 | 126   | 102  |
| tan 1          | 255 | 165   | 79   |
| tan 2          | 238 | 154   | 73   |
| tan 3          | 205 | 133   | 63   |
| tan 4          | 139 | 90    | 43   |
| chocolate 1    | 255 | 127   | 36   |
| chocolate 2    | 238 | 118   | 33   |
| chocolate 3    | 205 | 102   | 29   |
| chocolate 4    | 139 | 69    | 19   |
| firebrick 1    | 255 | 48    | 48   |
| firebrick 2    | 238 | 44    | 44   |
| firebrick 3    | 205 | 38    | 38   |
| firebrick 4    | 139 | 26    | 26   |
| brown 1        | 255 | 64    | 64   |
| brown 2        | 238 | 59    | 59   |
| brown 3        | 205 | 51    | 51   |
| brown 4        | 139 | 35    | 35   |
| salmon 1       | 255 | 140   | 105  |
| salmon 2       | 238 | 130   | 98   |
| salmon 3       | 205 | 112   | 84   |
| salmon 4       | 139 | 76    | 57   |
| light salmon 1 | 255 | 160   | 122  |
| light salmon 2 | 238 | 149   | 114  |
| light salmon 3 | 205 | 129   | 98   |
| light salmon 4 | 139 | 87    | 66   |
| orange 1       | 255 | 165   | 0    |
| orange 2       | 238 | 154   | 0    |
| orange 3       | 205 | 133   | 0    |
| orange 4       | 139 | 90    | 0    |
| dark orange 1  | 255 | 127   | 0    |
| dark orange 2  | 238 | 118   | 0    |
| dark orange 3  | 205 | 102   | 0    |
| dark orange 4  | 139 | 69    | 0    |
| coral 1        | 255 | 114   | 86   |
| coral 2        | 238 | 106   | 80   |
| coral 3        | 205 | 91    | 69   |
| coral 4        | 139 | 62    | 47   |
| tomato 1       | 255 | 99    | 71   |
| tomato 2       | 238 | 92    | 66   |
| tomato 3       | 205 | 79    | 57   |
| tomato 4       | 139 | 54    | 38   |
| orange red 1   | 255 | 69    | 0    |
| orange red 2   | 238 | 64    | 0    |
| orange red 3   | 205 | 55    | 0    |
| orange red 4   | 139 | 37    | 0    |
| red 1          | 255 | 0     | 0    |
| red 2          | 238 | 0     | 0    |
| red 3          | 205 | 0     | 0    |
| red 4          | 139 | 0     | 0    |
| deep pink 1    | 255 | 20    | 147  |
| deep pink 2    | 238 | 18    | 137  |
| deep pink 3    | 205 | 16    | 118  |
| deep pink 4    | 139 | 10    | 80   |
| hot pink 1     | 255 | 110   | 180  |
| hot pink 2     | 238 | 106   | 167  |
| hot pink 3     | 205 | 96    | 144  |
| hot pink 4     | 139 | 58    | 98   |
| pink 1         | 255 | 181   | 197  |
| pink 2         | 238 | 169   | 184  |
| pink 3         | 205 | 145   | 158  |
| pink 4         | 139 | 99    | 108  |
| light pink 1   | 255 | 174   | 185  |
| light pink 2   | 238 | 162   | 173  |
| light pink 3   | 205 | 140   | 149  |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name              | Red | Green | Blue |
|-------------------|-----|-------|------|
| light pink 4      | 139 | 95    | 101  |
| pale violet red 1 | 255 | 130   | 171  |
| pale violet red 2 | 238 | 121   | 159  |
| pale violet red 3 | 205 | 104   | 137  |
| pale violet red 4 | 139 | 71    | 93   |
| maroon 1          | 255 | 52    | 179  |
| maroon 2          | 238 | 48    | 167  |
| maroon 3          | 205 | 41    | 144  |
| maroon 4          | 139 | 28    | 98   |
| violet red 1      | 255 | 62    | 150  |
| violet red 2      | 238 | 58    | 140  |
| violet red 3      | 205 | 50    | 120  |
| violet red 4      | 139 | 34    | 82   |
| magenta 1         | 255 | 0     | 255  |
| magenta 2         | 238 | 0     | 238  |
| magenta 3         | 205 | 0     | 205  |
| magenta 4         | 139 | 0     | 139  |
| orchid 1          | 255 | 131   | 250  |
| orchid 2          | 238 | 122   | 233  |
| orchid 3          | 205 | 105   | 201  |
| orchid 4          | 139 | 71    | 137  |
| plum 1            | 255 | 187   | 255  |
| plum 2            | 238 | 174   | 238  |
| plum 3            | 205 | 150   | 205  |
| plum 4            | 139 | 102   | 139  |
| medium orchid 1   | 224 | 102   | 255  |
| medium orchid 2   | 209 | 95    | 238  |
| medium orchid 3   | 180 | 82    | 205  |
| medium orchid 4   | 122 | 55    | 139  |
| dark orchid 1     | 191 | 62    | 255  |
| dark orchid 2     | 178 | 58    | 238  |
| dark orchid 3     | 154 | 50    | 205  |
| dark orchid 4     | 104 | 34    | 139  |
| purple 1          | 155 | 48    | 255  |
| purple 2          | 145 | 44    | 238  |
| purple 3          | 125 | 38    | 205  |
| purple 4          | 85  | 26    | 139  |
| medium purple 1   | 171 | 130   | 255  |
| medium purple 2   | 159 | 121   | 238  |
| medium purple 3   | 137 | 104   | 205  |
| medium purple 4   | 93  | 71    | 139  |
| thistle 1         | 255 | 225   | 255  |
| thistle 2         | 238 | 210   | 238  |
| thistle 3         | 205 | 181   | 205  |
| thistle 4         | 139 | 123   | 139  |
| grey 0            | 0   | 0     | 0    |
| grey 1            | 3   | 3     | 3    |
| grey 2            | 5   | 5     | 5    |
| grey 3            | 8   | 8     | 8    |
| grey 4            | 10  | 10    | 10   |
| grey 5            | 13  | 13    | 13   |
| grey 6            | 15  | 15    | 15   |
| grey 7            | 18  | 18    | 18   |
| grey 8            | 20  | 20    | 20   |
| grey 9            | 23  | 23    | 23   |
| grey 10           | 26  | 26    | 26   |
| grey 11           | 28  | 28    | 28   |
| grey 12           | 31  | 31    | 31   |
| grey 13           | 33  | 33    | 33   |
| grey 14           | 36  | 36    | 36   |
| grey 15           | 38  | 38    | 38   |
| grey 16           | 41  | 41    | 41   |
| grey 17           | 43  | 43    | 43   |
| grey 18           | 46  | 46    | 46   |
| grey 19           | 48  | 48    | 48   |
| grey 20           | 51  | 51    | 51   |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name    | Red | Green | Blue |
|---------|-----|-------|------|
| grey 21 | 54  | 54    | 54   |
| grey 22 | 56  | 56    | 56   |
| grey 23 | 59  | 59    | 59   |
| grey 24 | 61  | 61    | 61   |
| grey 25 | 64  | 64    | 64   |
| grey 26 | 66  | 66    | 66   |
| grey 27 | 69  | 69    | 69   |
| grey 28 | 71  | 71    | 71   |
| grey 29 | 74  | 74    | 74   |
| grey 30 | 77  | 77    | 77   |
| grey 31 | 79  | 79    | 79   |
| grey 32 | 82  | 82    | 82   |
| grey 33 | 84  | 84    | 84   |
| grey 34 | 87  | 87    | 87   |
| grey 35 | 89  | 89    | 89   |
| grey 36 | 92  | 92    | 92   |
| grey 37 | 94  | 94    | 94   |
| grey 38 | 97  | 97    | 97   |
| grey 39 | 99  | 99    | 99   |
| grey 40 | 102 | 102   | 102  |
| grey 41 | 105 | 105   | 105  |
| grey 42 | 107 | 107   | 107  |
| grey 43 | 110 | 110   | 110  |
| grey 44 | 112 | 112   | 112  |
| grey 45 | 115 | 115   | 115  |
| grey 46 | 117 | 117   | 117  |
| grey 47 | 120 | 120   | 120  |
| grey 48 | 122 | 122   | 122  |
| grey 49 | 125 | 125   | 125  |
| grey 50 | 127 | 127   | 127  |
| grey 51 | 130 | 130   | 130  |
| grey 52 | 133 | 133   | 133  |
| grey 53 | 135 | 135   | 135  |
| grey 54 | 138 | 138   | 138  |
| grey 55 | 140 | 140   | 140  |
| grey 56 | 143 | 143   | 143  |
| grey 57 | 145 | 145   | 145  |
| grey 58 | 148 | 148   | 148  |
| grey 59 | 150 | 150   | 150  |
| grey 60 | 153 | 153   | 153  |
| grey 61 | 156 | 156   | 156  |
| grey 62 | 158 | 158   | 158  |
| grey 63 | 161 | 161   | 161  |
| grey 64 | 163 | 163   | 163  |
| grey 65 | 166 | 166   | 166  |
| grey 66 | 168 | 168   | 168  |
| grey 67 | 171 | 171   | 171  |
| grey 68 | 173 | 173   | 173  |
| grey 69 | 176 | 176   | 176  |
| grey 70 | 179 | 179   | 179  |
| grey 71 | 181 | 181   | 181  |
| grey 72 | 184 | 184   | 184  |
| grey 73 | 186 | 186   | 186  |
| grey 74 | 189 | 189   | 189  |
| grey 75 | 191 | 191   | 191  |
| grey 76 | 194 | 194   | 194  |
| grey 77 | 196 | 196   | 196  |
| grey 78 | 199 | 199   | 199  |
| grey 79 | 201 | 201   | 201  |
| grey 80 | 204 | 204   | 204  |
| grey 81 | 207 | 207   | 207  |
| grey 82 | 209 | 209   | 209  |
| grey 83 | 212 | 212   | 212  |
| grey 84 | 214 | 214   | 214  |
| grey 85 | 217 | 217   | 217  |
| grey 86 | 219 | 219   | 219  |

Table 14.21: X11 colour names and corresponding RGB colour values

| Name         | Red | Green | Blue |
|--------------|-----|-------|------|
| grey 87      | 222 | 222   | 222  |
| grey 88      | 224 | 224   | 224  |
| grey 89      | 227 | 227   | 227  |
| grey 90      | 229 | 229   | 229  |
| grey 91      | 232 | 232   | 232  |
| grey 92      | 235 | 235   | 235  |
| grey 93      | 237 | 237   | 237  |
| grey 94      | 240 | 240   | 240  |
| grey 95      | 242 | 242   | 242  |
| grey 96      | 245 | 245   | 245  |
| grey 97      | 247 | 247   | 247  |
| grey 98      | 250 | 250   | 250  |
| grey 99      | 252 | 252   | 252  |
| grey 100     | 255 | 255   | 255  |
| dark grey    | 169 | 169   | 169  |
| dark blue    | 0   | 0     | 139  |
| dark cyan    | 0   | 139   | 139  |
| dark magenta | 139 | 0     | 139  |
| dark red     | 139 | 0     | 0    |
| light green  | 144 | 238   | 144  |

## Prompt examples

To map the order parameter values,  $S^2$ , onto the structure using the classic style, type:

```
relax> molmol.macro_apply('s2')

relax> molmol.macro_apply(data_type='s2')

relax> molmol.macro_apply(data_type='s2',
                           style="classic")
```

---

### 14.2.79 molmol.macro\_run



## Synopsis

Open and execute the Molmol macro file.

## Defaults

`molmol.macro_run(file=None, dir='molmol')`

## Keyword arguments

`file`: The name of the Molmol macro file.

`dir`: The directory name.

## Description

This user function is for opening and running a Molmol macro located within a text file.

## Prompt examples

To execute the macro file 's2.mac' located in the directory 'molmol', type:

```
relax> molmol.macro_run(file='s2.mac')

relax> molmol.macro_run(file='s2.mac', dir='
molmol')
```



## 14.2.80 molmol.macro\_write




### Synopsis

Create Molmol macros.

### Defaults

**molmol.macro\_write**(data\_type=None, style='classic', colour\_start\_name=None, colour\_start\_rgb=None, colour\_end\_name=None, colour\_end\_rgb=None, colour\_list=None, file=None, dir='molmol', force=False)

### Keyword arguments

**data\_type**: The data type to map to the structure.

**style**: The style of the macro.

**colour\_start\_name**: The name of the starting colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the starting colour RGB colour array cannot be given.

**colour\_start\_rgb**: The starting colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the starting colour name cannot be given.

**colour\_end\_name**: The name of the ending colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the ending colour RGB colour array cannot be given.

**colour\_end\_rgb**: The ending colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the ending colour name cannot be given.

**colour\_list**: The colour list to search for the colour names. This can be either 'molmol' or 'x11'.

**file**: The optional name of the file.

**dir**: The optional directory to save the file to.

**force**: A flag which, if set to True, will cause the file to be overwritten.

### Description

This allows residues specific values to be mapped to a structure through the creation of a Molmol '\*.mac' macro which can be executed in Molmol by clicking on 'File, Macro, Execute User...'. Currently only the 'classic' style, which is described below, is available.

### Colour

The values are coloured based on a linear colour gradient which is specified through starting and ending colours. These can either be a string to identify one of the RGB (red, green, blue) colour arrays listed in the tables below, or you can give the RGB vector itself. For example, 'white' and [1.0, 1.0, 1.0] both select the same colour. Leaving both colours unset will select the default colour gradient which for each type of analysis is described below.

When supplying the colours as strings, two lists of colours can be selected from which to match the strings. These are the default Molmol colour list and the X11 colour list, both of which are described in the tables below. The default behaviour is to first search the Molmol list and then the X11 colour list, raising an error if neither contain the name. To explicitly select these lists, set the colour list to either 'molmol' or 'x11'.

### Model-free classic style

Creator: Edward d'Auvergne

Argument string: "classic"

**Description**: The classic style draws the backbone of a protein in a cylindrical bond style. Rather than colouring the amino acids to which the NH bond belongs, the three covalent bonds of the peptide bond from Ca to Ca in which the NH bond is located are coloured. Deselected residues are shown as black lines.

Supported data types:

Please see Table 14.19 on page 349.

### Molmol RGB colour arrays

The following table is a list of colours used in Molmol and their corresponding RGB colour values ranging from 0 to 1.

Please see Table 14.20 on page 350.

### X11 RGB colour arrays

The following table is the list of X11 colour names and their corresponding RGB colour values ranging from 0 to 255.

Please see Table 14.21 on page 351.

### Prompt examples

To create a Molmol macro mapping the order parameter values,  $S^2$ , onto the structure using the classic style, type:

```
relax> molmol.macro_write('s2')
```

```
relax> molmol.macro_write(data_type='s2')  
  
relax> molmol.macro_write(data_type='s2',  
    style="classic", file='s2.mac', dir='  
    molmol')
```

---

## 14.2.81 molmol.ribbon



### Synopsis

Apply the Molmol ribbon style.

### Defaults

**molmol.ribbon()**

### Description

This applies the Molmol ribbon style which is equivalent to clicking on ‘ribbon’ in the Molmol side menu. To do this, the following commands are executed:

CalcAtom ‘H’

CalcAtom ‘HN’

CalcSecondary

XMacStand ribbon.mac

### Prompt examples

To apply the ribbon style to the PDB file loaded, type:

```
relax> molmol.ribbon()
```

## 14.2.82 molmol.tensor\_pdb



### Synopsis

Display the diffusion tensor PDB geometric object over the loaded PDB.

### Defaults

**molmol.tensor\_pdb**(file=None)

### Keyword arguments

**file**: The name of the PDB file containing the tensor geometric object.

### Description

In executing this user function, a PDB file must have previously been loaded, a geometric object or polygon representing the Brownian rotational diffusion tensor will be overlain with the loaded PDB file and displayed within Molmol. The PDB file containing the geometric object must be created using the complementary structure.create\_diff\_tensor\_pdb user function.

To display the diffusion tensor, the multiple commands will be executed. To overlay the structure with the diffusion tensor, everything will be selected and reoriented and moved to their original PDB frame positions:

```
SelectAtom ''
SelectBond ''
SelectAngle ''
SelectDist ''
SelectPrim ''
RotateInit
MoveInit
```

Next the tensor PDB file is read in, selected, and the covalent bonds of the PDB CONECT records calculated:

```
ReadPdb file
SelectMol '@file'
CalcBond 1 1 1
```

Then only the atoms and bonds of the geometric object are selected and the 'ball/stick' style applied:

```
SelectAtom 'O'
SelectBond 'O'
SelectAtom ':TNS'
SelectBond ':TNS'
XMacStand ball_stick.mac
```

The appearance is finally touched up:

```
RadiusAtom 1
SelectAtom ':TNS@C*'
RadiusAtom 1.5
```

---

### 14.2.83 molmol.view



#### Synopsis

View the collection of molecules from the loaded PDB file.

#### Defaults

`molmol.view()`

#### Description

This will simply launch Molmol.

#### Prompt examples

```
relax> molmol.view()
```

---

### 14.2.84 monte\_carlo.create\_data



#### Synopsis

Create the Monte Carlo simulation data.

#### Defaults

`monte_carlo.create_data(method='back_calc')`

#### Keyword arguments

`method`: The simulation method.

#### Description

The method can either be set to back calculation (Monte Carlo) or direct (bootstrapping), the choice of which determines the simulation type. If the values or parameters are calculated rather than minimised, this option will have no effect. Errors should only be propagated via Monte Carlo simulations if errors have been measured.

For error analysis, the method should be set to back calculation which will result in proper Monte Carlo simulations. The data used for each simulation is back calculated from the minimised model parameters and is randomised using Gaussian noise where the standard deviation is from the original error set. When the method is set to back calculation, this function should only be called after the model is fully minimised.

The simulation type can be changed by setting the method to direct. This will result in bootstrapping simulations which cannot be used in error analysis (and which are no longer Monte Carlo simulations). However, these simulations are required for certain model selection techniques (see the documentation for the model selection user function for details), and can be used for other purposes. Rather than the data being back calculated from the fitted model parameters, the data is generated by taking the original data and randomising using Gaussian noise with the standard deviations set to the original error set.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

- 1 – The measured data set together with the corresponding error set should be loaded into relax.

- 2 – Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
- 3 – To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
- 4 – The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
- 5 – Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
- 6 – Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
- 7 – Failed simulations are removed using the techniques of model elimination.
- 8 – The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example for model-free analysis using the prompt UI mode which includes only the functions required for implementing the above steps is:

```
relax> grid_search(inc=11)
# Step 2.

relax> minimise('newton')
# Step 2.

relax> monte_carlo.setup(number=500)
# Step 3.

relax> monte_carlo.create_data(method='
back_calc') # Step 4.

relax> monte_carlo.initial_values()
# Step 5.
```

```
relax> minimise('newton')
# Step 6.
```

```
relax> eliminate()
# Step 7.
```

```
relax> monte_carlo.error_analysis()
# Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc()
# Step 2.
```

```
relax> monte_carlo.setup(number=500)
# Step 3.
```

```
relax> monte_carlo.create_data(method='
back_calc') # Step 4.
```

```
relax> calc()
# Step 6.
```

```
relax> monte_carlo.error_analysis()
# Step 8.
```

### 14.2.85 monte\_carlo.error\_analysis



#### Synopsis

Calculate parameter errors from the Monte Carlo simulations.

#### Defaults

`monte_carlo.error_analysis()`

#### Description

Parameter errors are calculated as the standard deviation of the distribution of parameter values. This function should never be used if parameter values are obtained by minimisation and the simulation data are generated using the method `'direct'`. The reason is because only true Monte Carlo simulations can give the true parameter errors.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

- 1 – The measured data set together with the corresponding error set should be loaded into relax.
- 2 – Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
- 3 – To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
- 4 – The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
- 5 – Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).

6 – Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.

7 – Failed simulations are removed using the techniques of model elimination.

8 – The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example for model-free analysis using the prompt UI mode which includes only the functions required for implementing the above steps is:

```
relax> grid_search(inc=11)
# Step 2.

relax> minimise('newton')
# Step 2.

relax> monte_carlo.setup(number=500)
# Step 3.

relax> monte_carlo.create_data(method='
back_calc')
# Step 4.

relax> monte_carlo.initial_values()
# Step 5.

relax> minimise('newton')
# Step 6.

relax> eliminate()
# Step 7.

relax> monte_carlo.error_analysis()
# Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc()
# Step 2.

relax> monte_carlo.setup(number=500)
# Step 3.

relax> monte_carlo.create_data(method='
back_calc')
# Step 4.

relax> calc()
# Step 6.

relax> monte_carlo.error_analysis()
# Step 8.
```

## 14.2.86 monte\_carlo.initial\_values



### Synopsis

Set the initial simulation parameter values.

### Defaults

`monte_carlo.initial_values()`

### Description

This only effects where minimisation occurs and can therefore be skipped if the values or parameters are calculated rather than minimised. However, if accidentally run in this case, the results will be unaffected. It should only be called after the model or run is fully minimised. Once called, the functions ‘`grid_search`’ and ‘`minimise`’ will only effect the simulations and not the model parameters.

The initial values of the parameters for each simulation is set to the minimised parameters of the model. A grid search can be undertaken for each simulation instead, although this is computationally expensive and unnecessary. The minimisation function should be executed for a second time after running this function.

### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

- 1 – The measured data set together with the corresponding error set should be loaded into relax.
- 2 – Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
- 3 – To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
- 4 – The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.

- 5 – Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
- 6 – Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
- 7 – Failed simulations are removed using the techniques of model elimination.
- 8 – The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example for model-free analysis using the prompt UI mode which includes only the functions required for implementing the above steps is:

```
relax> grid_search(inc=11)
                                     # Step 2.

relax> minimise('newton')
                                     # Step 2.

relax> monte_carlo.setup(number=500)
                                     # Step 3.

relax> monte_carlo.create_data(method='
back_calc')
                                     # Step 4.

relax> monte_carlo.initial_values()
                                     # Step 5.

relax> minimise('newton')
                                     # Step 6.

relax> eliminate()
                                     # Step 7.

relax> monte_carlo.error_analysis()
                                     # Step 8.

An example for reduced spectral density mapping is:

relax> calc()
                                     # Step 2.
```

```

relax> monte_carlo.setup(number=500)
                                # Step 3.

relax> monte_carlo.create_data(method='
    back_calc')                  # Step 4.

relax> calc()

                                # Step 6.

relax> monte_carlo.error_analysis()
                                # Step 8.

```

---

## 14.2.87 monte\_carlo.off



### Synopsis

Turn the Monte Carlo simulations off.

### Defaults

**monte\_carlo.off()**

### Description

This will turn off the Monte Carlo simulations so that subsequent optimisation will operate directly on the model parameters and not on the simulations.

### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

- 1 – The measured data set together with the corresponding error set should be loaded into relax.
- 2 – Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
- 3 – To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
- 4 – The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
- 5 – Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
- 6 – Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.



7 – Failed simulations are removed using the techniques of model elimination.

8 – The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example for model-free analysis using the prompt UI mode which includes only the functions required for implementing the above steps is:

```
relax> grid_search(inc=11)
# Step 2.

relax> minimise('newton')
# Step 2.

relax> monte_carlo.setup(number=500)
# Step 3.

relax> monte_carlo.create_data(method='
back_calc') # Step 4.

relax> monte_carlo.initial_values()
# Step 5.

relax> minimise('newton')
# Step 6.

relax> eliminate()
# Step 7.

relax> monte_carlo.error_analysis()
# Step 8.

An example for reduced spectral density mapping is:

relax> calc()
# Step 2.

relax> monte_carlo.setup(number=500)
# Step 3.

relax> monte_carlo.create_data(method='
back_calc') # Step 4.

relax> calc()
# Step 6.

relax> monte_carlo.error_analysis()
# Step 8.
```

## 14.2.88 monte\_carlo.on



### Synopsis

Turn the Monte Carlo simulations on.

### Defaults

**monte\_carlo.on()**

### Description

This will turn on the Monte Carlo simulations so that subsequent optimisation will operate on the simulations rather than on the real model parameters.

### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

- 1 – The measured data set together with the corresponding error set should be loaded into relax.
- 2 – Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
- 3 – To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
- 4 – The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
- 5 – Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
- 6 – Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.

- 7 – Failed simulations are removed using the techniques of model elimination.
- 8 – The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example for model-free analysis using the prompt UI mode which includes only the functions required for implementing the above steps is:

```
relax> grid_search(inc=11)
                        # Step 2.

relax> minimise('newton')
                        # Step 2.

relax> monte_carlo.setup(number=500)
                        # Step 3.

relax> monte_carlo.create_data(method='
back_calc')           # Step 4.

relax> monte_carlo.initial_values()
                        # Step 5.

relax> minimise('newton')
                        # Step 6.

relax> eliminate()
                        # Step 7.

relax> monte_carlo.error_analysis()
                        # Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc()
                        # Step 2.

relax> monte_carlo.setup(number=500)
                        # Step 3.

relax> monte_carlo.create_data(method='
back_calc')           # Step 4.

relax> calc()
                        # Step 6.

relax> monte_carlo.error_analysis()
                        # Step 8.
```

## 14.2.89 monte\_carlo.setup



### Synopsis

Set up the Monte Carlo simulations.

### Defaults

**monte\_carlo.setup**(number=500)

### Keyword arguments

number: The number of Monte Carlo simulations.

### Description

This must be called prior to any of the other Monte Carlo functions. The effect is that the number of simulations will be set and that simulations will be turned on.

### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

- 1 – The measured data set together with the corresponding error set should be loaded into relax.
- 2 – Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
- 3 – To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
- 4 – The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
- 5 – Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).

- 6 – Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
- 7 – Failed simulations are removed using the techniques of model elimination.
- 8 – The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example for model-free analysis using the prompt UI mode which includes only the functions required for implementing the above steps is:

```
relax> grid_search(inc=11)
                                # Step 2.

relax> minimise('newton')
                                # Step 2.

relax> monte_carlo.setup(number=500)
                                # Step 3.

relax> monte_carlo.create_data(method='
    back_calc')                  # Step 4.

relax> monte_carlo.initial_values()
                                # Step 5.

relax> minimise('newton')
                                # Step 6.

relax> eliminate()
                                # Step 7.

relax> monte_carlo.error_analysis()
                                # Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc()
                                # Step 2.

relax> monte_carlo.setup(number=500)
                                # Step 3.

relax> monte_carlo.create_data(method='
    back_calc')                  # Step 4.

relax> calc()
                                # Step 6.

relax> monte_carlo.error_analysis()
                                # Step 8.
```

## 14.2.90 n\_state\_model.CoM



### Synopsis

The defunct centre of mass (CoM) analysis.

### Defaults

**n\_state\_model.CoM**(pivot\_point=[0.0, 0.0, 0.0], centre=None)

### Keyword arguments

**pivot\_point**: The pivot point of the motions between the two domains.

**centre**: Manually specify the CoM of the initial position prior to the N rotations to the positions of the N states. This is optional.

### Description

WARNING: This analysis is now defunct!

This is used for analysing the domain motion information content of the N states from the N-state model. The states do not correspond to physical states, hence nothing can be extracted from the individual states. This analysis involves the calculation of the pivot to centre of mass (pivot-CoM) order parameter and subsequent cone of motions.

For the analysis, both the pivot point and centre of mass must be specified. The supplied pivot point must be a vector of floating point numbers of length 3. If the centre of mass is supplied, it must also be a vector of floating point numbers (of length 3). If the centre of mass is not supplied, then the CoM will be calculated from the selected parts of a previously loaded structure.

### Prompt examples

To perform an analysis where the pivot is at the origin and the CoM is set to the N-terminal domain of a previously loaded PDB file (the C-terminal domain has been deselected), type:

```
relax> n_state_model.CoM()
```

To perform an analysis where the pivot is at the origin (because the real pivot has been shifted to this position) and the CoM is at the position [0, 0, 1], type one of:

```
relax> n_state_model.CoM(centre=[0, 0, 1])
```

```
relax> n_state_model.CoM(centre=[0.0, 0.0, 1
    .0])
```

```
relax> n_state_model.CoM(pivot_point=[0.0, 0
    .0, 0.0], centre=[0.0, 0.0, 1.0])
```

## 14.2.91 n\_state\_model.cone\_pdb



### Synopsis

Create a PDB file representing the cone models from the centre of mass (CoM) analysis.

### Defaults

**n\_state\_model.cone\_pdb**(cone\_type=None, scale=1.0, file='cone.pdb', dir=None, force=False)

### Keyword arguments

**cone\_type**: The type of cone model to represent.

**scale**: Value for scaling the pivot-CoM distance which the size of the cone defaults to.

**file**: The name of the PDB file.

**dir**: The directory where the file is located.

**force**: A flag which, if set to True, will overwrite the any pre-existing file.

### Description

WARNING: This analysis is now defunct!

This creates a PDB file containing an artificial geometric structure to represent the various cone models. These models include:

'diff in cone'

'diff on cone'

The model can be selected by setting the cone type to one of these values. The cone is represented as an isotropic cone with its axis parallel to the average pivot-CoM vector, the vertex placed at the pivot point of the domain motions, and the length of the edge of the cone equal to the pivot-CoM distance multiplied by the scaling factor. The resultant PDB file can subsequently read into any molecular viewer.

There are four different types of residue within the PDB. The pivot point is represented as a single carbon atom of the residue 'PIV'. The cone consists of numerous H atoms of the residue 'CON'. The average pivot-CoM vector is presented as the residue 'AVE' with one carbon atom positioned at the pivot and the other at the head of the

vector (after scaling by the scaling factor). Finally, if Monte Carlo have been performed, there will be multiple 'MCC' residues representing the cone for each simulation, and multiple 'MCA' residues representing the varying average pivot-CoM vector for each simulation.

To create the diffusion in a cone PDB representation, a uniform distribution of vectors on a sphere is generated using spherical coordinates with the polar angle defined from the average pivot-CoM vector. By incrementing the polar angle using an arccos distribution, a radial array of vectors representing latitude are created while incrementing the azimuthal angle evenly creates the longitudinal vectors. These are all placed into the PDB file as H atoms and are all connected using PDB CONECT records. Each H atom is connected to its two neighbours on the both the longitude and latitude. This creates a geometric PDB object with longitudinal and latitudinal lines representing the filled cone.

---

## 14.2.92 n\_state\_model.elim\_no\_prob



### Synopsis

Eliminate the structures or states with no probability.

### Defaults

`n_state_model.elim_no_prob()`

### Description

This will simply remove the structures from the N-state analysis which have an optimised probability of zero.

### Prompt examples

Simply type:

```
relax> n_state_model.elim_no_prob(N=8)
```

### 14.2.93 `n_state_model.number_of_states`



#### Synopsis

Set the number of states in the N-state model.

#### Defaults

`n_state_model.number_of_states(N=1)`

#### Keyword arguments

**N:** The number of states.

#### Description

Prior to optimisation, the number of states in the N-state model can be specified. If the number of states is not set, then this parameter will be equal to the number of loaded structures - the ensemble size.

#### Prompt examples

To set up an 8-state model, type:

```
relax> n_state_model.number_of_states(N=8)
```

### 14.2.94 `n_state_model.ref_domain`



#### Synopsis

Set the reference domain for the ‘2-domain’ N-state model.

#### Defaults

`n_state_model.ref_domain(ref=None)`

#### Keyword arguments

**ref:** The domain which will act as the frame of reference. This is only valid for the ‘2-domain’ N-state model.

#### Description

Prior to optimisation of the ‘2-domain’ N-state model, which of the two domains will act as the frame of reference must be specified. The N-states will be rotations of the other domain, so to switch the frame of reference to the other domain simply transpose the rotation matrices.

#### Prompt examples

To set up a 5-state model with ‘C’ domain being the frame of reference, type:

```
relax> n_state_model.ref_domain(ref='C')
```

## 14.2.95 `n_state_model.select_model`



### Synopsis

Select the N-state model type and set up the model.

### Defaults

```
n_state_model.select_model(model='population')
```

### Keyword arguments

`model`: The name of the preset N-state model.

### Description

Prior to optimisation, the N-state model type should be selected. The preset models are:

**‘population’** – The N-state model whereby only populations are optimised. The structures loaded into relax are assumed to be fixed, *i.e.* the orientations are not optimised, or if two domains are present the Euler angles for each state are fixed. The parameters of the model include the weight or probability for each state and the alignment tensors - {p0, p1, ..., pN, Axx, Ayy, Axy, Axz, Ayz, ...}.

**‘fixed’** – The N-state model whereby all motions are fixed and all populations are fixed to the set probabilities. The parameters of the model are simply the parameters of each alignment tensor {Axx, Ayy, Axy, Axz, Ayz, ...}.

**‘2-domain’** – The N-state model for a system of two domains, where one domain experiences a reduced tensor.

### Prompt examples

To analyse populations of states, type:

```
relax> n_state_model.select_model(model='
populations')
```

## 14.2.96 `noe.read_restraints`



### Synopsis

Read NOESY or ROESY restraints from a file.

### Defaults

```
noe.read_restraints(file=None, dir=None, proton1_col=
None, proton2_col=None, lower_col=None, upper_col=
None, sep=None)
```

### Keyword arguments

`file`: The name of the file containing the restraint data.

`dir`: The directory where the file is located.

`proton1_col`: The column containing the first proton of the NOE or ROE cross peak.

`proton2_col`: The column containing the second proton of the NOE or ROE cross peak.

`lower_col`: The column containing the lower NOE bound.

`upper_col`: The column containing the upper NOE bound.

`sep`: The column separator (the default is white space).

### Description

The format of the file will be automatically determined, for example Xplor formatted restraint files. A generically formatted file is also supported if it contains minimally four columns with the two proton names and the upper and lower bounds, as specified by the column numbers. The proton names need to be in the spin ID string format.

### Prompt examples

To read the Xplor formatted restraint file ‘NOE.xpl’, type one of:

```
relax> noe.read_restraints('NOE.xpl')
```

```
relax> noe.read_restraints(file='NOE.xpl')
```

To read the generic formatted file ‘noes’, type one of:

```
relax> noe.read_restraints(file='NOE.xpl',
proton1_col=0, proton2_col=1, lower_col
=2, upper_col=3)
```

14.2.97 **noe.spectrum\_type****Synopsis**

Set the steady-state NOE spectrum type for pre-loaded peak intensities.

**Defaults**

**noe.spectrum\_type**(spectrum\_type=None, spectrum\_id=None)

**Keyword arguments**

**spectrum\_type**: The type of steady-state NOE spectrum, one of 'ref' for the reference spectrum or 'sat' for the saturated spectrum.

**spectrum\_id**: The spectrum ID string.

**Description**

The spectrum type can be one of the following:

The steady-state NOE reference spectrum.

The steady-state NOE spectrum with proton saturation turned on.

Peak intensities should be loaded before this user function via the `spectrum.read_intensities` user function. The intensity values will then be associated with a spectrum ID string which can be used here.

14.2.98 **palmer.create****Synopsis**

Create the Modelfree4 input files.

**Defaults**

**palmer.create**(dir=None, force=False, binary='modelfree4', diff\_search='none', sims=0, sim\_type='pred', trim=0, steps=20, constraints=True, heteronuc\_type='15N', atom1='N', atom2='H', spin\_id=None)

**Keyword arguments**

**dir**: The directory to place the files.

**force**: A flag which if set to True will cause the results file to be overwritten if it already exists.

**binary**: The name of the executable Modelfree program file.

**diff\_search**: See the Modelfree4 manual for 'diffusion\_search'.

**sims**: The number of Monte Carlo simulations.

**sim\_type**: See the Modelfree4 manual.

**trim**: See the Modelfree4 manual.

**steps**: See the Modelfree4 manual.

**constraints**: A flag specifying whether the parameters should be constrained. The default is to turn constraints on (constraints=True).

**heteronuc\_type**: A three letter string describing the heteronucleus type, ie '15N', '13C', etc.

**atom1**: The symbol of the X heteronucleus in the PDB file.

**atom2**: The symbol of the H nucleus in the PDB file.

**spin\_id**: The spin identification string.

**Description**

The following files are created

'dir/mfin'

'dir/mfdata'



```
'dir/mfpar'
'dir/mfmodel'
'dir/run.sh'
```

The file 'dir/run.sh' contains the single command,

```
'modelfree4 -i mfin -d mfddata -p mfpar -m
mfmodel -o mfout -e out',
```

which can be used to execute modelfree4.

If you would like to use a different Modelfree executable file, change the binary name to the appropriate file name. If the file is not located within the environment's path, include the full path in front of the binary file name.

---

## 14.2.99 palmer.execute



### Synopsis

Perform a model-free optimisation using Modelfree4.

### Defaults

**palmer.execute**(dir=None, force=False, binary='modelfree4')

### Keyword arguments

**dir**: The directory to place the files.

**force**: A flag which if set to True will cause the results file to be overwritten if it already exists.

**binary**: The name of the executable Modelfree program file.

### Description

Modelfree 4 will be executed as

```
$ modelfree4 -i mfin -d mfddata -p mfpar -m
mfmodel -o mfout -e out
```

If a PDB file is loaded and non-isotropic diffusion is selected, then the file name will be placed on the command line as '**-s pdb\_file\_name**'.

If you would like to use a different Modelfree executable file, change the binary name to the appropriate file name. If the file is not located within the environment's path, include the full path in front of the binary file name.

---

**14.2.100 palmer.extract****Synopsis**

Extract data from the Modelfree4 ‘mfout’ star formatted file.

**Defaults**

**palmer.extract**(dir=None)

**Keyword arguments**

**dir**: The directory where the file ‘mfout’ is found.

**Description**

The model-free results will be extracted from the Modelfree4 results file ‘mfout’ located in the given directory.

---

**14.2.101 paramag.centre****Synopsis**

Specify which atom is the paramagnetic centre.

**Defaults**

**paramag.centre**(pos=None, atom\_id=None, pipe=None, verbosity=1, fix=True, ave\_pos=True, force=False)

**Keyword arguments**

**pos**: The atomic position of the paramagnetic centre.

**atom\_id**: The atom ID string.

**pipe**: The data pipe containing the structures to extract the centre from.

**verbosity**: The amount of information to print out.

**fix**: A flag specifying if the paramagnetic centre should be fixed during optimisation.

**ave\_pos**: A flag specifying if the position of the atom is to be averaged across all models.

**force**: A flag which if True will cause the current paramagnetic centre to be overwritten.

**Description**

This is required for specifying where the paramagnetic centre is located in the loaded structure file. If no structure number is given, then the average atom position will be calculated if multiple structures are loaded.

A different set of structures than those loaded into the current data pipe can also be used to determine the position, or its average. This can be achieved by loading the alternative structures into another data pipe, and then specifying that pipe.

If the average position flag is set to True, the average position from all models will be used as the position of the paramagnetic centre. If False, then the positions from all structures will be used. If multiple positions are used, then a fast paramagnetic centre motion will be assumed so that PCSs for a single tensor will be calculated for each position, and the PCS values linearly averaged.

## Prompt examples

If the paramagnetic centre is the lanthanide Dysprosium which is labelled as  $\text{Dy}$  in a loaded PDB file, then type one of:

```
relax> paramag.centre('Dy')
```

```
relax> paramag.centre(atom_id='Dy')
```

If the carbon atom 'C1' of residue '4' in the PDB file is to be used as the paramagnetic centre, then type:

```
relax> paramag.centre(':4@C1')
```

To state that the  $\text{Dy}^{3+}$  atomic position is [0.136, 12.543, 4.356], type one of:

```
relax> paramag.centre([0.136, 12.543, 4.356  
    ])
```

```
relax> paramag.centre(pos=[0.136, 12.543, 4  
    .356])
```

To find an unknown paramagnetic centre, type:

```
relax> paramag.centre(fix=False)
```

---

### 14.2.102 pcs.back\_calc



## Synopsis

Back calculate the pseudo-contact shifts.

## Defaults

```
pcs.back_calc(align_id=None)
```

## Keyword arguments

`align_id`: The alignment ID string.

## Description

This will back calculate the pseudo-contact shifts if the paramagnetic centre, temperature and magnetic field strength has been specified, an alignment tensor is present, and atomic positions have been loaded into the relax data store.

**14.2.103 pcs.calc\_q\_factors****Synopsis**

Calculate the PCS Q factor for the selected spins.

**Defaults**

`pcs.calc_q_factors(spin_id=None)`

**Keyword arguments**

**spin\_id:** The spin ID string for restricting to subset of all selected spins.

**Description**

For this to work, the back-calculated PCS data must first be generated by the analysis specific code. Otherwise a warning will be given.

**Prompt examples**

To calculate the PCS Q factor for only the spins '@H26', '@H27', and '@H28', type one of:

```
relax> pcs.calc_q_factors('@H26 & @H27 &
    @H28')
```

```
relax> pcs.calc_q_factors(spin_id='@H26 &
    @H27 & @H28')
```

**14.2.104 pcs.copy****Synopsis**

Copy PCS data from one data pipe to another.

**Defaults**

`pcs.copy(pipe_from=None, pipe_to=None, align_id=None)`

**Keyword arguments**

**pipe\_from:** The name of the pipe to copy the PCS data from.

**pipe\_to:** The name of the pipe to copy the PCS data to.

**align\_id:** The alignment ID string.

**Description**

This function will copy PCS data from 'pipe\_from' to 'pipe\_to'. If align\_id is not given then all PCS data will be copied, otherwise only a specific data set will be.

**Prompt examples**

To copy all PCS data from pipe 'm1' to pipe 'm9', type one of:

```
relax> pcs.copy('m1', 'm9')
```

```
relax> pcs.copy(pipe_from='m1', pipe_to='m9'
    )
```

```
relax> pcs.copy('m1', 'm9', None)
```

```
relax> pcs.copy(pipe_from='m1', pipe_to='m9'
    , align_id=None)
```

To copy only the 'Th' PCS data from 'm3' to 'm6', type one of:

```
relax> pcs.copy('m3', 'm6', 'Th')
```

```
relax> pcs.copy(pipe_from='m3', pipe_to='m6'
    , align_id='Th')
```

---

14.2.105 pcs.corr\_plot**Synopsis**

Generate a correlation plot of the measured vs. the back-calculated PCSs.

**Defaults**

**pcs.corr\_plot**(format='grace', file='pcs\_corr\_plot.agr', dir=None, force=False)

**Keyword arguments**

format: The format of the plot data.

file: The name of the Grace file to create.

dir: The directory name.

force: A flag which if True will cause the file to be overwritten.

**Description**

Two formats are currently supported. If format is set to 'grace', then a Grace plot file will be created. If the format is not set then a plain text list of the measured and back-calculated data will be created.

**Prompt examples**

To create a Grace plot of the data, type:

```
relax> pcs.corr_plot()
```

To create a plain text list of the measured and back-calculated data, type one of:

```
relax> pcs.corr_plot(None)
```

```
relax> pcs.corr_plot(format=None)
```

## 14.2.106 pcs.delete

**Synopsis**

Delete the PCS data corresponding to the alignment ID.

**Defaults**

**pcs.delete**(align\_id=None)

**Keyword arguments**

align\_id: The alignment ID string of the data to delete.

**Description**

This will delete all PCS data associated with the alignment ID in the current data pipe.

**Prompt examples**

To delete the PCS data corresponding to align\_id='PH\_gel', type:

```
relax> pcs.delete('PH_gel')
```

---

**14.2.107 pcs.display****Synopsis**

Display the PCS data corresponding to the alignment ID.

**Defaults**

`pcs.display`(align\_id=None, bc=False)

**Keyword arguments**

**align\_id**: The alignment ID string.

**bc**: A flag which if set will display the back-calculated rather than measured RDCs.

**Description**

This will display all of the PCS data associated with the alignment ID in the current data pipe.

**Prompt examples**

To display the ‘phage’ PCS data, type:

```
relax> pcs.display('phage')
```

**14.2.108 pcs.read****Synopsis**

Read the PCS data from file.

**Defaults**

`pcs.read`(align\_id=None, file=None, dir=None, spin\_id\_col=None, mol\_name\_col=None, res\_num\_col=None, res\_name\_col=None, spin\_num\_col=None, spin\_name\_col=None, data\_col=None, error\_col=None, sep=None, spin\_id=None)

**Keyword arguments**

**align\_id**: The alignment ID string.

**file**: The name of the file containing the PCS data.

**dir**: The directory where the file is located.

**spin\_id\_col**: The spin ID string column (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col**: The molecule name column (alternative to the spin\_id\_col).

**res\_num\_col**: The residue number column (alternative to the spin\_id\_col).

**res\_name\_col**: The residue name column (alternative to the spin\_id\_col).

**spin\_num\_col**: The spin number column (alternative to the spin\_id\_col).

**spin\_name\_col**: The spin name column (alternative to the spin\_id\_col).

**data\_col**: The PCS data column.

**error\_col**: The experimental error column.

**sep**: The column separator (the default is white space).

**spin\_id**: The spin ID string to restrict the loading of data to certain spin subsets.

**Description**

This will read PCS data from a file and associate it with an alignment ID, either a new ID or a preexisting one with no PCS data.

The spin system can be identified in the file using two different formats. The first is the spin ID string column which can include the molecule name, the residue name and number, and the spin name and number. Alternatively the molecule name, residue number and name, and spin number and name columns can be supplied allowing this information to be in separate columns. Note that the numbering of columns starts at one. The spin ID can be used to restrict the reading to certain spin types, for example only  $^{15}\text{N}$  spins when only residue information is in the file.

### Prompt examples

The following commands will read the PCS data out of the file 'Tb.txt' where the columns are separated by the symbol ',', and store the PCSs under the ID 'Tb'.

```
relax> pcs.read('Tb', 'Tb.txt', sep=',')
```

To read the  $^{15}\text{N}$  and  $^1\text{H}$  PCSs from the file 'Eu.txt', where the  $^{15}\text{N}$  values are in the 4<sup>th</sup> column and the  $^1\text{H}$  in the 9<sup>th</sup>, type both the following:

```
relax> pcs.read('Tb', 'Tb.txt', spin_id='@N',  
               , res_num_col=1, data_col=4)
```

```
relax> pcs.read('Tb', 'Tb.txt', spin_id='@H',  
               , res_num_col=1, data_col=9)
```

---

## 14.2.109 pcs.set\_errors



### Synopsis

Set the errors for the PCSs.

### Defaults

```
pcs.set_errors(aligned_id=None, spin_id=None, sd=0.1)
```

### Keyword arguments

`align_id`: The optional alignment ID string.

`spin_id`: The optional spin ID string.

`sd`: The PCS standard deviation value in ppm.

### Description

If the PCS errors have not already been read from a PCS data file or if they need to be changed, then the errors can be set via this user function.

### 14.2.110 pcs.structural\_noise



#### Synopsis

Determine the PCS error due to structural noise via simulation.

#### Defaults

**pcs.structural\_noise**(align\_id=None, rmsd=0.2, sim\_num=1000, file=None, dir=None, force=False)

#### Keyword arguments

**align\_id**: The optional alignment ID string.

**rmsd**: The atomic position RMSD, in Å, to randomise the spin positions with for the simulations.

**sim\_num**: The number of simulations, N, to perform to determine the structural noise component of the PCS errors.

**file**: The optional name of the Grace file to plot the structural errors verses the paramagnetic centre to spin distances.

**dir**: The directory name to place the Grace file into.

**force**: A flag which if True will cause the file to be overwritten.

#### Description

The analysis of the pseudo-contact shift is influenced by two significant sources of noise - that of the NMR experiment and structural noise from the 3D molecular structure used. The closer the spin to the paramagnetic centre, the greater the influence of structural noise. This distance dependence is governed by the equation:

$$\text{sigma\_dist} = \frac{\sqrt{3} * \text{abs}(\text{delta}) * \text{RMSD}}{r},$$

where sigma\_dist is the distance component of the structural noise as a standard deviation, delta is the PCS value, RMSD is the atomic position root-mean-square deviation, and  $r$  is the paramagnetic centre to spin distance. When close to the paramagnetic centre, this error source

can exceed that of the NMR experiment. The equation for the angular component of the structural noise is more complicated. The PCS error is influenced by distance, angle in the alignment frame, and the magnetic susceptibility tensor.

For the simulation the following must already be set up in the current data pipe:

The position of the paramagnetic centre.

The alignment and magnetic susceptibility tensor.

The protocol for the simulation is as follows:

The lanthanide or paramagnetic centre position will be fixed. Its motion is assumed to be on the femto- to pico- and nanosecond timescales. Hence the motion is averaged over the evolution of the PCS and can be ignored.

The positions of the nuclear spins will be randomised N times. For each simulation a random unit vector will be generated. Then a random distance along the unit vector will be generated by sampling from a Gaussian distribution centered at zero, the original spin position, with a standard deviation set to the given RMSD. Both positive and negative displacements will be used.

The PCS for the randomised position will be back calculated.

The PCS standard deviation will be calculated from the N randomised PCS values.

The standard deviation will both be stored in the spin container data structure in the relax data store as well as being added to the already present PCS error (using variance addition). This will then be used in any optimisations involving the PCS.

If the alignment ID string is not supplied, the procedure will be applied to the PCS data from all alignments.



---

**14.2.111 pcs.weight****Synopsis**

Set optimisation weights on the PCS data.

**Defaults**

**pcs.weight**(align\_id=None, spin\_id=None, weight=1.0)

**Keyword arguments**

**align\_id**: The alignment ID string.

**spin\_id**: The spin ID string.

**weight**: The weighting value.

**Description**

This can be used to force the PCS to contribute more or less to the chi-squared optimisation statistic. The higher the value, the more importance the PCS will have.

**14.2.112 pcs.write****Synopsis**

Write the PCS data to file.

**Defaults**

**pcs.write**(align\_id=None, file=None, dir=None, bc=False, force=False)

**Keyword arguments**

**align\_id**: The alignment ID string.

**file**: The name of the file.

**dir**: The directory name.

**bc**: A flag which if set will write out the back-calculated rather than measured RDCs.

**force**: A flag which if True will cause the file to be overwritten.

**Description**

If no directory name is given, the file will be placed in the current working directory. The alignment ID is required for selecting which PCS data set will be written to file.

---

**14.2.113 pipe.bundle****Synopsis**

The grouping of data pipes into a bundle.

**Defaults**

`pipe.bundle(bundle=None, pipe=None)`

**Keyword arguments**

**bundle:** The pipe bundle is a special grouping or clustering of data pipes.

**pipe:** The name of the data pipe to add to the bundle.

**Description**

Data pipes can be grouped or clustered together through special structures known as pipe bundles. If the specified data pipe bundle does not currently exist, it will be created.

**Prompt examples**

To add the data pipes ‘test 1’, ‘test 2’, and ‘test 3’ to the bundle ‘first analysis’, type the following:

```
relax> pipe.bundle('first analysis 1', 'test 1')
```

```
relax> pipe.bundle('first analysis 1', 'test 2')
```

```
relax> pipe.bundle('first analysis 1', 'test 3')
```

---

**14.2.114 pipe.change\_type****Synopsis**

Change the type of the current data pipe.

**Defaults**

`pipe.change_type(pipe_type=None)`

**Keyword arguments**

**pipe\_type:** The type of data pipe.

**Description**

The data pipe type must be one of the following:

‘ct’ – Consistency testing.

‘frame order’ – Frame Order theories.

‘jw’ – Reduced spectral density mapping.

‘hybrid’ – Special hybrid pipe.

‘mf’ – Model-free analysis.

‘N-state’ – N-state model or ensemble analysis.

‘noe’ – Steady state NOE calculation.

‘relax\_disp’ – Relaxation dispersion.

‘relax\_fit’ – Relaxation curve fitting.

**Prompt examples**

To change the type of the current ‘frame order’ data pipe to the N-state model, type one of:

```
relax> pipe.change_type('N-state')
```

```
relax> pipe.change_type(pipe_type='N-state')
```

---

14.2.115 pipe.copy

## Synopsis

Copy a data pipe.

## Defaults

**pipe.copy**(pipe\_from=None, pipe\_to=None, bundle\_to=None)

## Keyword arguments

**pipe\_from**: The name of the source data pipe to copy the data from.

**pipe\_to**: The name of the target data pipe to copy the data to.

**bundle\_to**: If given, the new data pipe will be grouped into this bundle.

## Description

This allows the contents of a data pipe to be copied. If the source data pipe is not set, the current data pipe will be assumed. The target data pipe must not yet exist.

The optional bundling allows the newly created data pipe to be placed into either a new or existing data pipe bundle. If not specified, then the copied data pipe will not be associated with a bundle.

## Prompt examples

To copy the contents of the 'm1' data pipe to the 'm2' data pipe, type:

```
relax> pipe.copy('m1', 'm2')
```

```
relax> pipe.copy(pipe_from='m1', pipe_to='m2',
                '')
```

If the current data pipe is 'm1', then the following command can be used:

```
relax> pipe.copy(pipe_to='m2')
```

---

14.2.116 pipe.create

## Synopsis

Add a new data pipe to the relax data store.

## Defaults

**pipe.create**(pipe\_name=None, pipe\_type=None, bundle=None)

## Keyword arguments

**pipe\_name**: The name of the data pipe.

**pipe\_type**: The type of data pipe.

**bundle**: The optional pipe bundle is a special grouping or clustering of data pipes. If this is specified, the newly created data pipe will be added to this bundle.

## Description

The data pipe name can be any string however the data pipe type can only be one of the following:

- 'ct' – Consistency testing,
- 'frame order' – The Frame Order theories,
- 'jw' – Reduced spectral density mapping,
- 'hybrid' – A special hybrid pipe,
- 'mf' – Model-free analysis,
- 'N-state' – N-state model of domain motions,
- 'noe' – Steady state NOE calculation,
- 'relax\_disp' – Relaxation dispersion curve fitting,
- 'relax\_fit' – Relaxation curve fitting,

The pipe bundling concept is simply a way of grouping data pipes together. This is useful for a number of purposes:

The grouping or categorisation of data pipes, for example when multiple related analyses are performed.

In the auto-analyses, as all the data pipes that they spawn are bound together within the original bundle.

In the graphical user interface mode as analysis tabs are linked to specific pipe bundles.

## Prompt examples

To set up a model-free analysis data pipe with the name 'm5', type:

```
relax> pipe.create('m5', 'mf')
```

---

### 14.2.117 pipe.current



## Synopsis

Print the name of the current data pipe.

## Defaults

`pipe.current()`

## Prompt examples

To run the user function, type:

```
relax> pipe.current()
```

---

**14.2.118 pipe.delete****Synopsis**

Delete a data pipe from the relax data store.

**Defaults**

**pipe.delete**(pipe\_name=None)

**Keyword arguments**

**pipe\_name**: The name of the data pipe to delete.

**Description**

This will permanently remove the data pipe and all of its contents from the relax data store. If the pipe name is not given, then all data pipes will be deleted.

**14.2.119 pipe.display****Synopsis**

Print a list of all the data pipes.

**Defaults**

**pipe.display**()

**Prompt examples**

To run the user function, type:

**relax> pipe.display()**

**14.2.120 pipe.hybridise****Synopsis**

Create a hybrid data pipe by fusing a number of other data pipes.

**Defaults**

`pipe.hybridise(hybrid=None, pipes=None)`

**Keyword arguments**

**hybrid:** The name of the hybrid data pipe to create.

**pipes:** An array containing the names of all data pipes to hybridise.

**Description**

This user function can be used to construct hybrid models. An example of the use of a hybrid model could be if the protein consists of two independent domains. These two domains could be analysed separately, each having their own optimised diffusion tensors. The N-terminal domain data pipe could be called 'N\_sphere' while the C-terminal domain could be called 'C\_ellipsoid'. These two data pipes could then be hybridised into a single data pipe. This hybrid data pipe can then be compared via model selection to a data pipe whereby the entire protein is assumed to have a single diffusion tensor.

The requirements for data pipes to be hybridised is that the molecules, sequences, and spin systems for all the data pipes is the same, and that no spin system is allowed to be selected in two or more data pipes. The selections must not overlap to allow for rigorous statistical comparisons.

**Prompt examples**

The two data pipes 'N\_sphere' and 'C\_ellipsoid' could be hybridised into a single data pipe called 'mixed model' by typing:

```
relax> pipe.hybridise('mixed model', ['
    N_sphere', 'C_ellipsoid'])
```

```
relax> pipe.hybridise(hybrid='mixed model',
    pipes=['N_sphere', 'C_ellipsoid'])
```

**14.2.121 pipe.switch****Synopsis**

Switch between the data pipes of the relax data store.

**Defaults**

`pipe.switch(pipe_name=None)`

**Keyword arguments**

**pipe\_name:** The name of the data pipe.

**Description**

This will switch between the various data pipes within the relax data store.

**Prompt examples**

To switch to the 'ellipsoid' data pipe, type:

```
relax> pipe.switch('ellipsoid')
```

```
relax> pipe.switch(pipe_name='ellipsoid')
```

---

**14.2.122**   `pymol.cartoon`**Synopsis**

Apply the PyMOL cartoon style and colour by secondary structure.

**Defaults**

`pymol.cartoon()`

**Description**

This applies the PyMOL cartoon style which is equivalent to hiding everything and clicking on show cartoon. It also colours the cartoon with red helices, yellow strands, and green loops. The following commands are executed:

```
cmd.hide('everything', file)
cmd.show('cartoon', file)
util.cbss(file, 'red', 'yellow', 'green')
```

where file is the file name without the '.pdb' extension.

**Prompt examples**

To apply this user function, type:

```
relax> pymol.cartoon()
```

---

**14.2.123**   `pymol.clear_history`**Synopsis**

Clear the PyMOL command history.

**Defaults**

`pymol.clear_history()`

**Description**

This will clear the Pymol history from memory.

---

**14.2.124** `pymol.command`**Synopsis**

Execute a user supplied PyMOL command.

**Defaults**

`pymol.command(command=None)`

**Keyword arguments**

`command`: The PyMOL command to execute.

**Description**

This allows PyMOL commands to be passed to the program. This can be useful for automation or scripting.

**Prompt examples**

To reinitialise the PyMOL instance, type:

```
relax> pymol.command("reinitialise")
```

---

**14.2.125** `pymol.cone_pdb`**Synopsis**

Display the cone PDB geometric object.

**Defaults**

`pymol.cone_pdb(file=None)`

**Keyword arguments**

`file`: The name of the PDB file containing the cone geometric object.

**Description**

The PDB file containing the geometric object must be created using the complementary `frame_order.cone_pdb` or `n_state_model.cone_pdb` user functions.

The cone PDB file is read in using the command:

```
load file
```

The average CoM-pivot point vector, the residue 'AVE' is displayed using the commands:

```
select resn AVE  
show sticks, 'sele'  
color blue, 'sele'
```

The cone object, the residue 'CON', is displayed using the commands:

```
select resn CON  
hide ('sele')  
show sticks, 'sele'  
color white, 'sele'
```



---

## Colour

### 14.2.126 pymol.macro\_apply



#### Synopsis

Execute PyMOL macros.

#### Defaults

```
pymol.macro_apply(data_type=None, style='classic',
colour_start_name=None, colour_start_rgb=None,
colour_end_name=None, colour_end_rgb=None,
colour_list=None)
```

#### Keyword arguments

**data\_type:** The data type to map to the structure.

**style:** The style of the macro.

**colour\_start\_name:** The name of the starting colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the starting colour RGB colour array cannot be given.

**colour\_start\_rgb:** The starting colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the starting colour name cannot be given.

**colour\_end\_name:** The name of the ending colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the ending colour RGB colour array cannot be given.

**colour\_end\_rgb:** The ending colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the ending colour name cannot be given.

**colour\_list:** The colour list to search for the colour names. This can be either 'molmol' or 'x11'.

#### Description

This allows spin specific values to be mapped to a structure through PyMOL macros. Currently only the 'classic' style, which is described below, is available.

The values are coloured based on a linear colour gradient which is specified through starting and ending colours. These can either be a string to identify one of the RGB (red, green, blue) colour arrays listed in the tables below, or you can give the RGB vector itself. For example, 'white' and [1.0, 1.0, 1.0] both select the same colour. Leaving both colours unset will select the default colour gradient which for each type of analysis is described below.

When supplying the colours as strings, two lists of colours can be selected from which to match the strings. These are the default Molmol colour list and the X11 colour list, both of which are described in the tables below. The default behaviour is to first search the Molmol list and then the X11 colour list, raising an error if neither contain the name. To explicitly select these lists, set the colour list to either 'molmol' or 'x11'.

#### Model-free classic style

Creator: Edward d'Auvergne

Argument string: "classic"

**Description:** The classic style draws the backbone of a protein in a cylindrical bond style. Rather than colouring the amino acids to which the NH bond belongs, the three covalent bonds of the peptide bond from Ca to Ca in which the NH bond is located are coloured. Deselected residues are shown as black lines.

Supported data types:

Please see Table 14.19 on page 349.

#### Molmol RGB colour arrays

The following table is a list of colours used in Molmol and their corresponding RGB colour values ranging from 0 to 1.

Please see Table 14.20 on page 350.

#### X11 RGB colour arrays

The following table is the list of X11 colour names and their corresponding RGB colour values ranging from 0 to 255.

Please see Table 14.21 on page 351.

#### Prompt examples

To map the order parameter values,  $S^2$ , onto the structure using the classic style, type:

```
relax> pymol.macro_apply('s2')
```

```
relax> pymol.macro_apply(data_type='s2')
```

```
relax> pymol.macro_apply(data_type='s2',  
    style="classic")
```

---

## 14.2.127 pymol.macro\_run



### Synopsis

Open and execute the PyMOL macro file.

### Defaults

`pymol.macro_run(file=None, dir='pymol')`

### Keyword arguments

`file`: The name of the PyMOL macro file.

`dir`: The directory name.

### Description

This user function is for opening and running a PyMOL macro located within a text file.

### Prompt examples

To execute the macro file 's2.pml' located in the directory 'pymol', type:

```
relax> pymol.macro_run(file='s2.pml')
```

```
relax> pymol.macro_run(file='s2.pml', dir='  
    pymol')
```

## 14.2.128 pymol.macro\_write



### Synopsis

Create PyMOL macros.

### Defaults

**pymol.macro\_write**(data\_type=None, style='classic', colour\_start\_name=None, colour\_start\_rgb=None, colour\_end\_name=None, colour\_end\_rgb=None, colour\_list=None, file=None, dir='pymol', force=False)

### Keyword arguments

**data\_type**: The data type to map to the structure.

**style**: The style of the macro.

**colour\_start\_name**: The name of the starting colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the starting colour RGB colour array cannot be given.

**colour\_start\_rgb**: The starting colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the starting colour name cannot be given.

**colour\_end\_name**: The name of the ending colour of the linear colour gradient. This can be either one of the X11 or one of the Molmol colour names listed in the description. If this is set, then the ending colour RGB colour array cannot be given.

**colour\_end\_rgb**: The ending colour of the linear colour gradient. This is an RGB colour array with values ranging from 0 to 1. If this is set, then the ending colour name cannot be given.

**colour\_list**: The colour list to search for the colour names. This can be either 'molmol' or 'x11'.

**file**: The optional name of the file.

**dir**: The optional directory to save the file to.

**force**: A flag which, if set to True, will cause the file to be overwritten.

### Description

This allows residues specific values to be mapped to a structure through the creation of a PyMOL macro which can be executed in PyMOL by clicking on 'File, Macro, Execute User...'. Currently only the 'classic' style, which is described below, is available.

### Colour

The values are coloured based on a linear colour gradient which is specified through starting and ending colours. These can either be a string to identify one of the RGB (red, green, blue) colour arrays listed in the tables below, or you can give the RGB vector itself. For example, 'white' and [1.0, 1.0, 1.0] both select the same colour. Leaving both colours unset will select the default colour gradient which for each type of analysis is described below.

When supplying the colours as strings, two lists of colours can be selected from which to match the strings. These are the default Molmol colour list and the X11 colour list, both of which are described in the tables below. The default behaviour is to first search the Molmol list and then the X11 colour list, raising an error if neither contain the name. To explicitly select these lists, set the colour list to either 'molmol' or 'x11'.

### Model-free classic style

Creator: Edward d'Auvergne

Argument string: "classic"

Description: The classic style draws the backbone of a protein in a cylindrical bond style. Rather than colouring the amino acids to which the NH bond belongs, the three covalent bonds of the peptide bond from Ca to Ca in which the NH bond is located are coloured. Deselected residues are shown as black lines.

Supported data types:

Please see Table 14.19 on page 349.

### Molmol RGB colour arrays

The following table is a list of colours used in Molmol and their corresponding RGB colour values ranging from 0 to 1.

Please see Table 14.20 on page 350.

### X11 RGB colour arrays

The following table is the list of X11 colour names and their corresponding RGB colour values ranging from 0 to 255.

Please see Table 14.21 on page 351.

### Prompt examples

To create a PyMOL macro mapping the order parameter values,  $S^2$ , onto the structure using the classic style, type:

```
relax> pymol.macro_write('s2')
```

```
relax> pymol.macro_write(data_type='s2')

relax> pymol.macro_write(data_type='s2',
    style="classic", file='s2.pml', dir='
    pymol')
```

---

### 14.2.129 pymol.tensor\_pdb



#### Synopsis

Display the diffusion tensor PDB geometric object over the loaded PDB.

#### Defaults

**pymol.tensor\_pdb**(file=None)

#### Keyword arguments

**file**: The name of the PDB file containing the tensor geometric object.

#### Description

In executing this user function, a PDB file must have previously been loaded into this data pipe a geometric object or polygon representing the Brownian rotational diffusion tensor will be overlain with the loaded PDB file and displayed within PyMOL. The PDB file containing the geometric object must be created using the complementary `structure.create_diff_tensor_pdb` user function.

The tensor PDB file is read in using the command:

```
load file
```

The centre of mass residue 'COM' is displayed using the commands:

```
select resn COM
```

```
show dots, 'sele'
```

```
color blue, 'sele'
```

The axes of the diffusion tensor, the residue 'AXS', is displayed using the commands:

```
select resn AXS
```

```
hide ('sele')
```

```
show sticks, 'sele'
```

```
color cyan, 'sele'
```

label 'sele', name

The simulation axes, the residues 'SIM', are displayed using the commands:

```
select resn SIM
```

```
colour cyan, 'sele'
```

---

### 14.2.130 pymol.vector\_dist



#### Synopsis

Display the PDB file representation of the XH vector distribution.

#### Defaults

**pymol.vector\_dist**(file='XH\_dist.pdb')

#### Keyword arguments

**file**: The name of the PDB file containing the vector distribution.

#### Description

A PDB file of the macromolecule must have previously been loaded as the vector distribution will be overlain with the macromolecule within PyMOL. The PDB file containing the vector distribution must be created using the complementary `structure.create_vector_dist` user function.

The vector distribution PDB file is read in using the command:

```
load file
```

---

**14.2.131** `pymol.view`**Synopsis**

View the collection of molecules from the loaded PDB file.

**Defaults**

`pymol.view()`

**Description**

This will simply launch Pymol.

**Prompt examples**

```
relax> pymol.view()
```

---

**14.2.132** `rdc.back_calc`**Synopsis**

Back calculate the residual dipolar couplings.

**Defaults**

`rdc.back_calc(align_id=None)`

**Keyword arguments**

`align_id`: The alignment ID string.

**Description**

This will back calculate the residual dipolar couplings (RDCs) if an alignment tensor is present and inter-dipole vectors have been loaded into the relax data store.

---

14.2.133 rdc.calc\_q\_factors

## Synopsis

Calculate the RDC Q factor for the selected spins.

## Defaults

`rdc.calc_q_factors(spin_id=None)`

## Keyword arguments

`spin_id`: The spin ID string for restricting to subset of all selected spins.

## Description

For this to work, the back-calculated RDC data must first be generated by the analysis specific code. Otherwise a warning will be given.

## Prompt examples

To calculate the RDC Q factor for only the spins '@H26', '@H27', and '@H28', type one of:

```
relax> rdc.calc_q_factors('@H26 & @H27 &
                           @H28')
```

```
relax> rdc.calc_q_factors(spin_id='@H26 &
                           @H27 & @H28')
```

---

14.2.134 rdc.copy

## Synopsis

Copy RDC data from one data pipe to another.

## Defaults

`rdc.copy(pipe_from=None, pipe_to=None, align_id=None)`

## Keyword arguments

`pipe_from`: The name of the pipe to copy the RDC data from.

`pipe_to`: The name of the pipe to copy the RDC data to.

`align_id`: The alignment ID string.

## Description

This function will copy RDC data from 'pipe\_from' to 'pipe\_to'. If `align_id` is not given then all RDC data will be copied, otherwise only a specific data set will be.

## Prompt examples

To copy all RDC data from pipe 'm1' to pipe 'm9', type one of:

```
relax> rdc.copy('m1', 'm9')
```

```
relax> rdc.copy(pipe_from='m1', pipe_to='m9'
                 )
```

```
relax> rdc.copy('m1', 'm9', None)
```

```
relax> rdc.copy(pipe_from='m1', pipe_to='m9'
                 , align_id=None)
```

To copy only the 'Th' RDC data from 'm3' to 'm6', type one of:

```
relax> rdc.copy('m3', 'm6', 'Th')
```

```
relax> rdc.copy(pipe_from='m3', pipe_to='m6'
                 , align_id='Th')
```

---

**14.2.135 rdc.corr\_plot****Synopsis**

Generate a correlation plot of the measured vs. the back-calculated RDCs.

**Defaults**

**rdc.corr\_plot**(format='grace', file='rdc\_corr\_plot.agr', dir=None, force=False)

**Keyword arguments**

**format**: The format of the plot data.

**file**: The name of the Grace file to create.

**dir**: The directory name.

**force**: A flag which if True will cause the file to be overwritten.

**Description**

Two formats are currently supported. If format is set to 'grace', then a Grace plot file will be created. If the format is not set then a plain text list of the measured and back-calculated data will be created.

**Prompt examples**

To create a Grace plot of the data, type:

```
relax> rdc.corr_plot()
```

To create a plain text list of the measured and back-calculated data, type one of:

```
relax> rdc.corr_plot(None)
```

```
relax> rdc.corr_plot(format=None)
```

**14.2.136 rdc.delete****Synopsis**

Delete the RDC data corresponding to the alignment ID.

**Defaults**

**rdc.delete**(align\_id=None)

**Keyword arguments**

**align\_id**: The alignment ID string of the data to delete.

**Description**

This will delete all RDC data associated with the alignment ID in the current data pipe.

**Prompt examples**

To delete the RDC data corresponding to align\_id='PH\_gel', type:

```
relax> rdc.delete('PH_gel')
```



---

**14.2.137 rdc.display****Synopsis**

Display the RDC data corresponding to the alignment ID.

**Defaults**

**rdc.display**(align\_id=None, bc=False)

**Keyword arguments**

**align\_id**: The alignment ID string.

**bc**: A flag which if set will display the back-calculated rather than measured RDCs.

**Description**

This will display all of the RDC data associated with the alignment ID in the current data pipe.

**Prompt examples**

To display the 'phage' RDC data, type:

```
relax> rdc.display('phage')
```

---

**14.2.138 rdc.read****Synopsis**

Read the RDC data from file.

**Defaults**

**rdc.read**(align\_id=None, file=None, dir=None, data\_type='D', spin\_id1\_col=1, spin\_id2\_col=2, data\_col=None, error\_col=None, sep=None, neg\_g\_corr=False, absolute=False)

**Keyword arguments**

**align\_id**: The alignment ID string.

**file**: The name of the file containing the RDC data.

**dir**: The directory where the file is located.

**data\_type**: Specify if the RDC data is in the D or 2D format, or the T = J + D format.

**spin\_id1\_col**: The spin ID string column for the first spin.

**spin\_id2\_col**: The spin ID string column for the second spin.

**data\_col**: The RDC data column.

**error\_col**: The experimental error column.

**sep**: The column separator (the default is white space).

**neg\_g\_corr**: A flag which is used to correct for the negative gyromagnetic ratio of  $^{15}\text{N}$ . If set to True, all RDC values will be inverted prior to being stored in the relax data store.

**absolute**: A flag which indicates that the loaded RDCs are are signless.

**Description**

This will read RDC data from a file and associate it with an alignment ID, either a new ID or a preexisting one with no RDC data.

The data type is used to specify how the RDC is defined. It can be set to a number of values:

'D' means that the splitting in the aligned sample was taken as J + D.

‘2D’ means that the splitting in the aligned sample was assumed to be  $J + 2D$ .

‘T’ means that the file contains  $T = J + D$  values.

Internally, relax uses the D notation. Therefore if set to ‘2D’, the values will be doubled when read in. If the ‘T’ data type is specified, then J couplings must be present for this data to be of any use.

If the negative gyromagnetic ratio correction flag is set, a sign inversion will be applied to all RDC values to be loaded. This is sometimes needed for  $^{15}\text{N}$  if the data is not compensated for the negative gyromagnetic ratio.

The absolute RDCs flag is used for RDCs in which the sign is unknown. All absolute RDCs loaded will be converted to positive values.

## Prompt examples

The following commands will read the RDC data out of the file ‘Tb.txt’ where the columns are separated by the symbol ‘,’ and store the RDCs under the ID ‘Tb’:

```
relax> rdc.read('Tb', 'Tb.txt', sep=',')
```

If the individual spin RDC errors are located in the file ‘rdc\_err.txt’ in column number 5, then to read these values into relax, assuming  $J + D$  was measured, type one of:

```
relax> rdc.read('phage', 'rdc_err.txt',
               data_type='D', error_col=5)
```

```
relax> rdc.read(aligned_id='phage', file='
               rdc_err.txt', data_type='D', error_col
               =5)
```

## 14.2.139 rdc.set\_errors



### Synopsis

Set the errors for the RDCs.

### Defaults

```
rdc.set_errors(aligned_id=None, spin_id1=None, spin_id2=
None, sd=1.0)
```

### Keyword arguments

**aligned\_id**: The optional alignment ID string.

**spin\_id1**: The optional spin ID string of the first spin.

**spin\_id2**: The optional spin ID string of the second spin.

**sd**: The RDC standard deviation value in Hertz.

### Description

If the RDC errors have not already been read from a RDC data file or if they need to be changed, then the errors can be set via this user function.

---

**14.2.140 rdc.weight****Synopsis**

Set optimisation weights on the RDC data.

**Defaults**

**rdc.weight**(align\_id=None, spin\_id=None, weight=1.0)

**Keyword arguments**

**align\_id**: The alignment ID string.

**spin\_id**: The spin ID string.

**weight**: The weighting value.

**Description**

This can be used to force the RDC to contribute more or less to the chi-squared optimisation statistic. The higher the value, the more importance the RDC will have.

**14.2.141 rdc.write****Synopsis**

Write the RDC data to file.

**Defaults**

**rdc.write**(align\_id=None, file=None, dir=None, bc=False, force=False)

**Keyword arguments**

**align\_id**: The alignment ID string.

**file**: The name of the file.

**dir**: The directory name.

**bc**: A flag which if set will write out the back-calculated rather than measured RDCs.

**force**: A flag which if True will cause the file to be overwritten.

**Description**

If no directory name is given, the file will be placed in the current working directory. The alignment ID is required for selecting which RDC data set will be written to file.

**14.2.142 relax\_data.back\_calc****Synopsis**

Back calculate the relaxation data at the given frequency.

**Defaults**

**relax\_data.back\_calc**(ri\_id=None, ri\_type=None, frq=None)

**Keyword arguments**

**ri\_id**: The relaxation data ID string.

**ri\_type**: The relaxation data type, ie 'R1', 'R2', or 'NOE'.

**frq**: The spectrometer frequency in Hz.

**Description**

This allows relaxation data of the given type and frequency to be back calculated from the model parameter values. If the relaxation data ID, type and frequency are not given, then relaxation data matching that currently loaded in the relax data store will be back-calculated.

**14.2.143 relax\_data.copy****Synopsis**

Copy relaxation data from one pipe to another.

**Defaults**

**relax\_data.copy**(pipe\_from=None, pipe\_to=None, ri\_id=None)

**Keyword arguments**

**pipe\_from**: The name of the pipe to copy the relaxation data from.

**pipe\_to**: The name of the pipe to copy the relaxation data to.

**ri\_id**: The relaxation data ID string.

**Description**

This will copy relaxation data from one data pipe to another. If the relaxation ID data string is not given then all relaxation data will be copied, otherwise only a specific data set will be copied.

**Prompt examples**

To copy all relaxation data from pipe 'm1' to pipe 'm9', type one of:

```
relax> relax_data.copy('m1', 'm9')
```

```
relax> relax_data.copy(pipe_from='m1',
    pipe_to='m9')
```

```
relax> relax_data.copy('m1', 'm9', None)
```

```
relax> relax_data.copy(pipe_from='m1',
    pipe_to='m9', ri_id=None)
```

To copy only the NOE relaxation data with the ID string of 'NOE\_800' from 'm3' to 'm6', type one of:

```
relax> relax_data.copy('m3', 'm6', 'NOE_800'
    )
```

```
relax> relax_data.copy(pipe_from='m3',
    pipe_to='m6', ri_id='NOE_800')
```

---

**14.2.144** `relax_data.delete`**Synopsis**

Delete the data corresponding to the relaxation data ID string.

**Defaults**

`relax_data.delete(ri_id=None)`

**Keyword arguments**

`ri_id`: The relaxation data ID string.

**Description**

The relaxation data corresponding to the given relaxation data ID string will be removed from the current data pipe.

**Prompt examples**

To delete the relaxation data corresponding to the ID 'NOE\_600', type:

```
relax> relax_data.delete('NOE_600')
```

---

**14.2.145** `relax_data.display`**Synopsis**

Display the data corresponding to the relaxation data ID string.

**Defaults**

`relax_data.display(ri_id=None)`

**Keyword arguments**

`ri_id`: The relaxation data ID string.

**Description**

This will display the relaxation data corresponding to the given ID.

**Prompt examples**

To display the NOE relaxation data at 600 MHz with the ID string 'NOE\_600', type:

```
relax> relax_data.display('NOE_600')
```

### 14.2.146 `relax_data.peak_intensity_type`



#### Synopsis

Specify if heights or volumes were used to measure the peak intensities.

#### Defaults

`relax_data.peak_intensity_type(ri_id=None, type='height')`

#### Keyword arguments

`ri_id`: The relaxation data ID string.

`type`: The peak intensity type.

#### Description

This is essential for BMRB data deposition. It is used to specify whether peak heights or peak volumes were measured. The two currently allowed values for the peak intensity type are `'height'` and `'volume'`.

### 14.2.147 `relax_data.read`



#### Synopsis

Read  $R_1$ ,  $R_2$ , NOE, or  $R_{2eff}$  relaxation data from a file.

#### Defaults

`relax_data.read(ri_id=None, ri_type=None, frq=None, file=None, dir=None, spin_id_col=None, mol_name_col=None, res_num_col=None, res_name_col=None, spin_num_col=None, spin_name_col=None, data_col=None, error_col=None, sep=None, spin_id=None)`

#### Keyword arguments

`ri_id`: The relaxation data ID string. This must be a unique identifier.

`ri_type`: The relaxation data type, i.e. `'R1'`, `'R2'`, `'NOE'`, or `'R2eff'`.

`frq`: The exact proton frequency of the spectrometer in Hertz. See the `'sfrq'` parameter in the Varian procpvar file or the `'SF01'` parameter in the Bruker acquis file.

`file`: The name of the file containing the relaxation data.

`dir`: The directory where the file is located.

`spin_id_col`: The spin ID string column (an alternative to the mol, res, and spin name and number columns).

`mol_name_col`: The molecule name column (alternative to the spin\_id\_col).

`res_num_col`: The residue number column (alternative to the spin\_id\_col).

`res_name_col`: The residue name column (alternative to the spin\_id\_col).

`spin_num_col`: The spin number column (alternative to the spin\_id\_col).

`spin_name_col`: The spin name column (alternative to the spin\_id\_col).

`data_col`: The relaxation data column.

`error_col`: The experimental error column.

`sep`: The column separator (the default is white space).

`spin_id`: The spin ID string to restrict the loading of data to certain spin subsets.

## Description

This will load the relaxation data into the relax data store. The data is associated with the spectrometer frequency in Hertz. For subsequent analysis, this frequency must be set to the exact field strength. This value is stored in the 'sfrq' parameter in the Varian procar file or the 'SF01' parameter in the Bruker acquis file.

The spin system can be identified in the file using two different formats. The first is the spin ID string column which can include the molecule name, the residue name and number, and the spin name and number. Alternatively the molecule name, residue number, residue name, spin number and/or spin name columns can be supplied allowing this information to be in separate columns. Note that the numbering of columns starts at one. The spin ID string can be used to restrict the reading to certain spin types, for example only  $^{15}\text{N}$  spins when only residue information is in the file.

## Prompt examples

The following commands will read the protein NOE relaxation data collected at 600 MHz out of a file called 'noe.600.out' where the residue numbers, residue names, data, errors are in the first, second, third, and forth columns respectively.

```
relax> relax_data.read('NOE_600', 'NOE', 599
    .7 * 1e6, 'noe.600.out', res_num_col=1,
    res_name_col=2, data_col=3, error_col
    =4)
```

```
relax> relax_data.read(ri_id='NOE_600',
    ri_type='NOE', frq=600.0 * 1e6, file='
    noe.600.out', res_num_col=1,
    res_name_col=2, data_col=3, error_col
    =4)
```

The following commands will read the  $R_2$  data out of the file 'r2.out' where the residue numbers, residue names, data, errors are in the second, third, fifth, and sixth columns respectively. The columns are separated by commas.

```
relax> relax_data.read('R2_800', 'R2', 8.0 *
    1e8, 'r2.out', res_num_col=2,
    res_name_col=3, data_col=5, error_col
    =6, sep=',')
```

```
relax> relax_data.read(ri_id='R2_800',
    ri_type='R2', frq=8.0*1e8, file='r2.out
    ', res_num_col=2, res_name_col=3,
    data_col=5, error_col=6, sep=',')
```

The following commands will read the  $R_1$  data out of the file 'r1.out' where the columns are separated by the symbol '%'

```
relax> relax_data.read('R1_300', 'R1', 300.1
    * 1e6, 'r1.out', sep='%')
```

## 14.2.148 relax\_data.temp\_calibration



## Synopsis

Specify the per-experiment temperature calibration method used.

## Defaults

`relax_data.temp_calibration(ri_id=None, method=None)`

## Keyword arguments

`ri_id`: The relaxation data ID string.

`method`: The per-experiment temperature calibration method.

## Description

For the proper measurement of relaxation data, per-experiment temperature calibration is essential. This user function is not for inputting standard MeOH/ethylene glycol/etc. calibration of a spectrometer - this temperature setting is of no use when you are running experiments which pump in large amounts of power into the probe head.

The  $R_1$  experiment should be about the same temperature as a HSQC and hence be close to the standard MeOH/ethylene glycol spectrometer calibration. However the  $R_2$  CPMG or spin lock and, to a lesser extent, the NOE pre-saturation pump a lot more power into the probe head. The power differences can either cause the temperature in the sample to be too high or too low. This is unpredictable as the thermometer used by the VT unit is next to the coils in the probe head and not inside the NMR sample. So the VT unit tries to control the temperature inside the probe head rather than in the NMR sample. However between the thermometer and the sample is the water of the sample, the glass of the NMR tube, the air gap where the VT unit controls air flow and the outside components of the probe head protecting the electronics. If the sample, the probe head or the VT unit is changed, this will have a different affect on the per-experiment temperature. The VT unit responds differently under different conditions and may sometimes over or under compensate by a couple of degrees. Therefore each relaxation data set from each spectrometer requires a per-experiment calibration.

Specifying the per-experiment calibration method is needed for BMRB data deposition. The currently allowed methods are:

```
'methanol',
'monoethylene glycol',
'no calibration applied'.
```

Other methods will be accepted if supplied.

---

## 14.2.149 relax\_data.temp\_control



### Synopsis

Specify the temperature control method used.

### Defaults

**relax\_data.temp\_control**(ri\_id=None, method=None)

### Keyword arguments

**ri\_id**: The relaxation data ID string.

**method**: The control method.

### Description

For the proper measurement of relaxation data, explicit temperature control techniques are essential. A number of factors can cause significant temperature fluctuations between individual relaxation experiments. This includes the daily temperature cycle of the room housing the spectrometer, different amounts of power for the individual experiments, etc.

The best methods for eliminating such problems are single scan interleaving and temperature compensation block. Single scan interleaving is the most powerful technique for averaging the temperature fluctuations not only across different experiments, but also across the entire measurement time. The application of off-resonance temperature compensation blocks at the start of the experiment is useful for the  $R_2$  and will normalise the temperature between the individual experiments, but single scan or single fid interleaving is nevertheless required for normalising the temperature across the entire measurement.

Specifying the temperature control method is needed for BMRB data deposition. The currently allowed methods are:

```
'single scan interleaving',
'temperature compensation block',
'single scan interleaving and temperature
compensation block',
'single fid interleaving',
'single experiment interleaving',
'no temperature control applied'.
```



---

**14.2.150 relax\_data.type****Synopsis**

Set the type of relaxation data.

**Defaults**

**relax\_data.type**(ri\_id=None, ri\_type=None)

**Keyword arguments**

**ri\_id**: The relaxation data ID string of the data to set the frequency of.

**ri\_type**: The relaxation data type, i.e. 'R1', 'R2', or 'NOE'.

**Description**

This allows the type associated with the relaxation data to be either set or reset. This type must be one of 'R1', 'R2', or 'NOE'.

**14.2.151 relax\_data.write****Synopsis**

Write relaxation data to a file.

**Defaults**

**relax\_data.write**(ri\_id=None, file=None, dir=None, bc=False, force=False)

**Keyword arguments**

**ri\_id**: The relaxation data ID string.

**file**: The name of the file.

**dir**: The directory name.

**bc**: A flag which if True will cause the back-calculated data to be written to the file.

**force**: A flag which if True will cause the file to be overwritten.

**Description**

If no directory name is given, the file will be placed in the current working directory. The relaxation data ID string is required for selecting which relaxation data to write to file.

**14.2.152 relax\_disp.catia\_execute****Synopsis**

Perform a relaxation dispersion optimisation using Flemming Hansen's CATIA.

**Defaults**

**relax\_disp.catia\_execute**(dir=None, binary='catia')

**Keyword arguments**

**dir**: The directory containing all of the CATIA input files.

**binary**: The name of the executable CATIA program file.

**Description**

CATIA will be executed as

```
$ catia < Fit.catia
```

If you would like to use a different CATIA executable file, change the binary name to the appropriate file name. If the file is not located within the environment's path, include the full path in front of the binary file name.

**14.2.153 relax\_disp.catia\_input****Synopsis**

Create the input files for Flemming Hansen's CATIA program.

**Defaults**

**relax\_disp.catia\_input**(dir='catia', force=False)

**Keyword arguments**

**dir**: The directory to place the CATIA input files, output directory, etc.

**force**: A flag which if set to True will cause the files to be overwritten if they already exist.

**Description**

This will create all of the input file required for CATIA as well as the CATIA results output directory.

---

14.2.154 `relax_disp.cluster`

## Synopsis

Define clusters of spins for joint optimisation.

## Defaults

`relax_disp.cluster(cluster_id=None, spin_id=None)`

## Keyword arguments

`cluster_id`: The cluster identification string.

`spin_id`: The spin identifier string for the spin or group of spins to add to the cluster.

## Description

In a relaxation dispersion analysis, the parameters of the model of dispersion can either be optimised for each spin system separately or a number of spins can be grouped or clustered and the dispersion model parameters optimised for all spins in the cluster together. Clusters are identified by unique ID strings. Any spins not within a cluster will be optimised separately and individually.

If the cluster ID string already exists, the spins will be added to that pre-existing cluster. If no spin ID is given, then all spins will be added to the cluster.

The special cluster ID string ‘free spins’ is reserved for the pool of non-clustered spins. This can be used to remove a spin system from an already existing cluster by specifying this cluster ID and the desired spin ID.

## Prompt examples

To add the spins ‘:10N’ and ‘:30N’ to a new cluster called ‘cluster’, type one of:

```
relax> relax_disp.cluster('cluster', ':1,30N')
```

```
relax> relax_disp.cluster(cluster_id='cluster', spin_id=':1,30N')
```

---

14.2.155 `relax_disp.cpmg_freq`

## Synopsis

Set the CPMG frequency associated with a given spectrum.

## Defaults

`relax_disp.cpmg_freq(spectrum_id=None, cpmg_freq=None)`

## Keyword arguments

`spectrum_id`: The spectrum ID string to associate the CPMG frequency to.

`cpmg_freq`: The frequency, in Hz, of the CPMG pulse train.

## Description

This allows the CPMG pulse train frequency of a given spectrum to be set. If None is given for frequency, then the spectrum will be treated as a reference spectrum.

## Prompt examples

To identify the reference spectrum called ‘reference\_spectrum’, type one of:

```
relax> relax_disp.cpmg_freq(None, 'reference_spectrum')
```

```
relax> relax_disp.cpmg_freq(cpmg_freq=None, spectrum_id='reference_spectrum')
```

To set a frequency of 200 Hz for the spectrum ‘200\_Hz\_spectrum’, type one of:

```
relax> relax_disp.cpmg_freq(200, '200_Hz_spectrum')
```

```
relax> relax_disp.cpmg_freq(cpmg_freq=200, spectrum_id='200_Hz_spectrum')
```

### 14.2.156 relax\_disp.cpmgfit- \_execute



#### Synopsis

Optimisation of the CPMG data using Art Palmer's CPMGFit program.

#### Defaults

**relax\_disp.cpmgfit.execute**(dir=None, force=False, binary='cpmgfit')

#### Keyword arguments

**dir**: The directory containing all of the CPMGFit input files. If not given, this defaults to the model name in lower case.

**force**: A flag which if set to True will cause the results files to be overwritten if they already exist.

**binary**: The name of the executable CPMGFit program file.

#### Description

CPMGFit will be executed once per spin as:

```
$ cpmgfit -grid -xmgr -f dir/spin_x.in | tee
  dir/spin_x.out
```

where *x* is replaced by each spin ID string. If you would like to use a different CPMGFit executable file, change the binary name to the appropriate file name. If the file is not located within the environment's path, be sure to include the full path in front of the binary file name so it can be found.

### 14.2.157 relax\_disp.cpmgfit\_input



#### Synopsis

Create the input files for Art Palmer's CPMGFit program.

#### Defaults

**relax\_disp.cpmgfit\_input**(dir=None, force=False, binary='cpmgfit', spin\_id=None)

#### Keyword arguments

**dir**: The directory to place the files. If not given, this defaults to the model name in lower case.

**force**: A flag which if set to True will cause the files to be overwritten if they already exist.

**binary**: The name of the executable CPMGFit program file.

**spin\_id**: The spin identification string.

#### Description

The following files are created:

```
'dir/spin_x.in',
'dir/run.sh'.
```

One CPMGFit input file is created per spin and named '**dir/spin\_x.in**', where *x* is the spin ID string. The file '**dir/run.sh**' is a batch file for executing CPMGFit for all of the spin input files. If you would like to use a different CPMGFit executable file, change the binary name to the appropriate file name. If the file is not located within the environment's path, be sure to include the full path in front of the binary name so it can be found.

**14.2.158 relax\_disp.exp\_type****Synopsis**

Select the relaxation dispersion experiment type.

**Defaults**

`relax_disp.exp_type(spectrum_id=None, exp_type='SQ CPMG')`

**Keyword arguments**

**spectrum\_id:** The spectrum ID string to associate the spin-lock field strength to.

**exp\_type:** The type of relaxation dispersion experiment performed.

**Description**

For each peak intensity set loaded into relax, the type of experiment it comes from needs to be specified. By specifying this for each spectrum ID, multiple experiment types can be analysed simultaneously. This is assuming that an appropriate dispersion model exists for the experiment combination.

The currently supported experiments include:

‘SQ CPMG’ – The single quantum (SQ) CPMG-type experiments,

‘ZQ CPMG’ – The zero quantum (ZQ) CPMG-type experiments,

‘DQ CPMG’ – The double quantum (DQ) CPMG-type experiments,

‘MQ CPMG’ – The multiple quantum (MQ) CPMG-type experiments,

‘1H SQ CPMG’ – The 1H single quantum (SQ) CPMG-type experiments,

‘1H MQ CPMG’ – The 1H multiple quantum (MQ) CPMG-type experiments,

‘R1rho’ – The R1rho-type experiments.

**Prompt examples**

To set the experiment type to ‘SQ CPMG’ for the spectrum ID ‘nu\_4500.0\_800MHz’, type one of:

```
relax> relax_disp.exp_type('nu_4500.0_800MHz', 'SQ CPMG')
```

```
relax> relax_disp.exp_type(spectrum_id='nu_4500.0_800MHz', exp_type='SQ CPMG')
```

**14.2.159 relax\_disp.insignificance****Synopsis**

Deselect all spins with insignificant dispersion.

**Defaults**

**relax\_disp.insignificance**(level=2.0)

**Keyword arguments**

**level**: The  $R2_{\text{eff}}/R1_{\text{rho}}$  value in rad/s by which to judge insignificance. If the maximum difference between two points on all dispersion curves for a spin is less than this value, that spin will be deselected.

**Description**

This can be used to deselect all spins which have insignificant dispersion profiles. The insignificance value is the  $R2_{\text{eff}}/R1_{\text{rho}}$  value in rad/s by which to judge the dispersion curves by. If the maximum difference between two points on all dispersion curves for a spin is less than this value, that spin will be deselected.

**14.2.160 relax\_disp.nessy\_input****Synopsis**

Create the input files for Michael Bieri's NESSY program.

**Defaults**

**relax\_disp.nessy\_input**(dir=None, force=False, spin\_id=None)

**Keyword arguments**

**dir**: The directory to place the file and to use as the NESSY project directory. If not given, this defaults to the current directory.

**force**: A flag which if set to True will cause the files to be overwritten if they already exist.

**spin\_id**: The spin identification string.

**Description**

This will create a single NESSY save file called 'save.NESSY'. This will contain all of the dispersion data currently loaded in the relax data store. If the directory name is not supplied, this will default to the current directory.

**14.2.161 relax\_disp.parameter\_copy****14.2.162 relax\_disp.plot\_disp\_curves****Synopsis**

Copy dispersion specific parameters values from one data pipe to another.

**Synopsis**

Create 2D Grace plots of the dispersion curves for each spin system.

**Defaults**

**relax\_disp.parameter\_copy**(pipe\_from=None, pipe\_to=None)

**Defaults**

**relax\_disp.plot\_disp\_curves**(dir='grace', num\_points=1000, extend=500.0, force=False)

**Keyword arguments**

**pipe\_from**: The name of the pipe to copy from.

**pipe\_to**: The name of the pipe to copy to.

**Keyword arguments**

**dir**: The directory name to place all of the spin system files into.

**num\_points**: The total number of points to generate the interpolated dispersion curves with. This value has no effect for the numeric CPMG-based models.

**extend**: How far to extend the interpolated dispersion curves beyond the last dispersion point, *i.e.* the nu\_CPMG frequency or spin-lock field strength value, in Hertz.

**force**: A flag which, if set to True, will cause the files to be overwritten.

**Description**

This is a special function for copying relaxation dispersion parameters from one data pipe to another. It is much more advanced than the `value.copy` user function, in that clustering is taken into account. When the destination data pipe has spin clusters defined, then the new parameter values, when required, will be averaged.

For the cluster specific parameters, *i.e.* the populations of the states and the exchange parameters, an average value will be used as the starting point. For all other parameters, the R20 values for each spin and magnetic field, as well as the parameters related to the chemical shift difference  $\Delta\nu$ , the optimised values of the previous run will be directly copied.

**Prompt examples**

To copy the CSA values from the data pipe 'm1' to 'm2', type:

```
relax> value.parameter_copy('m1', 'm2', 'csa')
'
```

**Description**

This is used to create 2D Grace plots of the dispersion curves of the nu\_CPMG frequencies or spin-lock field strength versus the R2eff/R1rho values. One file will be created per spin system with the name '`disp-x.gr`', where *x* is related to the spin ID string. For each file, one Grace graph will be produced for each experiment.

Four sets of curves of R2eff/R1rho values will be produced per experiment and per magnetic field strength. These are the experimental values, the fitted values, the interpolated dispersion curves for the fitted solution, and the residuals. Different dispersion models result in different interpolated dispersion curves. For the numeric models which use CPMG-type data, the maximum interpolation resolution is constrained by the frequency of a single CPMG block for the entire relaxation period. For all other models, the interpolation resolution is not constrained and can be as fine as desired by setting the total number of interpolation points. Interpolated curves are not produced for the 'R2eff' model as they are not necessary.

### 14.2.163 relax\_disp.plot\_exp- \_curves



#### Synopsis

Create 2D Grace plots of the exponential curves.

#### Defaults

**relax\_disp.plot\_exp\_curves**(file=None, dir='grace', force=False, norm=False)

#### Keyword arguments

**file**: The name of the file.

**dir**: The directory name.

**force**: A flag which, if set to True, will cause the file to be overwritten.

**norm**: A flag which, if set to True, will cause all graphs to be normalised to a starting value of 1. This is for the normalisation of series type data.

#### Description

This is used to create 2D Grace plots of the individual exponential curves used to find the R2eff or R1rho values. This supplements the grace.write user function which is not capable of generating these curves in a reasonable format.

### 14.2.164 relax\_disp.r2eff\_read



#### Synopsis

Read R2eff/R1rho values and errors from a file.

#### Defaults

**relax\_disp.r2eff\_read**(id=None, file=None, dir=None, disp\_frq=None, spin\_id\_col=None, mol\_name\_col=None, res\_num\_col=None, res\_name\_col=None, spin\_num\_col=None, spin\_name\_col=None, data\_col=None, error\_col=None, sep=None)

#### Keyword arguments

**id**: The partial experiment ID string to identify this data with. The full ID string will be constructed as this ID followed by an underscore and then the dispersion point value from the file.

**file**: The name of the file.

**dir**: The directory name.

**disp\_frq**: For CPMG-type data, the frequency of the CPMG pulse train. For R1rho-type data, the spin-lock field strength nu1. The units must be Hertz

**spin\_id\_col**: The spin ID string column used by the generic file format (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col**: The molecule name column used by the generic file format (alternative to the spin ID column).

**res\_num\_col**: The residue number column used by the generic file format (alternative to the spin ID column).

**res\_name\_col**: The residue name column used by the generic file format (alternative to the spin ID column).

**spin\_num\_col**: The spin number column used by the generic file format (alternative to the spin ID column).

**spin\_name\_col**: The spin name column used by the generic file format (alternative to the spin ID column).

**data\_col**: The RDC data column.

**error\_col**: The experimental error column.

**sep**: The column separator used by the generic format (the default is white space).



## Description

This will read R2eff/R1rho data directly from a file. The data will be associated with an experiment ID string. A partial ID is to be supplied and then the full ID string will be constructed as this ID followed by an underscore and then the dispersion point value from the file (as ‘%s\_%s’ % (id, disp\_point)). The full IDs must already exist and have been used to set the type of dispersion experiment the data is from, spectrometer proton frequency of the data, and if needed the time of the relaxation period.

The format of this text file must be that each row corresponds to a unique spin system and that there is one file per dispersion point (i.e. per CPMG frequency nu\_CPMG or per spin-lock field strength nu1). The file must be in columnar format and information to identify the spin must be in columns of the file.

### 14.2.165 relax\_disp.r2eff\_read\_spin



#### Synopsis

Read R2eff/R1rho values and errors for a single spin from a file.

#### Defaults

```
relax_disp.r2eff_read_spin(id=None, spin_id=None, file=
None, dir=None, disp_point_col=None, offset_col=None,
data_col=2, error_col=3, sep=None)
```

#### Keyword arguments

id: The experiment ID string to identify this data with.

spin\_id: The spin identification string.

file: The name of the file.

dir: The directory name.

disp\_point\_col: The column containing the CPMG frequency or spin-lock field strength (Hz).

offset\_col: The column containing the offset information for R1rho-type data.

data\_col: The column containing the R2eff or R1rho data.

error\_col: The column containing the R2eff or R1rho error.

sep: The column separator (the default is white space).

## Description

This will read R2eff/R1rho data for a single spin directly from a file. The data will be associated with an experiment ID string. This ID can be used for setting the type of dispersion experiment the data is from, spectrometer proton frequency of the data, and the time of the relaxation period.

The format of this text file must be that each row corresponds to a dispersion point (i.e. per CPMG frequency nu\_CPMG or per spin-lock field strength nu1) and that there is one file per unique spin system. The file must be in columnar format. For R1rho data, the dispersion point column can be substituted for the offset values in Hertz.

**14.2.166 relax\_disp.relax\_time****Synopsis**

Set the relaxation delay time associated with each spectrum.

**Defaults**

`relax_disp.relax_time(spectrum_id=None, time=0.0)`

**Keyword arguments**

`spectrum_id`: The spectrum ID string.

`time`: The time, in seconds, of the relaxation period.

**Description**

Peak intensities should be loaded before calling this user function via the `spectrum.read_intensities` user function. The intensity values will then be associated with a spectrum identifier. To associate each spectrum identifier with a time point in the relaxation curve prior to optimisation, this user function should be called.

**14.2.167 relax\_disp.select\_model****Synopsis**

Select the relaxation dispersion model.

**Defaults**

`relax_disp.select_model(model='R2eff')`

**Keyword arguments**

`model`: The type of relaxation dispersion model to fit.

**Description**

A number of different dispersion models are supported. This includes both analytic models and numerical models. Models which are independent of the experimental data type are:

**'R2eff'** – This is the model used to determine the  $R_{2eff}/R_{1\rho}$  values and errors required as the base data for all other models,

**'No  $R_{ex}$ '** – This is the model for no chemical exchange being present.

**The SQ CPMG-type experiments**

The currently supported analytic models are:

**'LM63'** – The original Luz and Meiboom (1963) 2-site fast exchange equation with parameters  $\{R_{20}, \dots, \phi_{ex}, kex\}$ ,

**'LM63 3-site'** – The original Luz and Meiboom (1963) 3-site fast exchange equation with parameters  $\{R_{20}, \dots, \phi_{ex}, kex, \phi_{ex2}, kex2\}$ ,

**'CR72'** – The reduced Carver and Richards (1972) 2-site equation for most time scales whereby the simplification  $R_{20A} = R_{20B}$  is assumed. The parameters are  $\{R_{20}, \dots, pA, dw, kex\}$ ,

**'CR72 full'** – The full Carver and Richards (1972) 2-site equation for most time scales with parameters  $\{R_{20A}, R_{20B}, \dots, pA, dw, kex\}$ ,

**'IT99'** – The Ishima and Torchia (1999) 2-site model for all time scales with  $pA \gg pB$  and with parameters  $\{R_{20}, \dots, pA, dw, kex\}$ ,

**‘TSMFK01’** – The Tollinger, Kay et al. (2001) 2-site very-slow exchange model, range of microsecond to second time scale. Applicable in the limit of slow exchange, when  $\text{—R20A-R20B—} \ll k_{\text{AB}}, k_{\text{B}} \ll 1/\tau_{\text{CP}}$ . R20A is the transverse relaxation rate of site A in the absence of exchange.  $2\tau_{\text{CP}}$  is the time between successive 180 deg. pulses. The parameters are {R20A, ..., dw,  $k_{\text{AB}}$ }.

The currently supported numeric models are:

**‘NS CPMG 2-site 3D’** – The reduced numerical solution for the 2-site Bloch-McConnell equations using 3D magnetisation vectors whereby the simplification  $\text{R20A} = \text{R20B}$  is assumed. Its parameters are {R20, ..., pA, dw, kex},

**‘NS CPMG 2-site 3D full’** – The full numerical solution for the 2-site Bloch-McConnell equations using 3D magnetisation vectors. Its parameters are {R20A, R20B, ..., pA, dw, kex},

**‘NS CPMG 2-site star’** – The reduced numerical solution for the 2-site Bloch-McConnell equations using complex conjugate matrices whereby the simplification  $\text{R20A} = \text{R20B}$  is assumed. It has the parameters {R20, ..., pA, dw, kex},

**‘NS CPMG 2-site star full’** – The full numerical solution for the 2-site Bloch-McConnell equations using complex conjugate matrices with parameters {R20A, R20B, ..., pA, dw, kex},

**‘NS CPMG 2-site expanded’** – The numerical solution for the 2-site Bloch-McConnell equations expanded using Maple by Nikolai Skrynnikov. It has the parameters {R20, ..., pA, dw, kex}.

## The MMQ CPMG-type experiments

The currently supported models are:

**‘MMQ CR72’** – The the Carver and Richards (1972) 2-site model for most time scales expanded for MMQ CPMG data by Korzhnev et al., 2004, whereby the simplification  $\text{R20A} = \text{R20B}$  is assumed. Its parameters are {R20, ..., pA, dw, dwH, kex}.

**‘NS MMQ 2-site’** – The numerical solution for the 2-site Bloch-McConnell equations for combined proton-heteronuclear SQ, ZQ, DQ, and MQ CPMG data whereby the simplification  $\text{R20A} = \text{R20B}$  is assumed. Its parameters are {R20, ..., pA, dw, dwH, kex}.

**‘NS MMQ 3-site linear’** – The numerical solution for the 3-site Bloch-McConnell equations linearised with  $k_{\text{AC}} = k_{\text{CA}} = 0$  for combined proton-heteronuclear SQ, ZQ, DQ, and MQ CPMG data whereby the simplification  $\text{R20A} = \text{R20B} = \text{R20C}$  is assumed. Its parameters are {R20, ..., pA, dw(AB), dwH(AB), kex(AB), pB, dw(BC), dwH(BC), kex(BC)}.

**‘NS MMQ 3-site’** – The numerical solution for the 3-site Bloch-McConnell equations for combined proton-heteronuclear SQ, ZQ, DQ, and MQ CPMG data whereby the simplification  $\text{R20A} = \text{R20B} = \text{R20C}$  is assumed. Its parameters are {R20, ..., pA, dw(AB), dwH(AB), kex(AB), pB, dw(BC), dwH(BC), kex(BC), kex(AC)}.

## The R1rho-type experiments

The currently supported analytic models are:

**‘M61’** – The Meiboom (1961) 2-site fast exchange equation with parameters {R1rho, ...,  $\phi_{\text{ex}}$ , kex},

**‘M61 skew’** – The Meiboom (1961) 2-site equation for all time scales with  $p_{\text{A}} \gg p_{\text{B}}$  and with parameters {R1rho, ..., pA, dw, kex},

**‘DPL94’** – The Davis, Perlman and London (1994) 2-site fast exchange equation with parameters {R1rho, ...,  $\phi_{\text{ex}}$ , kex},

**‘TP02’** – The Trott and Palmer (2002) 2-site equation for all time scales with parameters {R1rho, ..., pA, dw, kex}.

**‘TAP03’** – The Trott, Abergel and Palmer (2003) off-resonance 2-site equation for all time scales with parameters {R1rho, ..., pA, dw, kex}.

**‘MP05’** – The Miloushev and Palmer (2005) 2-site off-resonance equation for all time scales with parameters {R1rho, ..., pA, dw, kex}.

The currently supported numeric models are:

**‘NS R1rho 2-site’** – The numerical solution for the 2-site Bloch-McConnell equations using 3D magnetisation vectors whereby the simplification  $\text{R20A} = \text{R20B} = \text{R20C}$  is assumed and linearised with  $k_{\text{AC}} = k_{\text{CA}} = 0$ . Its parameters are {R1rho, ..., pA, dw(AB), kex(AB), pB, dw(BC), kex(BC)}.

**‘NS R1rho 3-site linear’** – The numerical solution for the 3-site Bloch-McConnell equations using 3D magnetisation vectors whereby the simplification  $\text{R20A} = \text{R20B} = \text{R20C}$  is assumed. Its parameters are {R1rho, ..., pA, dw, kex}.

**‘NS R1rho 3-site’** – The numerical solution for the 3-site Bloch-McConnell equations using 3D magnetisation vectors. Its parameters are {R1rho, ..., pA, dw(AB), kex(AB), pB, dw(BC), kex(BC), kex(AC)}.

## Prompt examples

To pick the 2-site fast exchange model for all selected spins, type one of:

```
relax> relax_disp.select_model('LM63')
```

```
relax> relax_disp.select_model(model='LM63')
```

### 14.2.168 relax\_disp.sherekhan- \_input



#### Synopsis

Create the input files for Adam Mazur's ShereKhan program.

#### Defaults

**relax\_disp.sherekhan\_input**(force=False, spin\_id=None)

#### Keyword arguments

**force**: A flag which if set to True will cause the files to be overwritten if they already exist.

**spin\_id**: The spin identification string.

#### Description

This creates the files required for the ShereKhan server located at <http://sherekhan.bionmr.org/>. One file per spin cluster per field strength will be created. These will be placed in the directory 'clusterx' and named 'sherekhan\_frqy.in', where *x* is the cluster index starting from 1 and *y* is the magnetic field strength index starting from 1.

### 14.2.169 relax\_disp.spin\_lock\_field



#### Synopsis

Set the relaxation dispersion spin-lock field strength (nu1).

#### Defaults

**relax\_disp.spin\_lock\_field**(spectrum\_id=None, field=None)

#### Keyword arguments

**spectrum\_id**: The spectrum ID string to associate the spin-lock field strength to.

**field**: The spin-lock field strength, nu1, in Hz.

#### Description

This sets the spin-lock field strength, nu1, for the specified R1rho spectrum in Hertz.

#### Prompt examples

To set a spin-lock field strength of 2.1 kHz for the spectrum 'nu1\_2.1kHz\_relaxT\_0.010', type one of:

```
relax> relax_disp.spin_lock_field(2100, '
nu1_2.1kHz_relaxT_0.010')
```

```
relax> relax_disp.spin_lock_field(field
=2100, spectrum_id='
nu1_2.1kHz_relaxT_0.010')
```

**14.2.170 relax\_disp.spin\_lock\_offset****Synopsis**

Set the relaxation dispersion spin-lock offset (`omega_rf`).

**Defaults**

`relax_disp.spin_lock_offset(spectrum_id=None, offset=None)`

**Keyword arguments**

`spectrum_id`: The spectrum ID string to associate the spin-lock offset to.

`offset`: The spin-lock offset, `omega_rf`, in ppm.

**Description**

This sets the spin-lock offset, `omega_rf`, for the specified R1rho spectrum in ppm.

**Prompt examples**

To set a spin-lock offset of 110.0 ppm for the spectrum 'nu1\_2.1kHz\_relaxT\_0.010', type one of:

```
relax> relax_disp.spin_lock_offset('
    nu1_2.1kHz_relaxT_0.010', 110.0)

relax> relax_disp.spin_lock_offset(
    spectrum_id='nu1_2.1kHz_relaxT_0.010',
    offset=110.0)
```

**14.2.171 relax\_disp.write\_disp\_curves****Synopsis**

Create text files of the dispersion curves for each spin system.

**Defaults**

`relax_disp.write_disp_curves(dir=None, force=False)`

**Keyword arguments**

`dir`: The directory name to place all of the spin system files into.

`force`: A flag which, if set to True, will cause the files to be overwritten.

**Description**

This is used to create text files of the dispersion curves of R2eff/R1rho values, both measured and back calculated from the optimised dispersion model. The columns of the text file will be the experiment name, the magnetic field strength (as the proton frequency in MHz), dispersion point (nu\_CPMG or the spin-lock field strength), the experimental R2eff value, the back-calculated R2eff value, and the experimental R2eff error. One file will be created per spin system with the name 'disp\_x.out', where *x* is the spin ID string.

**14.2.172 relax\_fit.relax\_time****Synopsis**

Set the relaxation delay time associated with each spectrum.

**Defaults**

`relax_fit.relax_time(time=0.0, spectrum_id=None)`

**Keyword arguments**

`time`: The time, in seconds, of the relaxation period.

`spectrum_id`: The spectrum identification string.

**Description**

Peak intensities should be loaded before calling this user function via the `spectrum.read_intensities` user function. The intensity values will then be associated with a spectrum identifier. To associate each spectrum identifier with a time point in the relaxation curve prior to optimisation, this user function should be called.

**14.2.173 relax\_fit.select\_model****Synopsis**

Select the relaxation curve type.

**Defaults**

`relax_fit.select_model(model='exp')`

**Keyword arguments**

`model`: The type of relaxation curve to fit.

**Description**

The supported relaxation experiments include the default two parameter exponential fit, selected by setting the model type to `'exp'`, and the three parameter inversion recovery experiment in which the peak intensity limit is a non-zero value, selected by setting the model to `'inv'`.

The parameters of these two models are

`'exp'` –  $[R_x, I_0]$ ,

`'inv'` –  $[R_x, I_0, I_{inf}]$ .

---

14.2.174 reset

## Synopsis

Reinitialise the relax data storage object.

## Defaults

`reset()`

## Description

All of the data of the relax data storage object will be erased and hence relax will return to its initial state.

---

14.2.175 residue.copy

## Synopsis

Copy all data associated with a residue.

## Defaults

`residue.copy(pipe_from=None, res_from=None, pipe_to=None, res_to=None)`

## Keyword arguments

**pipe\_from:** The data pipe containing the residue from which the data will be copied. This defaults to the current data pipe.

**res\_from:** The residue ID string of the residue to copy the data from.

**pipe\_to:** The data pipe to copy the data to. This defaults to the current data pipe.

**res\_to:** The residue ID string of the residue to copy the data to. If left blank, the new residue will have the same name as the old.

## Description

This will copy all the data associated with the identified residue to the new, non-existent residue. The new residue cannot currently exist.

## Prompt examples

To copy the residue data from residue 1 to the new residue 2, type:

```
relax> residue.copy(res_from=':1', res_to=':2')
```

To copy residue 1 of the molecule 'Old mol' to residue 5 of the molecule 'New mol', type:

```
relax> residue.copy(res_from='#Old mol:1',
                    res_to='#New mol:5')
```

To copy the residue data of residue 1 from the data pipe 'm1' to 'm2', assuming the current data pipe is 'm1', type:

```
relax> residue.copy(res_from=':1', pipe_to='m2')
```

```
relax> residue.copy(pipe_from='m1', res_from=':1', pipe_to='m2', res_to=':1')
```

**14.2.176** `residue.create`**Synopsis**

Create a new residue.

**Defaults**

`residue.create(res_num=None, res_name=None, mol_name=None)`

**Keyword arguments**

`res_num`: The residue number.

`res_name`: The name of the residue.

`mol_name`: The name of the molecule to add the residue to.

**Description**

Using this, a new sequence can be generated without using the sequence user functions. However if the sequence already exists, the new residue will be added to the end of the residue list (the residue numbers of this list need not be sequential). The same residue number cannot be used more than once. A corresponding single spin system will be created for this residue. The spin system number and name or additional spin systems can be added later if desired.

**Prompt examples**

The following sequence of commands will generate the sequence 1 ALA, 2 GLY, 3 LYS:

```
relax> residue.create(1, 'ALA')
```

```
relax> residue.create(2, 'GLY')
```

```
relax> residue.create(3, 'LYS')
```

**14.2.177** `residue.delete`**Synopsis**

Delete residues from the current data pipe.

**Defaults**

`residue.delete(res_id=None)`

**Keyword arguments**

`res_id`: The residue ID string.

**Description**

This can be used to delete a single or sets of residues. See the ID string documentation for more information. If spin system/atom ids are included a `RelaxError` will be raised.

**Spin ID string documentation**

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.



---

14.2.178 `residue.display`**Synopsis**

Display information about the residue(s).

**Defaults**

`residue.display(res_id=None)`

**Keyword arguments**

`res_id`: The residue ID string.

**Description**

This will display the residue data loaded into the current data pipe.

**Spin ID string documentation**

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string `'@H*'` will select the protons 'H', 'H2', 'H98'.

---

14.2.179 `residue.name`**Synopsis**

Name the residues.

**Defaults**

`residue.name(res_id=None, name=None, force=False)`

**Keyword arguments**

`res_id`: The residue ID string corresponding to one or more residues.

`name`: The new name.

`force`: A flag which if True will cause the residue to be renamed.

**Description**

This simply allows residues to be named (or renamed).

**Spin ID string documentation**

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string `'@H*'` will select the protons 'H', 'H2', 'H98'.

## Prompt examples

The following sequence of commands will rename the sequence {1 ALA, 2 GLY, 3 LYS} to {1 XXX, 2 XXX, 3 XXX}:

```
relax> residue.name(':1', 'XXX', force=True)
```

```
relax> residue.name(':2', 'XXX', force=True)
```

```
relax> residue.name(':3', 'XXX', force=True)
```

Alternatively:

```
relax> residue.name(':1,2,3', 'XXX', force=True)
```

### 14.2.180 residue.number



## Synopsis

Number the residues.

## Defaults

`residue.number(res_id=None, number=None, force=False)`

## Keyword arguments

**res\_id:** The residue ID string corresponding to a single residue.

**number:** The new residue number.

**force:** A flag which if True will cause the residue to be renumbered.

## Description

This simply allows residues to be numbered. The new number cannot correspond to an existing residue.

## Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '`@H*`' will select the protons 'H', 'H2', 'H98'.

## Prompt examples

The following sequence of commands will renumber the sequence {1 ALA, 2 GLY, 3 LYS} to {101 ALA, 102 GLY, 103 LYS}:

```
relax> residue.number(':',1', 101, force=True)
```

```
relax> residue.number(':',2', 102, force=True)
```

```
relax> residue.number(':',3', 103, force=True)
```

---

### 14.2.181 results.display



#### Synopsis

Display the results.

#### Defaults

`results.display()`

#### Description

This will print to screen (STDOUT) the results contained within the current data pipe.

---

**14.2.182 results.read****Synopsis**

Read the contents of a relax results file into the relax data store.

**Defaults**

```
results.read(file='results', dir=None)
```

**Keyword arguments**

**file:** The name of the file to read results from.

**dir:** The directory where the file is located.

**Description**

This is able to handle uncompressed, bzip2 compressed files, or gzip compressed files automatically. The full file name including extension can be supplied, however, if the file cannot be found the file with `‘.bz2’` appended followed by the file name with `‘.gz’` appended will be searched for.

---

**14.2.183 results.write****Synopsis**

Write the results to a file.

**Defaults**

```
results.write(file='results', dir='pipe_name',
compress_type=1, force=False)
```

**Keyword arguments**

**file:** The name of the file to output results to. The default is `‘results’`. Optionally this can be a file object, or any object with a `write()` method.

**dir:** The directory name.

**compress\_type:** The type of compression to use when creating the file.

**force:** A flag which if True will cause the results file to be overwritten.

**Description**

This will write the entire contents of the current data pipe into an XML formatted file. This results file can then be read back into relax at a later point in time, or transfered to another machine. This is in contrast to the `state.save` user function whereby the entire data store, including all data pipes, are saved into a similarly XML formatted file.

To place the results file in the current working directory in the prompt and scripting modes, leave the directory unset. If the directory is set to the special name `‘pipe_name’`, then the results file will be placed into a directory with the same name as the current data pipe.

The default behaviour of this function is to compress the file using bzip2 compression. If the extension `‘.bz2’` is not included in the file name, it will be added. The compression can, however, be changed to either no compression or gzip compression. This is controlled by the compression type which can be set to

- 0** – No compression (no file extension),
- 1** – bzip2 compression (`‘.bz2’` file extension),
- 2** – gzip compression (`‘.gz’` file extension).

The complementary read function will automatically handle the compressed files.

---

**14.2.184 script****Synopsis**

Execute a relax script.

**Defaults**

`script(file=None, dir=None)`

**Keyword arguments**

`file`: The name of the file containing the relaxation data.

`dir`: The directory where the file is located.

**Description**

This will execute a relax or any ordinary Python script.

**14.2.185 select.all****Synopsis**

Select all spins in the current data pipe.

**Defaults**

`select.all()`

**Description**

This will select all spins, irregardless of their current state.

**Prompt examples**

To select all spins, simply type:

```
relax> select.all()
```

### 14.2.186 `select.domain`



To select all spins of the domain 'N-dom', preserving the current selections, simply type one of:

```
relax> select.domain('N-dom', 'AND', True)
```

```
relax> select.domain(domain_id='N-dom',  
                     boolean='AND', change_all=True)
```

## Synopsis

Select all spins and interatomic data containers of a domain.

## Defaults

`select.domain(domain_id=None, boolean='AND', change_all=True)`

## Keyword arguments

**domain\_id:** The domain ID string of the domain to select.

**boolean:** The boolean operator specifying how interatomic data containers should be selected.

**change\_all:** A flag specifying if all non-matching spin and interatomic data containers should be deselected.

## Description

This will select all spins and interatomic data containers of a given domain. This is defined by the domain ID string as specified by the previously executed domain-related user functions.

## Boolean operators

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

## Prompt examples

To select all spins of the domain 'N-dom', simply type one of:

```
relax> select.domain('N-dom', change_all=  
                    True)
```

```
relax> select.domain(domain_id='N-dom',  
                    change_all=True)
```

---

### 14.2.187 `select.interatom`



#### Synopsis

Select specific interatomic data containers.

#### Defaults

`select.interatom(spin_id1=None, spin_id2=None, boolean='OR', change_all=False)`

#### Keyword arguments

**spin\_id1:** The spin ID string of the first spin of the interatomic data container.

**spin\_id2:** The spin ID string of the second spin of the interatomic data container.

**boolean:** The boolean operator specifying how interatomic data containers should be selected.

**change\_all:** A flag specifying if all other interatomic data containers should be changed.

#### Description

This is used to select specific interatomic data containers which store information about spin pairs such as RDCs, NOEs, dipole-dipole pairs involved in relaxation, etc. The 'change\_all' flag default is False meaning that all interatomic data containers currently either selected or deselected will remain that way. Setting this to True will cause all interatomic data containers not specified by the spin ID strings to be selected.

#### Boolean operators

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

#### Prompt examples

To select all N-H backbone bond vectors of a protein, assuming these interatomic data containers have been already set up, type one of:

```
relax> select.interatom('@N', '@H')
```

```
relax> select.interatom(spin_id1='@N',  
                        spin_id2='@H')
```

To select all H-H interatomic vectors of a small organic molecule, type one of:

```
relax> select.interatom('@H*', '@H*')
```

```
relax> select.interatom(spin_id1='@H*',  
                        spin_id2='@H*')
```

## 14.2.188 select.read



### Synopsis

Select the spins contained in a file.

### Defaults

`select.read(file=None, dir=None, spin_id_col=None, mol_name_col=None, res_num_col=None, res_name_col=None, spin_num_col=None, spin_name_col=None, sep=None, spin_id=None, boolean='OR', change_all=False)`

### Keyword arguments

**file:** The name of the file containing the list of spins to select.

**dir:** The directory where the file is located.

**spin\_id\_col:** The spin ID string column (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col:** The molecule name column (alternative to the spin\_id\_col).

**res\_num\_col:** The residue number column (alternative to the spin\_id\_col).

**res\_name\_col:** The residue name column (alternative to the spin\_id\_col).

**spin\_num\_col:** The spin number column (alternative to the spin\_id\_col).

**spin\_name\_col:** The spin name column (alternative to the spin\_id\_col).

**sep:** The column separator (the default is white space).

**spin\_id:** The spin ID string to restrict the loading of data to certain spin subsets.

**boolean:** The boolean operator specifying how spins should be selected.

**change\_all:** A flag specifying if all other spins should be changed.

spin number and/or spin name columns can be supplied allowing this information to be in separate columns. Note that the numbering of columns starts at one. The spin ID string can be used to restrict the reading to certain spin types, for example only  $^{15}\text{N}$  spins when only residue information is in the file.

Empty lines and lines beginning with a hash are ignored.

The 'change\_all' flag default is False meaning that all spins currently either selected or deselected will remain that way. Setting this to True will cause all spins not specified in the file to be deselected.

### Boolean operators

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

### Prompt examples

To select all residues listed with residue numbers in the first column of the file 'isolated\_peaks', type one of:

```
relax> select.read('isolated_peaks',
                  res_num_col=1)
```

```
relax> select.read(file='isolated_peaks',
                  res_num_col=1)
```

To select the spins in the second column of the relaxation data file 'r1.600' while deselecting all other spins, for example type:

```
relax> select.read('r1.600', spin_num_col=2,
                  change_all=True)
```

```
relax> select.read(file='r1.600',
                  spin_num_col=2, change_all=True)
```

### Description

The spin system can be identified in the file using two different formats. The first is the spin ID string column which can include the molecule name, the residue name and number, and the spin name and number. Alternatively the molecule name, residue number, residue name,



---

**14.2.189 select.reverse****Synopsis**

Reversal of the spin selection for the given spins.

**Defaults**

`select.reverse(spin_id=None)`

**Keyword arguments**

`spin_id`: The spin ID string.

**Description**

By supplying the spin ID string, a subset of spins can have their selection status reversed.

**Prompt examples**

To select all currently deselected spins and deselect those which are selected type:

```
relax> select.reverse()
```

---

**14.2.190 select.spin****Synopsis**

Select specific spins.

**Defaults**

`select.spin(spin_id=None, boolean='OR', change_all=False)`

**Keyword arguments**

`spin_id`: The spin ID string.

`boolean`: The boolean operator specifying how spins should be selected.

`change_all`: A flag specifying if all other spins should be changed.

**Description**

The '`change_all`' flag default is False meaning that all spins currently either selected or deselected will remain that way. Setting this to True will cause all spins not specified by the spin ID string to be selected.

**Boolean operators**

The boolean operator can be used to change how spin systems or interatomic data containers are selected. The allowed values are: 'OR', 'NOR', 'AND', 'NAND', 'XOR', 'XNOR'. The following table details how the selections will occur for the different boolean operators.

Please see Table 14.1 on page 303.

**Prompt examples**

To select only glycines and alanines, assuming they have been loaded with the names GLY and ALA, type one of:

```
relax> select.spin(spin_id=':GLY|:ALA')
```

To select residue 5 CYS in addition to the currently selected residues, type one of:

```
relax> select.spin(':5')
```

```
relax> select.spin(':5&:CYS')
```

```
relax> select.spin(spin_id=':5&:CYS')
```

**14.2.191 sequence.attach\_protons****14.2.192 sequence.copy****Synopsis**

Attach protons to all heteronuclei.

**Defaults**

`sequence.attach_protons()`

**Description**

This can be used to attach protons to all the heteronuclei in the current data pipe. For each proton, a spin container will be created.

**Prompt examples**

To attach protons, simply type:

```
relax> sequence.attach_protons()
```

**Synopsis**

Copy the molecule, residue, and spin sequence data from one data pipe to another.

**Defaults**

`sequence.copy(pipe_from=None, pipe_to=None, empty=True)`

**Keyword arguments**

**pipe\_from:** The name of the data pipe to copy the sequence data from.

**pipe\_to:** The name of the data pipe to copy the sequence data to.

**empty:** A flag which if True will create a molecule, residue, and spin sequence in the target pipe lacking all of the spin data of the source pipe. If False, then the spin data will also be copied.

**Description**

This will copy the sequence data between data pipes. The destination data pipe must not contain any sequence data. If the source and destination pipes are not specified, then both will default to the current data pipe (hence providing one is essential).

**Prompt examples**

To copy the sequence from the data pipe 'm1' to the current data pipe, type:

```
relax> sequence.copy('m1')
```

```
relax> sequence.copy(pipe_from='m1')
```

To copy the sequence from the current data pipe to the data pipe 'm9', type:

```
relax> sequence.copy(pipe_to='m9')
```

To copy the sequence from the data pipe 'm1' to 'm2', type:

```
relax> sequence.copy('m1', 'm2')
```

```
relax> sequence.copy(pipe_from='m1', pipe_to='m2')
```

---

**14.2.193 sequence.display****Synopsis**

Display sequences of molecules, residues, and/or spins.

**Defaults**

**sequence.display**(sep=None, mol\_name\_flag=True, res\_num\_flag=True, res\_name\_flag=True, spin\_num\_flag=True, spin\_name\_flag=True)

**Keyword arguments**

**sep**: The column separator (the default of None corresponds to white space).

**mol\_name\_flag**: A flag which if True will cause the molecule name column to be shown.

**res\_num\_flag**: A flag which if True will cause the residue number column to be shown.

**res\_name\_flag**: A flag which if True will cause the residue name column to be shown.

**spin\_num\_flag**: A flag which if True will cause the spin number column to be shown.

**spin\_name\_flag**: A flag which if True will cause the spin name column to be shown.

**Description**

This will print out the sequence information of all loaded spins in the current data pipe.

---

**14.2.194 sequence.read****Synopsis**

Read the molecule, residue, and spin sequence from a file.

**Defaults**

**sequence.read**(file=None, dir=None, spin\_id\_col=None, mol\_name\_col=None, res\_num\_col=None, res\_name\_col=None, spin\_num\_col=None, spin\_name\_col=None, sep=None, spin\_id=None)

**Keyword arguments**

**file**: The name of the file containing the sequence data.

**dir**: The directory where the file is located.

**spin\_id\_col**: The spin ID string column (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col**: The molecule name column (alternative to the spin\_id\_col).

**res\_num\_col**: The residue number column (alternative to the spin\_id\_col).

**res\_name\_col**: The residue name column (alternative to the spin\_id\_col).

**spin\_num\_col**: The spin number column (alternative to the spin\_id\_col).

**spin\_name\_col**: The spin name column (alternative to the spin\_id\_col).

**sep**: The column separator (the default is white space).

**spin\_id**: The spin ID string to restrict the loading of data to certain spin subsets.

**Description**

The spin system can be identified in the file using two different formats. The first is the spin ID string column which can include the molecule name, the residue name and number, and the spin name and number. Alternatively the molecule name, residue number, residue name, spin number and/or spin name columns can be supplied allowing this information to be in separate columns. Note that the numbering of columns starts at one. The spin ID string can be used to restrict the reading to certain spin types, for example only <sup>15</sup>N spins when only residue information is in the file.

## Prompt examples

The following commands will read protein backbone 15N sequence data out of a file called 'seq' where the residue numbers and names are in the first and second columns respectively:

```
relax> sequence.read('seq')
```

```
relax> sequence.read('seq', res_num_col=1,
    res_name_col=2)
```

```
relax> sequence.read(file='seq', res_num_col=
    =1, res_name_col=2, sep=None)
```

The following commands will read the residue sequence out of the file 'noe.out' which also contains the NOE values:

```
relax> sequence.read('noe.out')
```

```
relax> sequence.read('noe.out', res_num_col=
    =1, res_name_col=2)
```

```
relax> sequence.read(file='noe.out',
    res_num_col=1, res_name_col=2)
```

The following commands will read the sequence out of the file 'noe.600.out' where the residue numbers are in the second column, the names are in the sixth column and the columns are separated by commas:

```
relax> sequence.read('noe.600.out',
    res_num_col=2, res_name_col=6, sep=',')
```

```
relax> sequence.read(file='noe.600.out',
    res_num_col=2, res_name_col=6, sep=',')
```

The following commands will read the RNA residues and atoms (including C2, C5, C6, C8, N1, and N3) from the file '500.NOE', where the residue number, residue name, spin number, and spin name are in the first to fourth columns respectively:

```
relax> sequence.read('500.NOE', res_num_col=
    =1, res_name_col=2, spin_num_col=3,
    spin_name_col=4)
```

```
relax> sequence.read(file='500.NOE',
    res_num_col=1, res_name_col=2,
    spin_num_col=3, spin_name_col=4)
```

## 14.2.195 sequence.write



### Synopsis

Write the molecule, residue, and spin sequence to a file.

### Defaults

```
sequence.write(file=None, dir=None, sep=None,
mol_name_flag=True, res_num_flag=True, res_name_flag=
True, spin_num_flag=True, spin_name_flag=True, force=
False)
```

### Keyword arguments

**file:** The name of the file.

**dir:** The directory name.

**sep:** The column separator (the default of None corresponds to white space).

**mol\_name\_flag:** A flag which if True will cause the molecule name column to be shown.

**res\_num\_flag:** A flag which if True will cause the residue number column to be shown.

**res\_name\_flag:** A flag which if True will cause the residue name column to be shown.

**spin\_num\_flag:** A flag which if True will cause the spin number column to be shown.

**spin\_name\_flag:** A flag which if True will cause the spin name column to be shown.

**force:** A flag which if True will cause the file to be overwritten.

### Description

Write the sequence data to file. If no directory name is given, the file will be placed in the current working directory.

---

**14.2.196 spectrometer.frequency** $\omega$ **Synopsis**

Set the spectrometer proton frequency of the experiment.

**Defaults**

**spectrometer.frequency**(id=None, frq=None, units='Hz')

**Keyword arguments**

**id**: The experiment identification string to set the frequency of.

**frq**: The spectrometer frequency. See the 'sfrq' parameter in the Varian procpa file or the 'SF01' parameter in the Bruker acqui file.

**units**: The units of frequency.

**Description**

This allows the spectrometer frequency of a given experiment to be set. The expected units are that of the proton resonance frequency in Hertz. See the 'sfrq' parameter in the Varian procpa file or the 'SF01' parameter in the Bruker acqui file for the exact value.

---

**14.2.197 spectrometer-temperature****Synopsis**

Specify the temperature of an experiment.

**Defaults**

**spectrometer.temperature**(id=None, temp=None)

**Keyword arguments**

**id**: The experiment identification string.

**temp**: The temperature of the experiment in Kelvin.

**Description**

This allows the temperature of an experiment to be set. This value should be in Kelvin. In certain analyses, for example those which use pseudocontact shift data, knowledge of the temperature is essential. For the pseudocontact shift, the experiment ID string should match one of the alignment IDs.

### 14.2.198 spectrum.baseplane\_rmsd



#### Synopsis

Set the baseplane RMSD of a given spin in a spectrum for error analysis.

#### Defaults

`spectrum.baseplane_rmsd(error=0.0, spectrum_id=None, spin_id=None)`

#### Keyword arguments

`error`: The baseplane RMSD error value.

`spectrum_id`: The spectrum ID string.

`spin_id`: The spin ID string.

#### Description

The spectrum ID identifies the spectrum associated with the error and must correspond to a previously loaded set of intensities. If the spin ID is unset, then the error value for all spins will be set to the supplied value.

### 14.2.199 spectrum.delete



#### Synopsis

Delete the spectral data corresponding to the spectrum ID string.

#### Defaults

`spectrum.delete(spectrum_id=None)`

#### Keyword arguments

`spectrum_id`: The unique spectrum ID string.

#### Description

The spectral data corresponding to the given spectrum ID string will be removed from the current data pipe.

#### Prompt examples

To delete the peak height data corresponding to the ID 'R1 ncyc5', type:

```
relax> spectrum.delete('R1 ncyc5')
```

## 14.2.200 spectrum.error\_analysis



### Synopsis

Perform an error analysis for peak intensities.

### Defaults

`spectrum.error_analysis(subset=None)`

### Keyword arguments

**subset:** The list of spectrum ID strings to restrict the error analysis to.

### Description

This user function must only be called after all peak intensities have been loaded and all other necessary spectral information set. This includes the baseplane RMSD and the number of points used in volume integration, both of which are only used if spectra have not been replicated.

The error analysis can be restricted to a subset of the loaded spectral data. This is useful, for example, if half the spectra have been collected on one spectrometer and the other half on a different spectrometer.

Six different types of error analysis are supported depending on whether peak heights or volumes are supplied, whether noise is determined from replicated spectra or the RMSD of the baseplane noise, and whether all spectra or only a subset have been duplicated. These are:

Please see Table 14.22 on page 440.

### Peak heights with baseplane noise RMSD

When none of the spectra have been replicated, then the peak height errors are calculated using the RMSD of the baseplane noise, the value of which is set by the `spectrum.baseplane_rmsd` user function. This results in a different error per peak per spectrum. The standard deviation error measure for the peak height,  $\sigma_I$ , is set to the RMSD value.

### Peak heights with partially replicated spectra

When spectra are replicated, the variance for a single spin at a single replicated spectra set is calculated by the formula

$$\sigma^2 = \text{sum}(\{I_i - I_{av}\}^2) / (n - 1),$$

where  $\sigma^2$  is the variance,  $\sigma$  is the standard deviation,  $n$  is the size of the replicated spectra set with  $i$  being the corresponding index,  $I_i$  is the peak intensity for spectrum  $i$ , and  $I_{av}$  is the mean over all spectra i.e. the sum of all peak intensities divided by  $n$ .

As the value of  $n$  in the above equation is always very low since normally only a couple of spectra are collected per replicated spectra set, the variance of all spins is averaged for a single replicated spectra set. Although this results in all spins having the same error, the accuracy of the error estimate is significantly improved.

If there are in addition to the replicated spectra loaded peak intensities which only consist of a single spectrum, i.e. not all spectra are replicated, then the variances of replicated replicated spectra sets will be averaged. This will be used for the entire experiment so that there will be only a single error value for all spins and for all spectra.

### Peak heights with all spectra replicated

If all spectra are collected in duplicate (triplicate or higher number of spectra are supported), the each replicated spectra set will have its own error estimate. The error for a single peak is calculated as when partially replicated spectra are collected, and these are again averaged to give a single error per replicated spectra set. However as all replicated spectra sets will have their own error estimate, variance averaging across all spectra sets will not be performed.

### Peak volumes with baseplane noise RMSD

The method of error analysis when no spectra have been replicated and peak volumes are used is highly dependent on the integration method. Many methods simply sum the number of points within a fixed region, either a box or oval object. The number of points used,  $N$ , must be specified by another user function in this class. Then the error is simply given by the sum of variances:

$$\sigma_{vol}^2 = \sigma_i^2 * N,$$

where  $\sigma_{vol}$  is the standard deviation of the volume,  $\sigma_i$  is the standard deviation of a single point assumed to be equal to the RMSD of the baseplane noise, and  $N$  is the total number of points used in the summation integration method. For a box integration method,

Table 14.22: The six peak intensity error analysis types.

| Int type | Noise source                           | Error scope                          |
|----------|--|--------------------------------------|
| Heights  | RMSD baseplane                         | One sigma per peak per spectrum      |
| Heights  | Partial duplicate + variance averaging | One sigma for all peaks, all spectra |
| Heights  | All replicated + variance averaging    | One sigma per replicated spectra set |
| Volumes  | RMSD baseplane                         | One sigma per peak per spectrum      |
| Volumes  | Partial duplicate + variance averaging | One sigma for all peaks, all spectra |
| Volumes  | All replicated + variance averaging    | One sigma per replicated spectra set |

this converts to the Nicholson, Kay, Baldissieri, Arango, Young, Bax, and Torchia (1992) Biochemistry, 31: 5253-5263 equation:

$$\text{sigma\_vol} = \text{sigma\_i} * \sqrt{n*m},$$

where  $n$  and  $m$  are the dimensions of the box. Note that a number of programs, for example peakint ([http://hugin.ethz.ch/wuthrich/software/xeasy/xeasy\\_m15.html](http://hugin.ethz.ch/wuthrich/software/xeasy/xeasy_m15.html)) does not use all points within the box. And if the number  $N$  can not be determined, this category of error analysis is not possible.

Also note that non-point summation methods, for example when line shape fitting is used to determine peak volumes, the equations above cannot be used. Hence again this category of error analysis cannot be used. This is the case for one of the three integration methods used by Sparky (<http://www.cgl.ucsf.edu/home/sparky/manual/peaks.html#Integration>). And if fancy techniques are used, for example as Cara does to deconvolute overlapping peaks (<http://www.cara.ethz.ch/Wiki/Integration>), this again makes this error analysis impossible.

## Peak volumes with partially replicated spectra

When peak volumes are measured by any integration method and a few of the spectra are replicated, then the intensity errors are calculated identically as described in the ‘Peak heights with partially replicated spectra’ section above.

## Peak volumes with all spectra replicated

With all spectra replicated and again using any integration methodology, the intensity errors can be calculated as described in the ‘Peak heights with all spectra replicated’ section above.

## 14.2.201 spectrum.integration\_points



### Synopsis

Set the number of summed points used in volume integration of a given spin in a spectrum.

### Defaults

**spectrum.integration\_points**( $N=\text{None}$ ,  $\text{spectrum\_id}=\text{None}$ ,  $\text{spin\_id}=\text{None}$ )

### Keyword arguments

**N**: The number of points used by the summation volume integration method.

**spectrum\_id**: The spectrum ID string.

**spin\_id**: Restrict setting the number to certain spins.

### Description

For a complete description of which integration methods and how many points  $N$  are used for different integration techniques, please see the `spectrum.error_analysis` user function documentation.

The spectrum ID identifies the spectrum associated with the value of  $N$  and must correspond to a previously loaded set of intensities. If the spin ID is unset, then the number of summed points for all spins will be set to the supplied value.



### 14.2.202 spectrum.read-intensities



#### Synopsis

Read peak intensities from a file.

#### Defaults

**spectrum.read\_intensities**(file=None, dir=None, spectrum\_id=None, dim=1, int\_method='height', int\_col=None, spin\_id\_col=None, mol\_name\_col=None, res\_num\_col=None, res\_name\_col=None, spin\_num\_col=None, spin\_name\_col=None, sep=None, spin\_id=None, ncproc=None)

#### Keyword arguments

**file**: The name of the file containing the intensity data.

**dir**: The directory where the file is located.

**spectrum\_id**: The unique spectrum ID string or list of strings to associate with the peak intensity values. If 'auto' is provided for a NMRPipe seriesTab formatted file, the IDs are auto generated in form of Z\_A{i}.

**dim**: Associate the data with the spins of any dimension in the peak list. This defaults to w1, the heteronucleus in HSQC type experiments.

**int\_method**: The method by which peaks were integrated.

**int\_col**: The optional column containing the peak intensity data (used by the generic intensity file format, or if the intensities are in a non-standard column).

**spin\_id\_col**: The spin ID string column used by the generic intensity file format (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col**: The molecule name column used by the generic intensity file format (alternative to the spin ID column).

**res\_num\_col**: The residue number column used by the generic intensity file format (alternative to the spin ID column).

**res\_name\_col**: The residue name column used by the generic intensity file format (alternative to the spin ID column).

**spin\_num\_col**: The spin number column used by the generic intensity file format (alternative to the spin ID column).

**spin\_name\_col**: The spin name column used by the generic intensity file format (alternative to the spin ID column).

**sep**: The column separator used by the generic intensity format (the default is white space).

**spin\_id**: The spin ID string used to restrict the loading of data to certain spin subsets.

**ncproc**: The Bruker specific FID intensity scaling factor.

#### Description

The peak intensity can either be from peak heights or peak volumes.

The spectrum ID is a label which is subsequently utilised by other user functions. If this identifier matches that of a previously loaded set of intensities, then this indicates a replicated spectrum.

The spectral dimension is used to specify if the intensity data should be loaded into the spins identified by the first dimension w1, second dimension w2, etc.

The integration method is required for the subsequent error analysis. When peak heights are measured, this should be set to 'height'. Volume integration methods are a bit varied and hence two values are accepted. If the volume integration involves pure point summation, with no deconvolution algorithms or other methods affecting peak heights, then the value should be set to 'point sum'. All other volume integration methods, e.g. line shape fitting, the value should be set to 'other'.

If a series of intensities extracted from Bruker FID files processed in Topspin or XWinNMR are to be compared, the ncproc parameter may need to be supplied. This is because this FID is stored using integer representation and is scaled using ncproc to avoid numerical truncation artifacts. If two spectra have significantly different maximal intensities, then ncproc will be different for both. The intensity scaling is binary, i.e.  $2^{**ncproc}$ . Therefore if spectrum A has an ncproc of 6 and spectrum B a value of 7, then a reference intensity in B will be double that of A. Internally, relax stores the intensities scaled by  $2^{**ncproc}$ .

#### File formats

The peak list or intensity file will be automatically determined.

**Sparky peak list**: The file should be a Sparky peak list saved after typing the command 'lt'. The default is to assume that columns 0, 1, 2, and 3 (1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, and 4<sup>th</sup>) contain the Sparky assignment, w1, w2, and peak intensity data respectively. The frequency data w1 and w2 are ignored while the peak intensity data can either be the peak height or volume displayed by changing the window options. If the peak intensity data is not within column 3, set the integration column to the appropriate number (column numbering starts from 0 rather than 1).

XEasy peak list: The file should be the saved XEasy text window output of the list peak entries command, 'tw' followed by 'le'. As the columns are fixed, the peak intensity column is hardwired to number 10 (the 11<sup>th</sup> column) which contains either the peak height or peak volume data. Because the columns are fixed, the integration column number will be ignored.

NMRView: The file should be a NMRView peak list. The default is to use column 16 (which contains peak heights) for peak intensities. To use peak volumes (or evolumes), `int_col` must be set to 15.

NMRPipe seriesTab: The file should be a NMRPipe-format Spectral Series list. If the `spectrum_id='auto'`, the IDs are auto generated in form of `Z-A{i}`.

Generic intensity file: This is a generic format which can be created by scripting to support non-supported peak lists. It should contain in the first few columns enough information to identify the spin. This can include columns for the molecule name, residue number, residue name, spin number, and spin name. Alternatively a spin ID string column can be used. The peak intensities can be placed in another column specified by the integration column number. Intensities from multiple spectra can be placed into different columns, and these can then be specified simultaneously by setting the integration column value to a list of columns. This list must be matched by setting the spectrum ID to a list of the same length. If columns are delimited by a character other than whitespace, this can be specified with the column separator. The spin ID can be used to restrict the loading to specific spin subsets.

## Prompt examples

To read the reference and saturated spectra peak heights from the Sparky formatted files 'ref.list' and 'sat.list', type:

```
relax> spectrum.read_intensities(file='
    ref.list', spectrum_id='ref')
```

```
relax> spectrum.read_intensities(file='
    sat.list', spectrum_id='sat')
```

To read the reference and saturated spectra peak heights from the XEasy formatted files 'ref.text' and 'sat.text', type:

```
relax> spectrum.read_intensities(file='
    ref.text', spectrum_id='ref')
```

```
relax> spectrum.read_intensities(file='
    sat.text', spectrum_id='sat')
```

## 14.2.203 spectrum.read\_spins



### Synopsis

Read peak assignments from a file and create spins.

### Defaults

```
spectrum.read_spins(file=None, dir=None, dim=1,
    spin_id_col=None, mol_name_col=None, res_num_col=
    None, res_name_col=None, spin_num_col=None,
    spin_name_col=None, sep=None, spin_id=None)
```

### Keyword arguments

`file`: The name of the file containing the intensity data.

`dir`: The directory where the file is located.

`dim`: Associate the data with the spins of any dimension in the peak list. This defaults to w1, the heteronucleus in HSQC type experiments.

`spin_id_col`: The spin ID string column used by the generic intensity file format (an alternative to the mol, res, and spin name and number columns).

`mol_name_col`: The molecule name column used by the generic intensity file format (alternative to the spin ID column).

`res_num_col`: The residue number column used by the generic intensity file format (alternative to the spin ID column).

`res_name_col`: The residue name column used by the generic intensity file format (alternative to the spin ID column).

`spin_num_col`: The spin number column used by the generic intensity file format (alternative to the spin ID column).

`spin_name_col`: The spin name column used by the generic intensity file format (alternative to the spin ID column).

`sep`: The column separator used by the generic intensity format (the default is white space).

`spin_id`: The spin ID string used to restrict the loading of data to certain spin subsets.

### Description

The spectral dimension is used to specify if the intensity data should be loaded into the spins identified by the first dimension w1, second dimension w2, etc.

## File formats

The peak list or intensity file will be automatically determined.

**Sparky peak list:** The file should be a Sparky peak list saved after typing the command 'lt'. The default is to assume that columns 0, 1, 2, and 3 (1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, and 4<sup>th</sup>) contain the Sparky assignment, w1, w2, and peak intensity data respectively. The frequency data w1 and w2 are ignored while the peak intensity data can either be the peak height or volume displayed by changing the window options. If the peak intensity data is not within column 3, set the integration column to the appropriate number (column numbering starts from 0 rather than 1).

**XEasy peak list:** The file should be the saved XEasy text window output of the list peak entries command, 'tw' followed by 'le'. As the columns are fixed, the peak intensity column is hardwired to number 10 (the 11<sup>th</sup> column) which contains either the peak height or peak volume data. Because the columns are fixed, the integration column number will be ignored.

**NMRView:** The file should be a NMRView peak list. The default is to use column 16 (which contains peak heights) for peak intensities. To use use peak volumes (or evolumes), int\_col must be set to 15.

**NMRPipe seriesTab:** The file should be a NMRPipe-format Spectral Series list. If the spectrum\_id='auto', the IDs are auto generated in form of Z\_A{i}.

**Generic intensity file:** This is a generic format which can be created by scripting to support non-supported peak lists. It should contain in the first few columns enough information to identify the spin. This can include columns for the molecule name, residue number, residue name, spin number, and spin name. Alternatively a spin ID string column can be used. The peak intensities can be placed in another column specified by the integration column number. Intensities from multiple spectra can be placed into different columns, and these can then be specified simultaneously by setting the integration column value to a list of columns. This list must be matched by setting the spectrum ID to a list of the same length. If columns are delimited by a character other than whitespace, this can be specified with the column separator. The spin ID can be used to restrict the loading to specific spin subsets.

## Prompt examples

To read the spin assignments from the Sparky formatted files 'ref.list' and 'sat.list', type:

```
relax> spectrum.read_spins(file='ref.list')

relax> spectrum.read_spins(file='sat.list')
```

To read the spin assignments from the XEasy formatted files 'ref.text' and 'sat.text', type:

```
relax> spectrum.read_spins(file='ref.text')

relax> spectrum.read_spins(file='sat.text')
```

## 14.2.204 spectrum.replicated



### Synopsis

Specify which spectra are replicates of each other.

### Defaults

`spectrum.replicated(spectrum_ids=None)`

### Keyword arguments

`spectrum_ids`: The list of replicated spectra ID strings.

### Description

This is used to identify which of the loaded spectra are replicates of each other. Specifying the replicates is essential for error analysis if the baseplane RMSD has not been supplied.

### Prompt examples

To specify that the NOE spectra labelled 'ref1', 'ref2', and 'ref3' are the same spectrum replicated, type one of:

```
relax> spectrum.replicated(['ref1', 'ref2',
                             'ref3'])

relax> spectrum.replicated(spectrum_ids=['
ref1', 'ref2', 'ref3'])
```

To specify that the two R<sub>2</sub> spectra 'ncyc2' and 'ncyc2b' are the same time point, type:

```
relax> spectrum.replicated(['ncyc2', 'ncyc2b
'])
```

## 14.2.205 spin.copy



## Synopsis

Copy all data associated with a spin.

## Defaults

`spin.copy(pipe_from=None, spin_from=None, pipe_to=None, spin_to=None)`

## Keyword arguments

**pipe\_from:** The data pipe containing the spin from which the data will be copied. This defaults to the current data pipe.

**spin\_from:** The spin identifier string of the spin to copy the data from.

**pipe\_to:** The data pipe to copy the data to. This defaults to the current data pipe.

**spin\_to:** The spin identifier string of the spin to copy the data to. If left blank, the new spin will have the same name as the old.

## Description

This will copy all the data associated with the identified spin to the new, non-existent spin. The new spin must not already exist.

## Prompt examples

To copy the spin data from spin 1 to the new spin 2, type:

```
relax> spin.copy(spin_from='@1', spin_to='@2')
'
```

To copy spin 1 of the molecule 'Old mol' to spin 5 of the molecule 'New mol', type:

```
relax> spin.copy(spin_from='#Old mol@1',
                 spin_to='#New mol@5')
```

To copy the spin data of spin 1 from the data pipe 'm1' to 'm2', assuming the current data pipe is 'm1', type:

```
relax> spin.copy(spin_from='@1', pipe_to='m2')
'
```

```
relax> spin.copy(pipe_from='m1', spin_from='@1',
                 pipe_to='m2', spin_to='@1')
```

## 14.2.206 spin.create



## Synopsis

Create a new spin.

## Defaults

`spin.create(spin_name=None, spin_num=None, res_name=None, res_num=None, mol_name=None)`

## Keyword arguments

**spin\_name:** The name of the spin.

**spin\_num:** The spin number.

**res\_name:** The name of the residue to add the spin to.

**res\_num:** The number of the residue to add the spin to.

**mol\_name:** The name of the molecule to add the spin to.

## Description

This will add a new spin data container to the relax data storage object. The same spin number cannot be used more than once.

## Prompt examples

The following sequence of commands will add the spins 1 C4, 2 C9, 3 C15 to residue number 10:

```
relax> spin.create('C4', 1, res_num=10)
```

```
relax> spin.create('C9', 2, res_num=10)
```

```
relax> spin.create('C15', 3, res_num=10)
```

---

### 14.2.207 spin.create\_pseudo



contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

#### Synopsis

Create a spin system representing a pseudo-atom.

#### Prompt examples

The following will create the pseudo-atom named 'Q9' consisting of the protons '@H16', '@H17', '@H18':

```
relax> spin.create_pseudo('Q9', members=['@H16', '@H17', '@H18'])
```

#### Defaults

`spin.create_pseudo(spin_name=None, spin_num=None, res_id=None, members=None, averaging='linear')`

#### Keyword arguments

**spin\_name:** The name of the pseudo-atom spin.

**spin\_num:** The spin number.

**res\_id:** The molecule and residue ID string identifying the position to add the pseudo-spin to.

**members:** A list of the atoms (as spin ID strings) that the pseudo-atom is composed of.

**averaging:** The positional averaging technique.

#### Description

This will create a spin data container representing a number of pre-existing spin containers as a pseudo-atom. The optional spin number must not already exist.

#### Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '<mol\_name>', the name of the molecule, '<res\_id>', the residue identifier which can be a number, name, or range of numbers, '<atom\_id>', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not

---

**14.2.208 spin.delete****Synopsis**

Delete spins.

**Defaults**

`spin.delete(spin_id=None)`

**Keyword arguments**

`spin_id`: The spin identifier string.

**Description**

This can be used to delete a single or sets of spins. See the identification string documentation below for more information.

**Spin ID string documentation**

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string `'@H*'` will select the protons 'H', 'H2', 'H98'.

---

**14.2.209 spin.display****Synopsis**

Display information about the spin(s).

**Defaults**

`spin.display(spin_id=None)`

**Keyword arguments**

`spin_id`: The spin identification string.

**Description**

This will display the spin data loaded into the current data pipe.

**Spin ID string documentation**

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string `'@H*'` will select the protons 'H', 'H2', 'H98'.

---

### 14.2.210 `spin.element`



#### Prompt examples

The set all spins of residue 1 to be carbons, type one of:

```
relax> spin.element('@1', 'C', force=True)
```

```
relax> spin.element(spin_id='@1', element='C', force=True)
```

#### Synopsis

Set the element type of the spin.

#### Defaults

```
spin.element(element=None, spin_id=None, force=False)
```

#### Keyword arguments

**element:** The IUPAC element name.

**spin\_id:** The spin identification string corresponding to one or more spins.

**force:** A flag which if True will cause the element to be changed.

#### Description

This allows the element type of the spins to be set.

#### Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

---

### 14.2.211 `spin.isotope`



#### Synopsis

Set the spins' nuclear isotope type.

#### Defaults

`spin.isotope(isotope=None, spin_id=None, force=False)`

#### Keyword arguments

**isotope:** The nuclear isotope name in the AE notation - the atomic mass number followed by the element symbol.

**spin\_id:** The spin identification string corresponding to one or more spins.

**force:** A flag which if True will cause the nuclear isotope to be changed.

#### Description

This allows the nuclear isotope type of the spins to be set.

#### Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '`@H*`' will select the protons '`H`', '`H2`', '`H98`'.

#### Prompt examples

The set all spins of residue 1 to the '`13C`' nuclear isotope, type one of:



```
relax> spin.isotope('@1', '13C', force=True)
```

```
relax> spin.isotope(spin_id='@1', isotope='13C', force=True)
```



---

### 14.2.212 spin.name



#### Synopsis

Name the spins.

#### Defaults

`spin.name(name=None, spin_id=None, force=False)`

#### Keyword arguments

**name:** The new name.

**spin\_id:** The spin identification string corresponding to one or more spins.

**force:** A flag which if True will cause the spin to be renamed.

#### Description

This simply allows spins to be named (or renamed). Spin naming often essential. For example when reading Sparky peak list files, then the spin name must match that in the file.

#### Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.



#### Prompt examples

The following sequence of commands will rename the sequence {1 C1, 2 C2, 3 C3} to {1 C11, 2 C12, 3 C13}:

```
relax> spin.name('@1', 'C11', force=True)
```

```
relax> spin.name('@2', 'C12', force=True)
```

```
relax> spin.name('@3', 'C13', force=True)
```

### 14.2.213 spin.number



#### Prompt examples

The following sequence of commands will renumber the sequence {1 C1, 2 C2, 3 C3} to {-1 C1, -2 C2, -3 C3}:

```
relax> spin.number('@1', -1, force=True)
```

```
relax> spin.number('@2', -2, force=True)
```

```
relax> spin.number('@3', -3, force=True)
```

#### Synopsis

Number the spins.

#### Defaults

`spin.number(spin_id=None, number=None, force=False)`

#### Keyword arguments

**spin\_id:** The spin identification string corresponding to a single spin.

**number:** The new spin number.

**force:** A flag which if True will cause the spin to be renumbered.

#### Description

This simply allows spins to be numbered. The new number cannot correspond to an existing spin number.

#### Spin ID string documentation

The identification string is composed of three components: the molecule ID token beginning with the '#' character, the residue ID token beginning with the ':' character, and the atom or spin system ID token beginning with the '@' character. Each token can be composed of multiple elements - one per spin - separated by the ',' character and each individual element can either be a number (which must be an integer, in string format), a name, or a range of numbers separated by the '-' character. Negative numbers are supported. The full ID string specification is `'#<mol_name> :<res_id>[, <res_id>[, <res_id>, ...]] @<atom_id>[, <atom_id>[, <atom_id>, ...]]'`, where the token elements are '`<mol_name>`', the name of the molecule, '`<res_id>`', the residue identifier which can be a number, name, or range of numbers, '`<atom_id>`', the atom or spin system identifier which can be a number, name, or range of numbers.

If one of the tokens is left out then all elements will be assumed to match. For example if the string does not contain the '#' character then all molecules will match the string. If only the molecule ID component is specified, then all spins of the molecule will match.

Regular expression can be used to select spins. For example the string '@H\*' will select the protons 'H', 'H2', 'H98'.

---

### 14.2.214 state.load



#### Synopsis

Load a saved program state.

#### Defaults

**state.load**(state='state.bz2', dir=None, force=False)

#### Keyword arguments

**state**: The file name, which can be a string or a file descriptor object, of a saved program state.

**dir**: The name of the directory in which the file is found.

**force**: A boolean flag which if True will cause the current program state to be overwritten.

#### Description

This is able to handle uncompressed, bzip2 compressed files, or gzip compressed files automatically. The full file name including extension can be supplied, however, if the file cannot be found, this function will search for the file name with `'.bz2'` appended followed by the file name with `'.gz'` appended.

For more advanced users, file descriptor objects are supported. If the force flag is set to True, then the relax data store will be reset prior to the loading of the saved state.

#### Prompt examples

The following commands will load the state saved in the file `'save'`.

```
relax> state.load('save')
```

```
relax> state.load(state='save')
```

Use one of the following commands to load the state saved in the bzip2 compressed file `'save.bz2'`:

```
relax> state.load('save')
```

```
relax> state.load(state='save')
```

```
relax> state.load('save.bz2')
```

```
relax> state.load(state='save.bz2', force=
    True)
```

---

### 14.2.215 state.save



#### Synopsis

Save the program state.

#### Defaults

**state.save**(state='state.bz2', dir=None, compress\_type=1, force=False)

#### Keyword arguments

**state**: The file name, which can be a string or a file descriptor object, to save the current program state in.

**dir**: The name of the directory in which to place the file.

**compress\_type**: The type of compression to use when creating the file.

**force**: A boolean flag which if set to True will cause the file to be overwritten.

#### Description

This will place the program state - the relax data store - into a file for later reloading or reference. The default format is an XML formatted file.

The default behaviour of this function is to compress the file using bzip2 compression. If the extension `'.bz2'` is not included in the file name, it will be added. The compression can, however, be changed to either no compression or gzip compression. This is controlled by the compression type which can be set to

0 – No compression (no file extension).

1 – bzip2 compression (`'.bz2'` file extension).

2 – gzip compression (`'.gz'` file extension).

#### Prompt examples

The following commands will save the current program state, uncompressed, into the file `'save'`:

```
relax> state.save('save', compress_type=0)
```

```
relax> state.save(state='save',
    compress_type=0)
```

The following commands will save the current program state into the bzip2 compressed file 'save.bz2':

```
relax> state.save('save')
```

```
relax> state.save(state='save')
```

```
relax> state.save('save.bz2')
```

```
relax> state.save(state='save.bz2')
```

If the file 'save' already exists, the following commands will save the current program state by overwriting the file.

```
relax> state.save('save', force=True)
```

```
relax> state.save(state='save', force=True)
```

---

## 14.2.216 structure.add\_atom



### Synopsis

Add an atom.

### Defaults

**structure.add\_atom**(atom\_name=None, res\_name=None, res\_num=None, pos=None, element=None, atom\_num=None, chain\_id=None, segment\_id=None, pdb\_record=None)

### Keyword arguments

**atom\_name**: The atom name.

**res\_name**: The residue name.

**res\_num**: The residue number.

**pos**: The atomic coordinates.

**element**: The element name.

**atom\_num**: The optional atom number.

**chain\_id**: The optional chain ID string.

**segment\_id**: The optional segment ID string.

**pdb\_record**: The optional PDB record name, e.g. 'ATOM' or 'HETATM'.

### Description

This allows atoms to be added to the internal structural object. To use the same atomic coordinates for all models, the atomic position can be an array of 3 values. Alternatively different coordinates can be used for each model if the atomic position is a rank-2 array where the first dimension matches the number of models currently present.

---

**14.2.217 structure.add\_model****Synopsis**

Add a new model.

**Defaults**

**structure.add\_model**(model\_num=None)

**Keyword arguments**

**model\_num**: The number of the new model.

**Description**

This allows new models to be added to the internal structural object. Note that no structural information is allowed to be present



---

**14.2.218 structure.connect\_atom****Synopsis**

Connect two atoms.

**Defaults**

**structure.connect\_atom**(index1=None, index2=None)

**Keyword arguments**

**index1**: The global index of the first atom.

**index2**: The global index of the second atom.

**Description**

This allows atoms to be connected in the internal structural object. The global index is normally equal to the PDB atom number minus 1.

### 14.2.219 structure.create\_diff- \_tensor\_pdb



#### Synopsis

Create a PDB file to represent the diffusion tensor.

#### Defaults

**structure.create\_diff\_tensor\_pdb**(scale=1.8e-06, file='tensor.pdb', dir=None, force=False)

#### Keyword arguments

**scale**: Value for scaling the diffusion rates.

**file**: The name of the PDB file.

**dir**: The directory to place the file into.

**force**: A flag which, if set to True, will overwrite the any pre-existing file.

#### Description

This creates a PDB file containing an artificial geometric structure to represent the diffusion tensor. A structure must have previously been read into relax. The diffusion tensor is represented by an ellipsoidal, spheroidal, or spherical geometric object with its origin located at the centre of mass (of the selected residues). This diffusion tensor PDB file can subsequently read into any molecular viewer.

There are four different types of residue within the PDB. The centre of mass of the selected residues is represented as a single carbon atom of the residue 'COM'. The ellipsoidal geometric shape consists of numerous H atoms of the residue 'TNS'. The axes of the tensor, when defined, are presented as the residue 'AXS' and consist of carbon atoms: one at the centre of mass and one at the end of each eigenvector. Finally, if Monte Carlo simulations were run and the diffusion tensor parameters were allowed to vary then there will be multiple 'SIM' residues, one for each simulation. These are essentially the same as the 'AXS' residue, representing the axes of the simulated tensors, and they will appear as a distribution.

As the Brownian rotational diffusion tensor is a measure of the rate of rotation about different axes - the larger the geometric object, the faster the diffusion of a molecule. For example the diffusion tensor of a water molecule is much larger than that of a macromolecule.

The effective global correlation time experienced by an XH bond vector, not to be confused with the Lipari and

Szabo parameter  $\tau_e$ , will be approximately proportional to the component of the diffusion tensor parallel to it. The approximation is not exact due to the multiexponential form of the correlation function of Brownian rotational diffusion. If an XH bond vector is parallel to the longest axis of the tensor, it will be unaffected by rotations about that axis, which are the fastest rotations of the molecule, and therefore its effective global correlation time will be maximal.

To set the size of the diffusion tensor within the PDB frame the unit vectors used to generate the geometric object are first multiplied by the diffusion tensor (which has the units of inverse seconds) then by the scaling factor (which has the units of second Å and has the default value of 1.8e-6 s.Å). Therefore the rotational diffusion rate per Å is equal the inverse of the scale value (which defaults to 5.56e5 s<sup>-1</sup>.Å). Using the default scaling value for spherical diffusion, the correspondence between global correlation time,  $\mathcal{Q}_{iso}$  diffusion rate, and the radius of the sphere for a number of discrete cases will be:

Please see Table 14.23 on page 455.

The scaling value has been fixed to facilitate comparisons within or between publications, but can be changed to vary the size of the tensor geometric object if necessary. Reporting the rotational diffusion rate per Å within figure legends would be useful.

To create the tensor PDB representation, a number of algorithms are utilised. Firstly the centre of mass is calculated for the selected residues and is represented in the PDB by a C atom. Then the axes of the diffusion are calculated, as unit vectors scaled to the appropriate length (multiplied by the eigenvalue  $\mathcal{Q}_x$ ,  $\mathcal{Q}_y$ ,  $\mathcal{Q}_z$ ,  $\mathcal{Q}_{||}$ ,  $\mathcal{Q}_{\perp}$ , or  $\mathcal{Q}_{iso}$  as well as the scale value), and a C atom placed at the position of this vector plus the centre of mass. Finally a uniform distribution of vectors on a sphere is generated using spherical coordinates. By incrementing the polar angle using an arccos distribution, a radial array of vectors representing latitude are created while incrementing the azimuthal angle evenly creates the longitudinal vectors. These unit vectors, which are distributed within the PDB frame and are of 1 Å in length, are first rotated into the diffusion frame using a rotation matrix (the spherical diffusion tensor is not rotated). Then they are multiplied by the diffusion tensor matrix to extend the vector out to the correct length, and finally multiplied by the scale value so that the vectors reasonably superimpose onto the macromolecular structure. The last set of algorithms place all this information into a PDB file. The distribution of vectors are represented by H atoms and are all connected using PDB CONECT records. Each H atom is connected to its two neighbours on the both the longitude and latitude. This creates a geometric PDB object with longitudinal and latitudinal lines.



### 14.2.221 `structure.create_vector_dist`



### 14.2.222 `structure.delete`



#### Synopsis

Create a PDB file representation of the distribution of XH bond vectors.

#### Defaults

`structure.create_vector_dist`(length=2e-09, file='XH\_dist.pdb', dir=None, symmetry=True, force=False)

#### Keyword arguments

**length:** The length of the vectors in the PDB representation (meters).

**file:** The name of the PDB file.

**dir:** The directory to place the file into.

**symmetry:** A flag which if True will create a second chain with reversed XH bond orientations.

**force:** A flag which if True will overwrite the file if it already exists.

#### Description

This creates a PDB file containing an artificial vectors, the length of which default to 20 Å. A structure must have previously been read into relax. The origin of the vector distribution is located at the centre of mass (of the selected residues). This vector distribution PDB file can subsequently be read into any molecular viewer.

Because of the symmetry of the diffusion tensor reversing the orientation of the XH bond vector has no effect. Therefore by setting the symmetry flag two chains 'A' and 'B' will be added to the PDB file whereby chain 'B' is chain 'A' with the XH bonds reversed.

#### Synopsis

Delete structural information.

#### Defaults

`structure.delete`(atom\_id=None)

#### Keyword arguments

**atom\_id:** The atom identification string.

#### Description

This will delete structural information from the current data pipe. All spin and sequence information loaded from these structures will be preserved - this only affects the structural data. The atom ID argument can be used to restrict deletion to parts of the loaded molecules.

#### Prompt examples

To delete everything, simply type:

```
relax> structure.delete()
```

To delete residues 50 to 100 of the molecule called 'Ap4Aase', type one of:

```
relax> structure.delete(':50-100')
```

```
relax> structure.delete(atom_id=':50-100')
```



### 14.2.223 structure.displacement



#### Synopsis

Determine the rotational and translational displacement between a set of models.

#### Defaults

**structure.displacement**(model\_from=None, model\_to=None, atom\_id=None, centroid=None)

#### Keyword arguments

**model\_from**: The optional model number for the starting position of the displacement.

**model\_to**: The optional model number for the ending position of the displacement.

**atom\_id**: The atom identification string.

**centroid**: The alternative position of the centroid.

#### Description

This user function allows the rotational and translational displacement between two models of the same structure to be calculated. The information will be printed out in various formats and held in the relax data store. This is directional, so there is a starting and ending position for each displacement. If the starting and ending models are not specified, then the displacements in all directions between all models will be calculated.

The atom ID, which uses the same notation as the spin ID strings, can be used to restrict the displacement calculation to certain molecules, residues, or atoms. This is useful if studying domain motions, secondary structure rearrangements, amino acid side chain rotations, etc.

By supplying the position of the centroid, an alternative position than the standard rigid body centre is used as the focal point of the motion. This allows, for example, a pivot of a rotational domain motion to be specified. This is not a formally correct algorithm, all translations will be zero, but does give an indication to the amplitude of the pivoting angle.

#### Prompt examples

To determine the rotational and translational displacements between all sets of models, type:

```
relax> structure.displacement()
```

To determine the displacement from model 5 to all other models, type:

```
relax> structure.displacement(model_from=5)
```

To determine the displacement of all models to model 5, type:

```
relax> structure.displacement(model_to=5)
```

To determine the displacement of model 2 to model 3, type one of:

```
relax> structure.displacement(2, 3)
```

```
relax> structure.displacement(model_from=2,
                               model_to=3)
```

**14.2.224 structure.find\_pivot****Synopsis**

Find the pivot point of the motion of a set of structures.

**Defaults**

**structure.find\_pivot**(models=None, atom\_id=None, init\_pos=None, func\_tol=1e-05, box\_limit=200)

**Keyword arguments**

**models**: The list of models to use.

**atom\_id**: The atom identification string.

**init\_pos**: The initial position of the pivot.

**func\_tol**: The function tolerance. This is used to terminate minimisation once the function value between iterations is less than the tolerance. The default value is 1e-5.

**box\_limit**: The pivot point is constrained withing a box of  $\pm x$  Åthe using the logarithmic barrier function together with simplex optimisation. This argument is the value of  $x$ .

**Description**

This is used to find pivot point of motion between a set of structural models. If the list of models is not supplied, then all models will be used.

The atom ID, which uses the same notation as the spin ID strings, can be used to restrict the search to certain molecules, residues, or atoms. For example to only use backbone heavy atoms in a protein, use the atom ID of '@N,C,CA,O', assuming those are the names of the atoms from the structural file.

By supplying the position of the centroid, an alternative position than the standard rigid body centre is used as the focal point of the superimposition. The allows, for example, the superimposition about a pivot point.

**14.2.225 structure.get\_pos****Synopsis**

Extract the atomic positions from the loaded structures for the given spins.

**Defaults**

**structure.get\_pos**(spin\_id=None, ave\_pos=True)

**Keyword arguments**

**spin\_id**: The spin identification string.

**ave\_pos**: A flag specifying if the position of the atom is to be averaged across models.

**Description**

This allows the atomic positions of the spins to be extracted from the loaded structures. This is automatically performed by the structure.load\_spins user function, but if the sequence information is generated in other ways, this user function allows the structural information to be obtained.

If averaging the atomic positions, then average position of all models will be loaded into the spin container. Otherwise the positions from all models will be loaded separately.

**Prompt examples**

For a model-free backbone amide nitrogen analysis whereby the N spins have already been created, to obtain the backbone N positions from the file '1F3Y.pdb' (which is a single protein), type the following two user functions:

```
relax> structure.read_pdb('1F3Y.pdb')
```

```
relax> structure.get_pos(spin_id='@N')
```

## 14.2.226 structure.load\_spins



## Synopsis

Load spins from the structure into the relax data store.

## Defaults

**structure.load\_spins**(spin\_id=None, mol\_name\_target=None, ave\_pos=True)

## Keyword arguments

**spin\_id**: The spin identification string for the selective loading of certain spins into the relax data store.

**mol\_name\_target**: The name of target molecule container, overriding the name of the loaded structures.

**ave\_pos**: A flag specifying if the position of the atom is to be averaged across models.

## Description

This allows a sequence to be generated within the relax data store using the atomic information from the structure already associated with this data pipe. The spin ID string is used to select which molecules, which residues, and which atoms will be recognised as spin systems within relax. If the spin ID is left unspecified, then all molecules, residues, and atoms will be placed within the data store (and all atoms will be treated as spins).

If averaging the atomic positions, then average position of all models will be loaded into the spin container. Otherwise the positions from all models will be loaded separately.

## Prompt examples

For a model-free backbone amide nitrogen analysis, to load just the backbone N sequence from the file '1F3Y.pdb' (which is a single protein), type the following two user functions:

```
relax> structure.read_pdb('1F3Y.pdb')
```

```
relax> structure.load_spins(spin_id='@N')
```

For an RNA analysis of adenine C8 and C2, guanine C8 and N1, cytidine C5 and C6, and uracil N3, C5, and C6, type the following series of commands (assuming that the PDB file with this atom naming has already been read):

```
relax> structure.load_spins(spin_id=":A@C8")
```

```
relax> structure.load_spins(spin_id=":A@C2")
```

```
relax> structure.load_spins(spin_id=":G@C8")
```

```
relax> structure.load_spins(spin_id=":G@N1")
```

```
relax> structure.load_spins(spin_id=":C@C5")
```

```
relax> structure.load_spins(spin_id=":C@C6")
```

```
relax> structure.load_spins(spin_id=":U@N3")
```

```
relax> structure.load_spins(spin_id=":U@C5")
```

```
relax> structure.load_spins(spin_id=":U@C6")
```

Alternatively using some Python programming:

```
relax> for id in [":A@C8", ":A@C2", ":G@C8",
                  ":G@N1", ":C@C5", ":C@C6", ":U@N3", ":U@C5", ":U@C6"]:
```

```
relax>     structure.load_spins(spin_id=id)
```

---

14.2.227 `structure.read_gaussian`

## Synopsis

Reading structures from Gaussian log files.

## Defaults

**structure.read\_gaussian**(file=None, dir=None, set\_mol\_name=None, set\_model\_num=None)

## Keyword arguments

**file**: The name of the Gaussian log file.

**dir**: The directory where the file is located.

**set\_mol\_name**: Set the names of the read molecules. If unset, then the molecules will be automatically labelled based on the file name or other information. This can either be a single name or a list of names.

**set\_model\_num**: Set the model numbers of the loaded molecules. This can be a single number or list of numbers.

## Description

The atomic positions from a Gaussian log file can be read into relax. If optimisation has been performed, the last set of atomic coordinates from the log will be read to obtain the final structure. The log file can be Gzip or Bzip2 compressed.

The setting of molecule names is used to name the molecules within the Gaussian file. If not set, then the molecules will be named after the file name, with the molecule number appended if more than one exists. By setting the molecule name or setting the model number, the loaded structure can be stored as a specific model or as a different molecule.

## Prompt examples

To load all structures from the Gaussian file 'taxol.log' in the directory '~/logs', including all models and all molecules, type one of:

```
relax> structure.read_gaussian('taxol.log',  
                               '~/logs')
```

```
relax> structure.read_gaussian(file='  
taxol.log', dir='logs')
```

---

14.2.228 `structure.read_pdb`

## Synopsis

Reading structures from PDB files.

## Defaults

**structure.read\_pdb**(file=None, dir=None, read\_mol=None, set\_mol\_name=None, read\_model=None, set\_model\_num=None, alt\_loc=None, merge=False)

## Keyword arguments

**file**: The name of the PDB file.

**dir**: The directory where the file is located.

**read\_mol**: If set, only the given molecule(s) will be read. The molecules are numbered consecutively from 1. If unset, then all molecules will be loaded. By providing a list of numbers such as [1, 2], multiple molecules will be read.

**set\_mol\_name**: Set the names of the read molecules. If unset, then the molecules will be automatically labelled based on the file name or other information. This can either be a single name or a list of names.

**read\_model**: If set, only the given model number(s) from the PDB file will be read. Otherwise all models will be read. This can be a single number or list of numbers.

**set\_model\_num**: Set the model numbers of the loaded molecules. If unset, then the PDB model numbers will be preserved if they exist. This can be a single number or list of numbers.

**alt\_loc**: The PDB ATOM record 'Alternate location indicator' field value.

**merge**: A flag which if set to True will try to merge the PDB structure into the currently loaded structures.

## Description

The reading of PDB files into relax is quite a flexible procedure allowing for both models, defined as an ensemble of the same molecule but with different atomic positions, and different molecules within the same model. One of more molecules can exist in one or more models. The flexibility allows PDB models to be converted into different molecules and different PDB files loaded as the same molecule but as different models.

In a PDB file, the models are specified by the MODEL PDB record. All the supported PDB readers in relax recognise this. The internal reader defines molecules using the TER PDB record. In both cases, the molecules will be numbered consecutively from 1.

Setting the molecule name allows the molecule within the PDB (within one model) to have a custom name. If not set, then the molecules will be named after the file name, with the molecule number appended if more than one exists.

Note that relax will complain if it cannot work out what to do.

This is able to handle uncompressed, bzip2 compressed files, or gzip compressed files automatically. The full file name including extension can be supplied, however, if the file cannot be found, this function will search for the file name with `‘.bz2’` appended followed by the file name with `‘.gz’` appended.

If a PDB file contains alternative atomic locations, then the alternate location indicator must be specified to allow one of the multiple coordinate sets to be select.

```
relax> structure.read_pdb('
    lactose_MCMM4_S1_1.pdb', set_mol_name='
    lactose_MCMM4_S1', set_model_num=1)
```

```
relax> structure.read_pdb('
    lactose_MCMM4_S1_2.pdb', set_mol_name='
    lactose_MCMM4_S1', set_model_num=2)
```

```
relax> structure.read_pdb('
    lactose_MCMM4_S1_3.pdb', set_mol_name='
    lactose_MCMM4_S1', set_model_num=3)
```

```
relax> structure.read_pdb('
    lactose_MCMM4_S1_4.pdb', set_mol_name='
    lactose_MCMM4_S1', set_model_num=4)
```

## Prompt examples

To load all structures from the PDB file `‘test.pdb’` in the directory `‘~/pdb’`, including all models and all molecules, type one of:

```
relax> structure.read_pdb('test.pdb', '~/pdb
    ')
```

```
relax> structure.read_pdb(file='test.pdb',
    dir='pdb')
```

To load the 10<sup>th</sup> model from the file `‘test.pdb’` and naming it `‘CaM’`, use one of:

```
relax> structure.read_pdb('test.pdb',
    read_model=10, set_mol_name='CaM')
```

```
relax> structure.read_pdb(file='test.pdb',
    read_model=10, set_mol_name='CaM')
```

To load models 1 and 5 from the file `‘test.pdb’` as two different structures of the same model, type one of:

```
relax> structure.read_pdb('test.pdb',
    read_model=[1, 5], set_model_num=[1,
    1])
```

```
relax> structure.read_pdb('test.pdb',
    set_mol_name=['CaM_1', 'CaM_2'],
    read_model=[1, 5], set_model_num=[1,
    1])
```

To load the files `‘lactose_MCMM4_S1_1.pdb’`, `‘lactose_MCMM4_S1_2.pdb’`, `‘lactose_MCMM4_S1_3.pdb’` and `‘lactose_MCMM4_S1_4.pdb’` as models, type the following sequence of commands:

### 14.2.229 structure.read\_xyz



#### Synopsis

Reading structures from XYZ files.

#### Defaults

**structure.read\_xyz**(file=None, dir=None, read\_mol=None, set\_mol\_name=None, read\_model=None, set\_model\_num=None)

#### Keyword arguments

**file**: The name of the XYZ file.

**dir**: The directory where the file is located.

**read\_mol**: If set, only the given molecule(s) will be read. The molecules are numbered consecutively from 1. If unset, then all molecules will be loaded. By providing a list of numbers such as [1, 2], multiple molecules will be read.

**set\_mol\_name**: Set the names of the read molecules. If unset, then the molecules will be automatically labelled based on the file name or other information. This can either be a single name or a list of names.

**read\_model**: If set, only the given model number(s) from the PDB file will be read. Otherwise all models will be read. This can be a single number or list of numbers.

**set\_model\_num**: Set the model numbers of the loaded molecules. If unset, then the PDB model numbers will be preserved if they exist. This can be a single number or list of numbers.

#### Description

The XYZ files with different models, which defined as an ensemble of the same molecule but with different atomic positions, can be read into relax. If there are several molecules in one xyz file, please separate them into different files and then load them individually. Loading different models and different molecules is controlled by specifying the molecule number read, setting the molecule names, specifying which model to read, and setting the model numbers.

The setting of molecule names is used to name the molecules within the XYZ (within one model). If not set, then the molecules will be named after the file name, with the molecule number appended if more than one exists.

Note that relax will complain if it cannot work out what to do.

#### Prompt examples

To load all structures from the XYZ file 'test.xyz' in the directory '~/xyz', including all models and all molecules, type one of:

```
relax> structure.read_xyz('test.xyz', '~/xyz')
```

```
relax> structure.read_xyz(file='test.xyz',
                           dir='xyz')
```

To load the 10<sup>th</sup> model from the file 'test.xyz' and naming it 'CaM', use one of:

```
relax> structure.read_xyz('test.xyz',
                           read_model=10, set_mol_name='CaM')
```

```
relax> structure.read_xyz(file='test.xyz',
                           read_model=10, set_mol_name='CaM')
```

To load models 1 and 5 from the file 'test.xyz' as two different structures of the same model, type one of:

```
relax> structure.read_xyz('test.xyz',
                           read_model=[1, 5], set_model_num=[1,
                                                                1])
```

```
relax> structure.read_xyz('test.xyz',
                           set_mol_name=['CaM_1', 'CaM_2'],
                           read_model=[1, 5], set_model_num=[1,
                                                                1])
```

To load the files 'test\_1.xyz', 'test\_2.xyz', 'test\_3.xyz' and 'test\_4.xyz' as models, type the following sequence of commands:

```
relax> structure.read_xyz('test_1.xyz',
                           set_mol_name='test_1', set_model_num=1)
```

```
relax> structure.read_xyz('test_2.xyz',
                           set_mol_name='test_2', set_model_num=2)
```

```
relax> structure.read_xyz('test_3.xyz',
                           set_mol_name='test_3', set_model_num=3)
```

```
relax> structure.read_xyz('test_4.xyz',
                           set_mol_name='test_4', set_model_num=4)
```

---

**14.2.230 structure.rmsd****Synopsis**

Determine the RMSD between the models.

**Defaults**

`structure.rmsd(atom_id=None)`

**Keyword arguments**

`atom_id`: The atom identification string.

**Description**

This allows the root mean squared deviation (RMSD) between all models to be calculated.

The atom ID, which uses the same notation as the spin ID strings, can be used to restrict the RMSD calculation to certain molecules, residues, or atoms.

**Prompt examples**

To determine the RMSD, simply type:

```
relax> structure.rmsd()
```

---

**14.2.231 structure.rotate****Synopsis**

Rotate the internal structural object about the given origin by the rotation matrix.

**Defaults**

`structure.rotate(R=array([[ 1., 0., 0.], [ 0., 1., 0.], [ 0., 0., 1.]]), origin=None, model=None, atom_id=None)`

**Keyword arguments**

`R`: The rotation matrix in forwards rotation notation.

`origin`: The origin or pivot of the rotation.

`model`: The model to rotate (which if not set will cause all models to be rotated).

`atom_id`: The atom identification string.

**Description**

This is used to rotate the internal structural data by the given rotation matrix. If the origin is supplied, then this will act as the pivot of the rotation. Otherwise, all structural data will be rotated about the point [0, 0, 0]. The rotation can be restricted to one specific model.

### 14.2.232 structure.superimpose



#### Synopsis

Superimpose a set of models of the same structure.

#### Defaults

`structure.superimpose(models=None, method='fit to mean', atom_id=None, centroid=None)`

#### Keyword arguments

**models:** The list of models to superimpose.

**method:** The superimposition method.

**atom\_id:** The atom identification string.

**centroid:** The alternative position of the centroid.

#### Description

This allows a set of models of the same structure to be superimposed to each other. Two superimposition methods are currently supported:

**'fit to mean'** – All models are fit to the mean structure. This is the default and most accurate method for an ensemble description. It is an iterative method which first calculates a mean structure and then fits each model to the mean structure using the Kabsch algorithm. This is repeated until convergence.

**'fit to first'** – This is quicker but is not as accurate for an ensemble description. The Kabsch algorithm is used to rotate and translate each model to be superimposed onto the first model.

If the list of models is not supplied, then all models will be superimposed.

The atom ID, which uses the same notation as the spin ID strings, can be used to restrict the superimpose calculation to certain molecules, residues, or atoms. For example to only superimpose backbone heavy atoms in a protein, use the atom ID of '@N,C,CA,O', assuming those are the names of the atoms from the structural file.

By supplying the position of the centroid, an alternative position than the standard rigid body centre is used as the focal point of the superimposition. This allows, for example, the superimposition about a pivot point.

#### Prompt examples

To superimpose all sets of models, type one of:

```
relax> structure.superimpose()
```

```
relax> structure.superimpose(method='fit to mean')
```

To superimpose the models 1, 2, 3, 5 onto model 4, type:

```
relax> structure.superimpose(models=[4, 1, 2, 3, 5], method='fit to first')
```

To superimpose an ensemble of protein structures using only the backbone heavy atoms, type one of:

```
relax> structure.superimpose(atom_id='@N,C,CA,O')
```

```
relax> structure.superimpose(method='fit to mean', atom_id='@N,C,CA,O')
```

To superimpose model 2 onto model 3 using backbone heavy atoms, type one of:

```
relax> structure.superimpose([3, 2], 'fit to first', '@N,C,CA,O')
```

```
relax> structure.superimpose(models=[3, 2], method='fit to first', atom_id='@N,C,CA,O')
```





### 14.2.235 structure.write\_pdb



#### Synopsis

Writing structures to a PDB file.

#### Defaults

**structure.write\_pdb**(file=None, dir=None, model\_num=None, compress\_type=0, force=False)

#### Keyword arguments

**file**: The name of the PDB file.

**dir**: The directory where the file is located.

**model\_num**: Restrict the writing of structural data to a single model in the PDB file.

**compress\_type**: The type of compression to use when creating the file.

**force**: A flag which if set to True will cause any pre-existing files to be overwritten.

#### Description

This will write all of the structural data loaded in the current data pipe to be converted to the PDB format and written to file. Specifying the model number allows single models to be output.

The default behaviour of this function is to not compress the file. The compression can, however, be changed to either bzip2 or gzip compression. If the `.bz2` or `.gz` extension is not included in the file name, it will be added. This behaviour is controlled by the compression type which can be set to

**0** — No compression (no file extension).

**1** — bzip2 compression (`.bz2` file extension).

**2** — gzip compression (`.gz` file extension).

#### Prompt examples

To write all models and molecules to the PDB file `ensemble.pdb` within the directory `~/pdb`, type one of:



```
relax> structure.write_pdb('ensemble.pdb', '
~/pdb')
```

```
relax> structure.write_pdb(file='
ensemble.pdb', dir='pdb')
```

To write model number 3 into the new file `test.pdb`, use one of:

```
relax> structure.write_pdb('test.pdb',
model_num=3)
```

```
relax> structure.write_pdb(file='test.pdb',
model_num=3)
```

---

**14.2.236 sys\_info****Synopsis**

Display all system information relating to this version of relax.

**Defaults**

`sys_info()`

**Description**

This will display all of the relax, Python, python package and hardware information currently being used by relax. This is useful for seeing if all packages are up to date and if the correct software versions are being used. It is also very useful information for reporting relax bugs.

---

**14.2.237 value.copy****Synopsis**

Copy spin specific data values from one data pipe to another.

**Defaults**

`value.copy(pipe_from=None, pipe_to=None, param=None)`

**Keyword arguments**

`pipe_from`: The name of the pipe to copy from.

`pipe_to`: The name of the pipe to copy to.

`param`: The parameter to copy. Only one parameter may be selected.

**Description**

If this is used to change values of previously minimised parameters, then the minimisation statistics (chi-squared value, iteration count, function count, gradient count, and Hessian count) will be reset.

**Regular expression**

The python function ‘`match`’, which uses regular expression, is used to determine which data type to set values to, therefore various `data_type` strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

‘`[]`’ – A sequence or set of characters to match to a single character. For example, ‘`[sS]2`’ will match both ‘`S2`’ and ‘`s2`’.

‘`^`’ – Match the start of the string.

‘`$`’ – Match the end of the string. For example, ‘`^[sS]2$`’ will match ‘`s2`’ but not ‘`S2f`’ or ‘`s2s`’.

‘`.`’ – Match any character.

**'x\*'** – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.

**'.\*'** – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

## Model-free set details

Setting a parameter value may have no effect depending on which model-free model is chosen, for example if  $S_f^2$  values and  $S_s^2$  values are set but the run corresponds to model-free model 'm4' then, because these data values are not parameters of the model, they will have no effect.

Note that the  $R_{ex}$  values are scaled quadratically with field strength and should be supplied as a field strength independent value. Use the following formula to get the correct value:

$$\text{value} = \text{rex} / (2.0 * \pi * \text{frequency}) ** 2$$

where:

rex is the chemical exchange value for the current frequency.

$\pi$  is in the namespace of relax, ie just type ' $\pi$ '.

frequency is the proton frequency corresponding to the data.

## Model-free data type string matching patterns

Please see Table 14.4 on page 312.

## Reduced spectral density mapping set details

In reduced spectral density mapping, three values must be set prior to the calculation of spectral density values: the bond length, CSA, and heteronucleus type.

## Reduced spectral density mapping data type string matching patterns

Please see Table 14.9 on page 323.

## Consistency testing set details

In consistency testing, only four values can be set, the bond length, CSA, angle Theta ('orientation') and correlation time values. These must be set prior to the calculation of consistency functions.

## Consistency testing data type string matching patterns

Please see Table 14.10 on page 323.

## Relaxation curve fitting set details

Only three parameters can be set, the relaxation rate ( $R_x$ ), the initial intensity ( $I_0$ ), and the intensity at infinity ( $I_{inf}$ ). Setting the parameter  $I_{inf}$  has no effect if the chosen model is that of the exponential curve which decays to zero.

## Relaxation curve fitting data type string matching patterns

Please see Table 14.8 on page 323.

## N-state model set details

Setting parameters for the N-state model is a little different from the other type of analyses as each state has a set of parameters with the same names as the other states. To set the parameters for a specific state c (ranging from 0 for the first to N-1 for the last, the number c should be added to the end of the parameter name. So the Euler angle  $\gamma$  of the third state is specified using the string 'gamma2'.

## N-state model data type string matching patterns

Please see Table 14.24 on page 469.

The objects corresponding to the object names are lists (or arrays) with each element corresponding to each state.

## Relaxation dispersion curve fitting set details

Only three parameters can be set for either the slow- or the fast-exchange regime. For the slow-exchange regime, these parameters include the transversal relaxation rate for state A ( $R_{2A}$ ), the exchange rate from state A to state (k<sub>AB</sub>) and the chemical shift difference between states A and B ( $\Delta\omega$ ). For the fast-exchange regime, these include the transversal relaxation rate ( $R_2$ ), the chemical exchange contribution to  $R_2$  ( $R_{ex}$ ) and the exchange rate (k<sub>ex</sub>). Setting parameters for a non selected model has no effect.

Table 14.24: N-state model data type string matching patterns.

| Data type            | Object name      | Patterns                        |
|----------------------|------------------|---------------------------------|
| Probabilities        | 'probs'          | 'p0', 'p1', 'p2', ..., 'pN'     |
| Euler angle $\alpha$ | 'alpha'          | 'alpha0', 'alpha1', ...         |
| Euler angle $\beta$  | 'beta'           | 'beta0', 'beta1', ...           |
| Euler angle $\gamma$ | 'gamma'          | 'gamma0', 'gamma1', ...         |
| Bond length          | 'r'              | 'r\$' or '[Bb]ond[ -][Ll]ength' |
| Heteronucleus type   | 'heteronuc_type' | '^[Hh]eteronucleus\$'           |
| Proton type          | 'proton_type'    | '^[Pp]roton\$'                  |

## Relaxation dispersion curve fitting data type string matching patterns

Please see Table 14.7 on page 322.

### Prompt examples

To copy the CSA values from the data pipe 'm1' to 'm2', type:

```
relax> value.copy('m1', 'm2', 'csa')
```

## 14.2.238 value.display



### Synopsis

Display spin specific data values.

### Defaults

```
value.display(param=None, scaling=1.0)
```

### Keyword arguments

**param:** The parameter to display. Only one parameter may be selected.

**scaling:** The factor to scale parameters by.

### Description

The values corresponding to the given parameter will be displayed. The scaling argument can be used to scale the parameter values. This can be useful for example in the case of the model-free  $R_{ex}$  parameter to obtain the spectrometer dependent value from the omega\_ex field strength independent internal value. Or to scale correlation times from seconds down to nanosecond or picosecond timescales.

### Regular expression

The python function 'match', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'[]' – A sequence or set of characters to match to a single character. For example, '[sS]2' will match both 'S2' and 's2'.

'^' – Match the start of the string.

'\$' – Match the end of the string. For example, '^[Ss]2\$' will match 's2' but not 'S2f' or 's2s'.

'.' – Match any character.

'x\*' – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.

'.\*' – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

## Model-free data type string matching patterns

Please see Table 14.4 on page 312.

## Model-free parameter writing details

For the model-free theory, it is assumed that  $R_{ex}$  values are scaled quadratically with field strength. The values will seem quite small as they will be written out as a field strength independent value. Hence please use the following formula to convert the value to that expected for a given magnetic field strength:

$$R_{ex} = \text{value} * (2.0 * \pi * \text{frequency}) ** 2$$

The frequency is that of the proton in Hertz.

## Reduced spectral density mapping data type string matching patterns

Please see Table 14.9 on page 323.

## Consistency testing data type string matching patterns

Please see Table 14.10 on page 323.

## NOE calculation data type string matching patterns

Please see Table 14.6 on page 322.

## Relaxation curve fitting data type string matching patterns

Please see Table 14.8 on page 323.

## N-state model data type string matching patterns

Please see Table 14.24 on page 469.

The objects corresponding to the object names are lists (or arrays) with each element corresponding to each state.

## Relaxation dispersion curve fitting data type string matching patterns

Please see Table 14.7 on page 322.

## Prompt examples

To show all CSA values, type:

```
relax> value.display('csa')
```

To display the model-free  $R_{ex}$  values scaled to 600 MHz, type one of:

```
relax> value.display('rex', scaling=(2.0*pi*600e6)**2)
```

```
relax> value.display(param='rex', scaling=(2.0*pi*600e6)**2)
```

## 14.2.239 value.read




## Synopsis

Read spin specific data values from a file.

## Defaults

```
value.read(param=None, scaling=1.0, file=None, dir=
None, spin_id_col=None, mol_name_col=None,
res_num_col=None, res_name_col=None, spin_num_col=
None, spin_name_col=None, data_col=None, error_col=
None, sep=None, spin_id=None)
```

## Keyword arguments

**param:** The parameter. Only one parameter may be selected.

**scaling:** The factor to scale parameters by.

**file:** The name of the file containing the values.

**dir:** The directory where the file is located.

**spin\_id\_col:** The spin ID string column (an alternative to the mol, res, and spin name and number columns).

**mol\_name\_col:** The molecule name column (alternative to the spin\_id\_col).

**res\_num\_col:** The residue number column (alternative to the spin\_id\_col).

**res\_name\_col:** The residue name column (alternative to the spin\_id\_col).

**spin\_num\_col:** The spin number column (alternative to the spin\_id\_col).

**spin\_name\_col:** The spin name column (alternative to the spin\_id\_col).

**data\_col:** The RDC data column.

**error\_col:** The experimental error column.

**sep:** The column separator (the default is white space).

**spin\_id:** The spin ID string to restrict the loading of data to certain spin subsets.

## Description

The spin system can be identified in the file using two different formats. The first is the spin ID string column which can include the molecule name, the residue name and number, and the spin name and number. Alternatively the molecule name, residue number, residue name, spin number and/or spin name columns can be supplied allowing this information to be in separate columns. Note that the numbering of columns starts at one. The spin ID string can be used to restrict the reading to certain spin types, for example only  $^{15}\text{N}$  spins when only residue information is in the file.

If this is used to change values of previously minimised parameters, then the minimisation statistics (chi-squared value, iteration count, function count, gradient count, and Hessian count) will be reset.

## Regular expression

The python function 'match', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'[]' – A sequence or set of characters to match to a single character. For example, '[sS]2' will match both 'S2' and 's2'.

'^' – Match the start of the string.

'\$' – Match the end of the string. For example, '^ [Ss]2\$' will match 's2' but not 'S2f' or 's2s'.

'.' – Match any character.

'x\*' – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.

'.\*' – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

## Model-free set details

Setting a parameter value may have no effect depending on which model-free model is chosen, for example if  $S_f^2$  values and  $S_s^2$  values are set but the run corresponds to model-free model 'm4' then, because these data values are not parameters of the model, they will have no effect.

Note that the  $R_{ex}$  values are scaled quadratically with field strength and should be supplied as a field strength independent value. Use the following formula to get the correct value:

`value = rex / (2.0 * pi * frequency) ** 2` **N-state model set details**

where:

rex is the chemical exchange value for the current frequency.

$\pi$  is in the namespace of relax, ie just type ' $\pi$ '.

frequency is the proton frequency corresponding to the data.

## Model-free data type string matching patterns

Please see Table 14.4 on page 312.

## Reduced spectral density mapping set details

In reduced spectral density mapping, three values must be set prior to the calculation of spectral density values: the bond length, CSA, and heteronucleus type.

## Reduced spectral density mapping data type string matching patterns

Please see Table 14.9 on page 323.

## Consistency testing set details

In consistency testing, only four values can be set, the bond length, CSA, angle Theta ('orientation') and correlation time values. These must be set prior to the calculation of consistency functions.

## Consistency testing data type string matching patterns

Please see Table 14.10 on page 323.

## Relaxation curve fitting set details

Only three parameters can be set, the relaxation rate (Rx), the initial intensity (I0), and the intensity at infinity (Iinf). Setting the parameter Iinf has no effect if the chosen model is that of the exponential curve which decays to zero.

## Relaxation curve fitting data type string matching patterns

Please see Table 14.8 on page 323.

Setting parameters for the N-state model is a little different from the other type of analyses as each state has a set of parameters with the same names as the other states. To set the parameters for a specific state c (ranging from 0 for the first to N-1 for the last, the number c should be added to the end of the parameter name. So the Euler angle  $\gamma$  of the third state is specified using the string '`gamma2`'.

## N-state model data type string matching patterns

Please see Table 14.24 on page 469.

The objects corresponding to the object names are lists (or arrays) with each element corresponding to each state.

## Relaxation dispersion curve fitting set details

Only three parameters can be set for either the slow- or the fast-exchange regime. For the slow-exchange regime, these parameters include the transversal relaxation rate for state A (R2A), the exchange rate from state A to state (k<sub>AB</sub>) and the chemical shift difference between states A and B (dw). For the fast-exchange regime, these include the transversal relaxation rate (R<sub>2</sub>), the chemical exchange contribution to R<sub>2</sub> (R<sub>ex</sub>) and the exchange rate (kex). Setting parameters for a non selected model has no effect.

## Relaxation dispersion curve fitting data type string matching patterns

Please see Table 14.7 on page 322.

## Prompt examples

To load 15N CSA values from the file '`csa_values`' in the directory '`data`', where spins are only identified by residue name and number, type one of the following:

```
relax> value.read('csa', 'data/csa_value',
                 spin_id='@N')
```

```
relax> value.read('csa', 'csa_value', dir='
data', spin_id='@N')
```

```
relax> value.read(param='csa', file='
csa_value', dir='data', res_num_col=1,
res_name_col=2, data_col=3, error_col
=4, spin_id='@N')
```



## 14.2.240 value.set

◦

## Synopsis

Set spin specific data values.

## Defaults

**value.set**(val=None, param=None, spin\_id=None, error=False)

## Keyword arguments

**val**: The value(s).

**param**: The parameter(s).

**spin\_id**: The spin ID string to restrict value setting to.

**error**: A flag which if True will cause the error rather than parameter to be set.

## Description

If this function is used to change values of previously minimised results, then the minimisation statistics (chi-squared value, iteration count, function count, gradient count, and Hessian count) will be reset to None.

The value can be None, a single value, or an array of values while the parameter can be None, a string, or array of strings. The choice of which combination determines the behaviour of this function. The following table describes what occurs in each instance. In these columns, 'None' corresponds to None, '1' corresponds to either a single value or single string, and 'n' corresponds to either an array of values or an array of strings.

Please see Table 14.25 on page 474.

## Spin identification

If the spin ID is left unset, then this will be applied to all spins. If the data is global non-spin specific data, such as diffusion tensor parameters, supplying the spin identifier will terminate the program with an error.

## Regular expression

The python function 'match', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'[]' – A sequence or set of characters to match to a single character. For example, '[sS]2' will match both 'S2' and 's2'.

'^' – Match the start of the string.

'\$' – Match the end of the string. For example, '^[Ss]2\$' will match 's2' but not 'S2f' or 's2s'.

'.' – Match any character.

'x\*' – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.

'.\*' – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

## Model-free set details

Setting a parameter value may have no effect depending on which model-free model is chosen, for example if  $S_f^2$  values and  $S_s^2$  values are set but the run corresponds to model-free model 'm4' then, because these data values are not parameters of the model, they will have no effect.

Note that the  $R_{ex}$  values are scaled quadratically with field strength and should be supplied as a field strength independent value. Use the following formula to get the correct value:

$$\text{value} = \text{rex} / (2.0 * \pi * \text{frequency}) ** 2$$

where:

rex is the chemical exchange value for the current frequency.

$\pi$  is in the namespace of relax, ie just type ' $\pi$ '.

frequency is the proton frequency corresponding to the data.

Table 14.25: The value and parameter combination options for the value.set user function.

| Value | Param | Description  |
|-------|-------|--|
| None  | None  | This case is used to set the model parameters prior to minimisation or calculation. The model parameters are set to the default values.  |
| 1     | None  | Invalid combination.   |
| n     | None  | This case is used to set the model parameters prior to minimisation or calculation. The length of the val array must be equal to the number of model parameters. The parameters will be set to the corresponding number. |
| None  | 1     | The parameter matching the string will be set to the default value.  |
| 1     | 1     | The parameter matching the string will be set to the supplied number.  |
| n     | 1     | Invalid combination.   |
| None  | n     | Each parameter matching the strings will be set to the default values.   |
| 1     | n     | Each parameter matching the strings will be set to the supplied number.  |
| n     | n     | Each parameter matching the strings will be set to the corresponding number. Both arrays must be of equal length.  |

Table 14.26: Model-free default values.

| Data type                                      | Object name        | Value        |
|--|--------------------|--------------|
| Local $\tau_m$                                 | 'local_tm'         | 10 * 1e-9    |
| Order parameters $S^2$ , $S_f^2$ , and $S_s^2$ | 's2', 's2f', 's2s' | 0.8          |
| Correlation time $\tau_e$                      | 'te'               | 100 * 1e-12  |
| Correlation time $\tau_f$                      | 'tf'               | 10 * 1e-12   |
| Correlation time $\tau_s$                      | 'ts'               | 1000 * 1e-12 |
| Chemical exchange relaxation                   | 'rex'              | 0.0          |
| CSA  | 'csa'              | -172 * 1e-6  |

## Model-free data type string matching patterns

Please see Table 14.4 on page 312.

## Model-free default values

Please see Table 14.26 on page 474.

## Diffusion tensor set details

If the diffusion tensor has not been setup, use the more powerful function ‘`diffusion_tensor.init`’ to initialise the tensor parameters. This function cannot be used to initialise a diffusion tensor.

The units of the parameters are:

Inverse seconds for  $\tau_m$ .

Seconds for  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_a$ ,  $\mathfrak{D}_x$ ,  $\mathfrak{D}_y$ ,  $\mathfrak{D}_z$ ,  $\mathfrak{D}_{||}$ ,  $\mathfrak{D}_{\perp}$ .

Unitless for  $\mathfrak{D}_{ratio}$  and  $\mathfrak{D}_r$ .

Radians for all angles ( $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\theta$ ,  $\phi$ ).

When setting a diffusion tensor parameter, the residue number has no effect. As the internal parameters of spherical diffusion are  $\{\tau_m\}$ , spheroidal diffusion are  $\{\tau_m, \mathfrak{D}_a, \theta, \phi\}$ , and ellipsoidal diffusion are  $\{\tau_m, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$ , supplying geometric parameters must be done in the following way. If a single geometric parameter is supplied, it must be one of  $\tau_m$ ,  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_a$ ,  $\mathfrak{D}_r$ , or  $\mathfrak{D}_{ratio}$ . For the parameters  $\mathfrak{D}_{||}$ ,  $\mathfrak{D}_{\perp}$ ,  $\mathfrak{D}_x$ ,  $\mathfrak{D}_y$ , and  $\mathfrak{D}_z$ , it is not possible to determine how to use the currently set values together with the supplied value to calculate the new internal parameters. For spheroidal diffusion, when supplying multiple geometric parameters, the set must belong to one of

$$\begin{aligned} &\{\tau_m, \mathfrak{D}_a\}, \\ &\{\mathfrak{D}_{iso}, \mathfrak{D}_a\}, \\ &\{\tau_m, \mathfrak{D}_{ratio}\}, \\ &\{\mathfrak{D}_{||}, \mathfrak{D}_{\perp}\}, \\ &\{\mathfrak{D}_{iso}, \mathfrak{D}_{ratio}\}, \end{aligned}$$

where either  $\theta$ ,  $\phi$ , or both orientational parameters can be additionally supplied. For ellipsoidal diffusion, again when supplying multiple geometric parameters, the set must belong to one of

$$\begin{aligned} &\{\tau_m, \mathfrak{D}_a, \mathfrak{D}_r\}, \\ &\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r\}, \\ &\{\mathfrak{D}_x, \mathfrak{D}_y, \mathfrak{D}_z\}, \end{aligned}$$

where any number of the orientational parameters,  $\alpha$ ,  $\beta$ , or  $\gamma$  can be additionally supplied.

## Diffusion tensor parameter string matching patterns

Please see Table 14.3 on page 312.

## Diffusion tensor parameter default values

Please see Table 14.27 on page 476.

## Reduced spectral density mapping set details

In reduced spectral density mapping, three values must be set prior to the calculation of spectral density values: the bond length, CSA, and heteronucleus type.

## Reduced spectral density mapping data type string matching patterns

Please see Table 14.9 on page 323.

## Reduced spectral density mapping default values

These default values are found in the file ‘`physical_constants.py`’.

Please see Table 14.28 on page 476.

## Consistency testing set details

In consistency testing, only four values can be set, the bond length, CSA, angle Theta (‘`orientation`’) and correlation time values. These must be set prior to the calculation of consistency functions.

## Consistency testing data type string matching patterns

Please see Table 14.10 on page 323.

## Consistency testing default values

These default values are found in the file ‘`physical_constants.py`’.

Please see Table 14.29 on page 476.

Table 14.27: Diffusion tensor parameter default values.

| Data type | Object name | Value         |
|-----------|-------------|---------------|
| tm        | 'tm'        | $10 * 1e-9$   |
| Diso      | 'Diso'      | $1.666 * 1e7$ |
| Da        | 'Da'        | 0.0           |
| Dr        | 'Dr'        | 0.0           |
| Dx        | 'Dx'        | $1.666 * 1e7$ |
| Dy        | 'Dy'        | $1.666 * 1e7$ |
| Dz        | 'Dz'        | $1.666 * 1e7$ |
| Dpar      | 'Dpar'      | $1.666 * 1e7$ |
| Dper      | 'Dper'      | $1.666 * 1e7$ |
| Dratio    | 'Dratio'    | 1.0           |
| alpha     | 'alpha'     | 0.0           |
| beta      | 'beta'      | 0.0           |
| gamma     | 'gamma'     | 0.0           |
| theta     | 'theta'     | 0.0           |
| phi       | 'phi'       | 0.0           |

Table 14.28: Reduced spectral density mapping default values.

| Data type | Object name | Value         |
|-----------|-------------|---------------|
| CSA       | 'csa'       | $-172 * 1e-6$ |

Table 14.29: Consistency testing default values.

| Data type          | Object name      | Value               |
|--------------------|------------------|---------------------|
| Bond length        | 'r'              | $1.02 * 1e-10$      |
| CSA                | 'csa'            | $-172 * 1e-6$       |
| Heteronucleus type | 'heteronuc_type' | ' $^{15}\text{N}$ ' |
| Angle $\theta$     | 'proton_type'    | ' $^1\text{H}$ '    |
| Proton type        | 'orientation'    | 15.7                |
| Correlation time   | 'tc'             | $13 * 1e-9$         |

## Relaxation curve fitting set details

Only three parameters can be set, the relaxation rate ( $R_x$ ), the initial intensity ( $I_0$ ), and the intensity at infinity ( $I_{inf}$ ). Setting the parameter  $I_{inf}$  has no effect if the chosen model is that of the exponential curve which decays to zero.

## Relaxation curve fitting data type string matching patterns

Please see Table 14.8 on page 323.

## Relaxation curve fitting default values

These values are completely arbitrary as peak heights (or volumes) are extremely variable and the  $R_x$  value is a compensation for both the  $R_1$  and  $R_2$  values.

Please see Table 14.30 on page 478.

## N-state model set details

Setting parameters for the N-state model is a little different from the other type of analyses as each state has a set of parameters with the same names as the other states. To set the parameters for a specific state  $c$  (ranging from 0 for the first to  $N-1$  for the last, the number  $c$  should be added to the end of the parameter name. So the Euler angle  $\gamma$  of the third state is specified using the string ' $\gamma_{c3}$ '.

## N-state model data type string matching patterns

Please see Table 14.24 on page 469.

The objects corresponding to the object names are lists (or arrays) with each element corresponding to each state.

## N-state model default values

Please see Table 14.31 on page 478.

In this table,  $N$  is the total number of states and  $c$  is the index of a given state ranging from 0 to  $N-1$ . The default probabilities are all set to be equal whereas the angles are given a range of values so that no 2 states are equal at the start of optimisation.

Note that setting the probability for state  $N$  will do nothing as it is equal to one minus all the other probabilities.

## Relaxation dispersion curve fitting set details

Only three parameters can be set for either the slow- or the fast-exchange regime. For the slow-exchange regime, these parameters include the transversal relaxation rate for state A ( $R_{2A}$ ), the exchange rate from state A to state B ( $k_{AB}$ ) and the chemical shift difference between states A and B ( $\Delta\omega$ ). For the fast-exchange regime, these include the transversal relaxation rate ( $R_2$ ), the chemical exchange contribution to  $R_2$  ( $R_{ex}$ ) and the exchange rate ( $k_{ex}$ ). Setting parameters for a non selected model has no effect.

## Relaxation dispersion curve fitting data type string matching patterns

Please see Table 14.7 on page 322.

## Relaxation dispersion default values

Please see Table 14.32 on page 478.

## Prompt examples

To set the parameter values for the current data pipe to the default values, for all spins, type:

```
relax> value.set()
```

To set the parameter values of residue 10, which is in the current model-free data pipe 'm4' and has the parameters  $\{S^2, \tau_e, R_{ex}\}$ , the following can be used.  $R_{ex}$  term is the value for the first given field strength.

```
relax> value.set([0.97, 2.048*1e-9, 0.149],
                 spin_id=':10')
```

```
relax> value.set(val=[0.97, 2.048*1e-9, 0
                    .149], spin_id=':10')
```

To set the CSA value of all spins to the default value, type:

```
relax> value.set(param='csa')
```

To set the CSA value of all spins to -172 ppm, type:

```
relax> value.set(-172 * 1e-6, 'csa')
```

```
relax> value.set(val=-172 * 1e-6, param='csa
                ')
```

To set the NH bond length of all spins to 1.02 Å, type:

```
relax> value.set(1.02 * 1e-10, 'r')
```

```
relax> value.set(val=1.02 * 1e-10, param='r'
                )
```

Table 14.30: Relaxation curve fitting default values.

| Data type             | Object name | Value   |
|-----------------------|-------------|---------|
| Relaxation rate       | 'rx'        | 8.0     |
| Initial intensity     | 'i0'        | 10000.0 |
| Intensity at infinity | 'iinf'      | 0.0     |

Table 14.31: N-state model default values.

| Data type            | Object name                 | Value                 |
|----------------------|-----------------------------|-----------------------|
| Probabilities        | 'p0', 'p1', 'p2', ..., 'pN' | 1/N                   |
| Euler angle $\alpha$ | 'alpha0', 'alpha1', ...     | $(c+1) * \pi / (N+1)$ |
| Euler angle $\beta$  | 'beta0', 'beta1', ...       | $(c+1) * \pi / (N+1)$ |
| Euler angle $\gamma$ | 'gamma0', 'gamma1', ...     | $(c+1) * \pi / (N+1)$ |

Table 14.32: Relaxation dispersion default values.

| Data type   | Object name | Value       |
|---|-------------|-------------|
| Transversal relaxation rate (rad/s)   | 'r2'        | 15.0        |
| Transversal relaxation rate for state A (rad/s)                                   | 'r2a'       | 15.0        |
| Transversal relaxation rate for state B (rad/s)                                   | 'r2b'       | 15.0        |
| Population of state A   | 'pA'        | 0.5         |
| Population of state B   | 'pB'        | 0.5         |
| Population of state C   | 'pC'        | 0.5         |
| The pA.pB.dw**2 parameter (ppm <sup>2</sup> )                                     | 'phi_ex'    | 5.0         |
| The pA.pB.dw**2 parameter of state B (ppm <sup>2</sup> )                          | 'phi_ex_B'  | 5.0         |
| The pA.pB.dw**2 parameter of state C (ppm <sup>2</sup> )                          | 'phi_ex_C'  | 5.0         |
| The pA.dw**2 parameter (ppm <sup>2</sup> )  | 'padw2'     | 1.0         |
| Chemical shift difference between states A and B (ppm)                            | 'dw'        | 0.0         |
| Chemical shift difference between states A and B for 3-site exchange (ppm)        | 'dw_AB'     | 0.0         |
| Chemical shift difference between states A and C for 3-site exchange (ppm)        | 'dw_AC'     | 0.0         |
| Chemical shift difference between states B and C for 3-site exchange (ppm)        | 'dw_BC'     | 0.0         |
| Proton chemical shift difference between states A and B (ppm)                     | 'dwH'       | 0.0         |
| Proton chemical shift difference between states A and B for 3-site exchange (ppm) | 'dwH_AB'    | 0.0         |
| Proton chemical shift difference between states A and C for 3-site exchange (ppm) | 'dwH_AC'    | 0.0         |
| Proton chemical shift difference between states B and C for 3-site exchange (ppm) | 'dwH_BC'    | 0.0         |
| Exchange rate (rad/s)   | 'kex'       | 10000.0     |
| Exchange rate between sites A and B for 3-site exchange (rad/s)                   | 'kex_AB'    | 10000.0     |
| Exchange rate between sites A and C for 3-site exchange (rad/s)                   | 'kex_AC'    | 10000.0     |
| Exchange rate between sites B and C for 3-site exchange (rad/s)                   | 'kex_BC'    | 10000.0     |
| Exchange rate between sites A and B (rad/s)                                       | 'kB'        | 10000.0     |
| Exchange rate between sites A and C (rad/s)                                       | 'kC'        | 10000.0     |
| Time of exchange (s/rad)  | 'tex'       | 1.0/10000.0 |
| Exchange rate from state A to state B (rad/s)                                     | 'k_AB'      | 10000.0     |
| Exchange rate from state B to state A (rad/s)                                     | 'k_BA'      | 10000.0     |

To set both the bond length and the CSA value to the default values, type:

```
relax> value.set(param=['r', 'csa'])
```

To set both  $\tau_f$  and  $\tau_s$  to 100 ps, type:

```
relax> value.set(100e-12, ['tf', 'ts'])
```

```
relax> value.set(val=100e-12, param=['tf', 'ts'])
```

To set the  $S^2$  and  $\tau_e$  parameter values of residue 126, Ca spins to 0.56 and 13 ps, type:

```
relax> value.set([0.56, 13e-12], ['s2', 'te'], ':126@Ca')
```

```
relax> value.set(val=[0.56, 13e-12], param=['s2', 'te'], spin_id=':126@Ca')
```

```
relax> value.set(val=[0.56, 13e-12], param=['s2', 'te'], spin_id=':126@Ca')
```

## 14.2.241 value.write



### Synopsis

Write spin specific data values to a file.

### Defaults

**value.write**(param=None, file=None, dir=None, scaling=1.0, comment=None, bc=False, force=False)

### Keyword arguments

**param**: The parameter.

**file**: The name of the file.

**dir**: The directory name.

**scaling**: The factor to scale parameters by.

**comment**: Text which will be added to the start of the file as comments. All lines will be prefixed by '# '.

**bc**: A flag which if True will cause the back calculated values to be written to file rather than the actual data.

**force**: A flag which, if set to True, will cause the file to be overwritten.

### Description

The values corresponding to the given parameter will be written to file. The scaling argument can be used to scale the parameter values. This can be useful for example in the case of the model-free  $R_{ex}$  parameter to obtain the spectrometer dependent value from the `omega_ex` field strength independent internal value. Or to scale correlation times from seconds down to nanosecond or picosecond timescales.

### Regular expression

The python function 'match', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'[]' – A sequence or set of characters to match to a single character. For example, '[sS]2' will match both 'S2' and 's2'.

'^' – Match the start of the string.

'\$' – Match the end of the string. For example, '^[sS]2\$' will match 's2' but not 'S2f' or 's2s'.

'.' – Match any character.

'x\*' – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.

'.\*' – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

## Model-free data type string matching patterns

Please see Table 14.4 on page 312.

## Model-free parameter writing details

For the model-free theory, it is assumed that  $R_{ex}$  values are scaled quadratically with field strength. The values will seem quite small as they will be written out as a field strength independent value. Hence please use the following formula to convert the value to that expected for a given magnetic field strength:

$$R_{ex} = \text{value} * (2.0 * \pi * \text{frequency}) ** 2$$

The frequency is that of the proton in Hertz.

## Reduced spectral density mapping data type string matching patterns

Please see Table 14.9 on page 323.

## Consistency testing data type string matching patterns

Please see Table 14.10 on page 323.

## NOE calculation data type string matching patterns

Please see Table 14.6 on page 322.

## Relaxation curve fitting data type string matching patterns

Please see Table 14.8 on page 323.

## N-state model data type string matching patterns

Please see Table 14.24 on page 469.

The objects corresponding to the object names are lists (or arrays) with each element corresponding to each state.

## Relaxation dispersion curve fitting data type string matching patterns

Please see Table 14.7 on page 322.

## Prompt examples

To write the CSA values to the file 'csa.txt', type one of:

```
relax> value.write('csa', 'csa.txt')
```

```
relax> value.write(param='csa', file='csa.txt')
```

To write the NOE values to the file 'noe', type one of:

```
relax> value.write('noe', 'noe.out')
```

```
relax> value.write(param='noe', file='noe.out')
```

```
relax> value.write(param='noe', file='noe.out')
```

```
relax> value.write(param='noe', file='noe.out', force=True)
```

To write the model-free  $R_{ex}$  values scaled to 600 MHz to the file 'rex\_600', type one of:

```
relax> value.write('rex', 'rex_600', scaling=(2.0*pi*600e6)**2)
```

```
relax> value.write(param='rex', file='rex_600', scaling=(2.0*pi*600e6)**2)
```



---

### 14.2.242 vmd.view

#### Synopsis

View the structures loaded into the relax data store using VMD.

#### Defaults

`vmd.view()`

#### Description

This will launch VMD with all of the structures loaded into the relax data store.

#### Prompt examples

```
relax> vmd.view()
```



## Chapter 15

# Licence

### 15.1 Copying, modification, sublicencing, and distribution of relax

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Version 3, 29 June 2007

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```

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